## Study on Libration Points of the Sun and the Interstellar Medium for Interstellar Travel

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## 1 INTRODUCTION

The subject of the present study is the analysis of the applicability of recent advances in transfer trajectory design in multi-body systems to the exploration of stars in the Solar Neighborhood. The new design techniques make use of Dynamical Systems Theory and have been recently given some publicity under the general term of "Interplanetary Superhighways" (Koon et al., 2001; Howell et al., 1997). The main advantage of these new techniques is that they exploit the dynamical characteristics of multi-body systems to identify transfer trajectories requiring very low energy input, which would otherwise go unobserved if classical two-body transfer techniques were applied.
The approach adopted in this study has been to first identify the dynamical character of the possible targets of stellar exploration both as subsystems (double, triple, etc. stellar systems) and possibly in combination with our Sun. The second part of the study was then addressed to investigating the applicability of the new techniques to the different contexts.
The study was conducted over a period of two months during April and May, 2004. Given this constraint, the study constitutes only a first attempt at the definition of analysis and design techniques applicable to interstellar exploration carried out using only the software tools accessible to the study team and not requiring further major development.
The first part of this report addresses the preliminary phase in which information about the Solar Neighborhood has been collected. This part has been particularly time consuming since the data sources are many and generally incomplete in several respects, making it necessary to merge information of differing quality, scope and accuracy. It must be realized, however, that stellar catalogues are a difficult business, since they have to extract information from the original observation records, published papers, other repertories, etc. which themselves suffer from the same inconsistencies and limitations just mentioned. This first task has at times required our intervention in terms of making the data consistent. This may happen for instance when the masses and the periods of double stars have to be merged from different sources, in which case either the periods must be recomputed or the masses redetermined, under the assumption that the mutual distance (or semimajor axis) is correct.
A list of all stars and star systems within a sphere of 6.7 parsecs has been produced. All binary, triple, quadruple and quintuple systems present in these first 77 objects have been identified. Specific information regarding the dynamical characteristics of 13 binaries, 2 triples and 2 planetary systems have been collected and discussed. In order to generate the initial conditions for numerical integration of the orbits of the individual stars and star systems, the position and velocity information have been appropriately processed and transformed into the required form. This finally brought to an understanding of the dynamical behaviour of the stars in the Solar Neighbourhood.
The second phase of the study addresses the design of transfer orbits to the nearby stars or star systems as well as transfers within target multi-body systems. The analysis is carried out with a view to the applicability in each case of the known paradigms, like the Circular Restricted Three-Body Problem, the Problem of the Two Fixed Centers (Whittaker, 1937), etc., clarifying when these are indeed an acceptable approximation and when the models have to be left aside and new directions explored.

Space missions to the stars have been considered for a long time and studies have been carried out even recently tryng to define the actual possibilities for the exploration of the Solar Neighborhood (McNutt, 2003). One of the fundamental questions, apart from the necessary technological advancements, is the limitations to be imposed on the length of the mission. Current wisdom holds that an acceptable duration is limited to a few human generations. This makes it possible for the designers and all involved in planning the mission to enjoy the wealth of information sent back to Earth by an automatic probe.

## 2 THE SOLAR NEIGHBOURHOOD

### 2.1 Catalogue comparisons: completeness of the data, accuracies, magnitude limits, sky coverage

For the purpose of the present study we define the solar neighbourhood as the volume of space centered at the Sun and occupied by stars with parallax $>150$ mas (i.e. within 6.7 pc from the Sun) (approximately represented in Figure 1).


Figure 1: The stars within 20 ly (= 6.13 parsecs) from the Sun (Hipparcos and Tycho Catalogue, $3^{\text {rd }}$ Gliese Catalogue).

We looked for a star catalogue capable of providing the most complete and accurate information for the largest number of stars within the given volume. In particular we were interested in: positional information (coordinates, parallaxes), kinematic data (proper motions, radial velocities) and stellar masses. We compared the following catalogues:

- Nearby Stars, Preliminary 3rd Version (Jahreiss \& Gliese, 1985; Gliese \& Jahreiss, 1989; Jahreiss \& Gliese, 1989; Gliese \& Jahreiss, 1991a; Gliese \& Jahreiss, 1991b; Jahreiss \& Gliese, 1993) which contains photometric, astrometric and spectroscopic data for stars within 25 parsecs of the Sun. It largely depends on a preliminary version (Spring 1989) of the new General Catalogue of Trigonometric Parallaxes (YPC) prepared by Dr. William F. van Altena (Yale University). The Gliese Catalogue lists 122 objects in the parallax range > 150 mas.
- Hipparcos \& Tycho: the Hipparcos satellite mission provided for 118,300 pre-selected stars the five astrometric parameters with an average formal error of 1.6 milli arcsec. For a full description of the data products the reader is referred to ESA (1997) and to the review published by van Leeuwen (1997). Here we would like to recall the limiting magnitude ( $\mathrm{V} \approx 12.4 \mathrm{mag}$ ) and the completeness (up to $V=7.3-9.0 \mathrm{mag}$ ) of the main (Hipparcos) catalogue. The number of entries in the parallax range $>150$ mas is 84 .
- Zakhozhaj Catalogue of Nearest stars until 10 pc (Zakhozhaj, 1998): it presents the stars with trigonometric, photometric and spectral parallaxes > 100 mas. The catalogue also contains data on components of multiple visual systems, on components of spectral-binary systems and on invisible components with masses $>0.08$ solar masses. The catalogue provides the main characteristics of stars such as the positions, proper motions, radial velocities, parallaxes, photometrical data and also masses and radii of stars. The completeness of the catalogue is about $70 \%$. It lists 122 objects with parallax larger than 150 mas. We were unable to identify the source of the data and the information on the errors.
- NStars Database (Henry et al., 2000): the NStars research project was initiated in 1998 and is based at the Northern Arizona University. Its objective is to provide the most current, complete and accurate source of scientific data about all stellar objects within the radius of 25 parsecs. At present this includes approximately 2,600 stars. The RECONS programme is part of the NStars project and constitutes the most complete dataset of stars within 10 parsecs of the Sun. The information listed in the RECONS database is obtained by combining data from different catalogues and authors, most noticeably: the Hipparcos Catalogue (ESA, 1997), the Yale Parallax Catalog (Van Altena \& Hoffleit, 1996), Söderhjelm (1999) and Tinney (1996) for the parallaxes; other quantities (proper motions, masses) are derived from the works published by Ducourant et al. (1998), Geballe et al. (2002), Scholz et al. (2003) and by the work of the RECONS research group itself. The RECONS database contains 140 objects closer than 6.7 pc .

The comparison among the above catalogues and databases suggested the adoption of the NStars Database to collect positions, parallaxes, proper motions and mass data, and the Gliese Catalogue for radial velocities. We compiled a database (see Table 1) that we used for all later computations. Missing data (always radial velocities and/or mass determinations) in Table 1 are replaced by large numbers (999) for computational reasons, flagged in red and excluded from subsequent reductions. Errors are explicitly reported only for parallax determinations; for the proper motions one should recover the sources of each entry among those cited above; the estimated mass (in units of the Sun's mass) of a star is based upon the $\mathrm{M}_{\mathrm{V}}$ (absolute magnitude) value and the empirical mass-luminosity relations of Henry \& McCarthy (1993): when an object is too faint for the relations to be applicable (fainter than $\mathrm{Mv}=20.00$ ) a mass of 0.5 is always listed (this is typically the case of white dwarfs).

The NStars Project web page offers some statistics regarding the astrometric properties of the nearby stars which we report in Figure 2, Figure 3, Figure 4 and Figure 5.
We have not been able to identify the typical or the average standard errors of the radial velocities published by the Gliese Catalogue.

| GLIIESE | HIP | common name | n | $\alpha$ (J2000.0) | $\delta$ (J2000.0) | $\Pi$ | $\Delta \Pi$ | $\mu$ | PA | M | $\mathbf{R}_{V}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | ( hms ) | ( ${ }^{\circ}{ }^{\prime \prime}$ ) | (") | (") | ("/yr) | ${ }^{\circ}$ ) | $\left(\mathrm{M}_{\text {sun }}\right)$ | (Km/s) |
| - |  | SUN | 1 | - | - | - |  | - | - | 1.000 | - |
| GL 551 | 70890 | Proxima Centauri | 1 | 142943.0 | -62 4046 | 0.77199 | 0.00225 | 3.853 | 281.5 | 0.107 | -16.000 |
| GL 559 | 71683 | alpha Centauri A | 2 | 143936.5 | -60 5002 | 0.74723 | 0.00117 | 3.710 | 277.5 | 1.144 | -26.200 |
| GL 559 | 71681 | alpha Centauri B | 2 | 143935.1 | -6050 14 | 0.74723 | 0.00117 | 3.724 | 284.8 | 0.916 | -18.100 |
| GL 699 | 87937 | Barnard's Star | 1 | 175748.5 | 044136 | 0.54698 | 0.00100 | 10.358 | 355.6 | 0.166 | -111.000 |
| GL 406 |  | Wolf 359 | 1 | 105629.2 | 070053 | 0.41910 | 0.00210 | 4.696 | 234.6 | 0.092 | 13.000 |
| GL 411 | 54035 | Lalande 21185 | 1 | 110320.2 | 355812 | 0.39342 | 0.00070 | 4.802 | 186.9 | 0.464 | -84.300 |
| GL 244 | 32349 | Sirius A | 2 | 064508.9 | -164258 | 0.38002 | 0.00128 | 1.339 | 204.1 | 1.991 | -9.400 |
| GL 244 |  | Sirius B | 2 | 064508.9 | -16 4258 | 0.38002 | 0.00128 | 1.339 | 204.1 | 0.500 | -9.400 |
| GL 65 |  | UV Ceti | 2 | 013901.3 | -17 5701 | 0.37370 | 0.00270 | 3.368 | 80.4 | 0.109 | 29.000 |
| GL 65 |  | BL Ceti | 2 | 013901.3 | -175701 | 0.37370 | 0.00270 | 3.368 | 80.4 | 0.102 | 32.000 |
| GL 729 | 92403 | Ross 154 | 1 | 184949.4 | -23 5010 | 0.33690 | 0.00178 | 0.666 | 106.8 | 0.171 | -12.100 |
| GL 905 |  | Ross 248 | 1 | 234154.7 | 441030 | 0.31600 | 0.00110 | 1.617 | 177.0 | 0.121 | -77.700 |
| GL 144 | 16537 | epsilon Eridani A | 2 | 033255.8 | -09 2730 | 0.30999 | 0.00079 | 0.977 | 271.1 | 0.850 | 16.900 |
| GJ 144 |  | epsilon Eridani B | 2 | 033255.8 | -09 2730 | 0.30999 | 0.00079 | 0.977 | 271.1 | 999.000 | 16.900 |
| GJ 887 | 114046 | Lacaille 9352 | 1 | 230552.0 | -35 5111 | 0.30364 | 0.00087 | 6.896 | 78.9 | 0.529 | 9.500 |
| GL 447 | 57548 | Ross 128 | 1 | 114744.4 | 004816 | 0.29872 | 0.00135 | 1.361 | 153.6 | 0.156 | -31.100 |
| GL 866 |  | EZ Aquarii A | 3 | 223833.4 | -151807 | 0.28950 | 0.00440 | 3.254 | 46.6 | 0.105 | -60.000 |
| GL 866 |  | EZ Aquarii B | 3 | 223833.4 | -151807 | 0.28950 | 0.00440 | 3.254 | 46.6 | 0.106 | -60.000 |
| GL 866 |  | EZ Aquarii C | 3 | 223833.4 | -151807 | 0.28950 | 0.00440 | 3.254 | 46.6 | 0.095 | -60.000 |
| GL 280 | 37279 | Procyon A | 2 | 073918.1 | 051330 | 0.28605 | 0.00081 | 1.259 | 214.7 | 1.569 | -4.000 |
| GL 280 |  | Procyon B | 2 | 073918.1 | 051330 | 0.28605 | 0.00081 | 1.259 | 214.7 | 0.500 | -4.000 |
| GL 820 | 104214 | 61 Cygni A | 2 | 210653.9 | 384458 | 0.28604 | 0.00056 | 5.281 | 51.9 | 0.703 | -64.800 |
| GL 820 | 104217 | 61 Cygni B | 2 | 210655.3 | 384431 | 0.28604 | 0.00056 | 5.172 | 52.6 | 0.630 | -64.300 |
| GL 725 | 91768 | DM+59 1915 A | 2 | 184246.7 | 593749 | 0.28300 | 0.00169 | 2.238 | 323.6 | 0.351 | -0.800 |
| GL 725 | 91772 | DM+59 1915 B | 2 | 184246.9 | 593737 | 0.28300 | 0.00169 | 2.313 | 323.0 | 0.259 | 1.200 |
| GL 15 | 1475 | GX Andromedae | 2 | 001822.9 | 440123 | 0.28059 | 0.00095 | 2.918 | 81.9 | 0.486 | 12.000 |
| GL 15 |  | GQ Andromedae | 2 | 001822.9 | 440123 | 0.28059 | 0.00095 | 2.918 | 81.9 | 0.163 | 11.300 |
| GL 845 | 108870 | Eps Indi A | 3 | 220321.7 | -564710 | 0.27584 | 0.00069 | 4.704 | 122.7 | 0.766 | -40.400 |
| GL 845 |  | Eps Indi B | 3 | 220410.5 | -564658 | 0.27584 | 0.00069 | 4.823 | 121.1 | 0.044 | -40.400 |
| GL 845 |  | Eps Indi C | 3 | 220410.5 | -564658 | 0.27584 | 0.00069 | 4.823 | 121.1 | 0.028 | -40.400 |
| GJ 1111 |  | DX Cancri | 1 | 082949.5 | 264637 | 0.27580 | 0.00300 | 1.29 | 242.2 | 0.087 | -5.000 |
| GL 71 | 8102 | Tau Ceti | 1 | 014404.1 | -15 5615 | 0.27439 | 0.00076 | 1.922 | 296.4 | 0.921 | -17.000 |
| GJ 1061 |  | RECONS 1 | 1 | 033600.0 | -443046 | 0.27200 | 0.00140 | 0.814 | 117.3 | 0.113 | -20.000 |
| GJ 54.1 |  | YZ Ceti | 1 | 011230.6 | -165957 | 0.26884 | 0.00295 | 1.372 | 61.9 | 0.136 | 28.000 |
| GJ 273 | 36208 | Luyten's Star | 1 | 072724.5 | 051333 | 0.26376 | 0.00125 | 3.738 | 171.2 | 0.257 | 18.200 |
| GJ 191 | 24186 | Kapteyn's Star | 1 | 051140.6 | -450106 | 0.25527 | 0.00086 | 8.67 | 131.4 | 0.393 | 245.500 |
| GJ 825 | 105090 | AX Microscopium | 1 | 211715.3 | -385203 | 0.25343 | 0.00112 | 3.455 | 250.6 | 0.600 | 28.200 |
| GJ 860 | 110893 | Kruger 60 A | 2 | 222759.5 | 574145 | 0.24806 | 0.00139 | 0.99 | 241.6 | 0.279 | -33.300 |
| GJ 860 |  | Kruger 60 B | 2 | 222759.5 | 574145 | 0.24806 | 0.00139 | 0.99 | 241.6 | 0.160 | -31.700 |
| DEN1048-3956 |  | RECONS 2 | 1 | 104814.7 | -39 5606 | 0.24790 | 0.00240 | 1.515 | 229.6 | 0.113 | 999.000 |
| GJ 234 | 30920 | Ross 614 A | 2 | 062923.4 | -024850 | 0.24434 | 0.00201 | 0.93 | 131.7 | 0.170 | 16.700 |
| GJ 234 |  | Ross 614 B | 2 | 062923.4 | -024850 | 0.24434 | 0.00201 | 0.93 | 131.7 | 0.097 | 16.700 |
| GJ 628 | 80824 | Wolf 1061 | 1 | 163018.1 | -1239 45 | 0.23601 | 0.00167 | 1.189 | 184.5 | 0.261 | -13.000 |
| GJ 35 | 3829 | WD 0046+051 | 1 | 004909.9 | 052319 | 0.23188 | 0.00179 | 2.978 | 155.5 | 0.500 | 54.000 |
| GJ 1 |  | - | 1 | 000524.4 | -372127 | 0.22920 | 0.00107 | 6.1 | 112.5 | 0.481 | 22.900 |
| GJ 473 |  | Wolf 424 A | 2 | 123317.2 | 090115 | 0.22790 | 0.00460 | 1.811 | 277.4 | 0.118 | -553.700 |
| GJ 473 |  | Wolf 424 B | 2 | 123317.2 | 090115 | 0.22790 | 0.00460 | 1.811 | 277.4 | 0.118 | -553.700 |
| GJ 83.1 |  | TZ Arietis | 1 | 020013.2 | 130308 | 0.22480 | 0.00290 | 2.097 | 147.8 | 0.140 | -31.000 |
| LHS 288 |  | - | 1 | 104431.8 | -611138 | 0.22250 | 0.01130 | 1.657 | 348.1 | 0.105 | 999.000 |
| GJ 687 |  | - | 1 | 173625.9 | 682021 | 0.22049 | 0.00082 | 1.309 | 194.2 | 0.390 | -23.200 |
| LHS 292 |  | - | 1 | 104812.6 | -1120 14 | 0.22030 | 0.00360 | 1.644 | 158.5 | 0.083 | -7.000 |
| GJ 674 |  | - | 1 | 172839.9 | -4653 43 | 0.22025 | 0.00159 | 1.05 | 146.9 | 0.361 | -10.200 |
| GJ 1245 |  | G 208-044 A | 3 | 195354.2 | 442455 | 0.22020 | 0.00100 | 0.731 | 143.1 | 0.114 | 999.000 |
| GJ 1245 |  | G 208-045 | 3 | 195355.2 | 442456 | 0.22020 | 0.00100 | 0.731 | 143.1 | 0.104 | 999.000 |
| GJ 1245 |  | G 208-044 B | 3 | 195354.2 | 442455 | 0.22020 | 0.00100 | 0.731 | 143.1 | 0.074 | 999.000 |
| GJ 440 |  | WD 1142-645 | 1 | 114542.9 | -64 5029 | 0.21657 | 0.00201 | 2.688 | 97.4 | 0.500 | 999.000 |
| GJ 1002 |  | - | 1 | 000643.8 | -0732 22 | 0.21300 | 0.00360 | 2.041 | 203.6 | 0.109 | -42.000 |
| GJ 876 | 113020 | Ross 780 | 3 | 225316.7 | -141549 | 0.21259 | 0.00196 | 1.174 | 125.1 | 0.273 | -1.500 |
| GJ 876 |  | - | 3 | 225316.7 | -141549 | 0.21259 | 0.00196 | 1.174 | 125.1 | 999.000 | $-1.500$ |
| GJ 876 |  | - | 3 | 225316.7 | -141549 | 0.21259 | 0.00196 | 1.174 | 125.1 | 999.000 | -1.500 |
| GJ 412 |  | - | 2 | 110528.6 | 433136 | 0.20602 | 0.00108 | 4.511 | 282.1 | 0.483 | 68.800 |
| GJ 412 |  | WX Ursae Majoris | 2 | 110530.4 | 433118 | 0.20602 | 0.00108 | 4.531 | 281.9 | 0.099 | 68.800 |
| GJ 380 |  | - | 1 | 101122.1 | 492715 | 0.20581 | 0.00067 | 1.452 | 249.7 | 0.642 | -25.400 |


| GJ 388 |  | - | 1 | 101936.4 | 195210 | 0.20460 | 0.00280 | 0.506 | 264.0 | 0.393 | 12.300 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| GJ 832 |  | - | 1 | 213334.0 | -49 0032 | 0.20278 | 0.00132 | 0.819 | 183.2 | 0.503 | 4.100 |
| LP 944-020 |  | - | 1 | 033935.2 | -35 2541 | 0.20140 | 0.00420 | 0.439 | 47.6 | 0.066 | 999.000 |
| GJ 682 |  | - | 1 | 173703.7 | -44 1909 | 0.19965 | 0.00230 | 1.176 | 217.1 | 0.213 | -60.000 |
| GJ 166 | 19849 | omicron 2 Eridani | 3 | 041516.3 | -0739 10 | 0.19900 | 0.00077 | 4.088 | 213.2 | 0.887 | -42.700 |
| GJ 166 |  | - | 3 | 041522.0 | -073935 | 0.19900 | 0.00077 | 4.073 | 212.4 | 0.500 | -21.000 |
| GJ 166 |  | - | 3 | 041522.0 | -073935 | 0.19900 | 0.00077 | 4.073 | 212.4 | 0.195 | -45.900 |
| GJ 873 | 112460 | EV Lacertae | 1 | 224649.7 | 442002 | 0.19804 | 0.00161 | 0.841 | 236.9 | 0.285 | -0.500 |
| GJ 702 | 88601 | 70 Ophiuchi A | 2 | 180527.3 | 023000 | 0.19596 | 0.00087 | 0.971 | 172.6 | 0.924 | -6.900 |
| GJ 702 |  | 70 Ophiuchi B | 2 | 180527.3 | 023000 | 0.19596 | 0.00087 | 0.971 | 172.6 | 0.701 | -10.000 |
| GJ 768 | 97649 | Altair | 1 | 195047.0 | 085206 | 0.19497 | 0.00086 | 0.661 | 54.3 | 1.710 | -26.100 |
| GJ 1116 |  | EI Cancri | 2 | 085814.9 | 194543 | 0.19120 | 0.00250 | 0.874 | 267.7 | 0.108 | -34.000 |
| GJ 1116 |  | - | 2 | 085814.9 | 194549 | 0.19120 | 0.00250 | 0.874 | 267.7 | 0.095 | -34.000 |
| G 099-049 |  | - | 1 | 060003.6 | 024220 | 0.18620 | 0.01010 | 0.241 | 108.0 | 0.195 | 999.000 |
| GJ 445 |  | - | 1 | 114741.4 | 784128 | 0.18584 | 0.00139 | 0.885 | 57.1 | 0.240 | -112.200 |
| GJ 1005 | 1242 | - | 2 | 001528.1 | -160802 | 0.18582 | 0.00297 | 0.955 | 130.3 | 0.177 | -29.000 |
| GJ 1005 |  | - | 2 | 001528.1 | -160802 | 0.18582 | 0.00297 | 0.955 | 130.3 | 0.105 | -29.000 |
| GJ 526 |  | - | 1 | 134543.8 | 145329 | 0.18421 | 0.00116 | 2.298 | 129.3 | 0.526 | 16.100 |
| LHS 1723 |  | RECONS 3 | 1 | 050157.0 | -06 5647 | 0.18270 | 0.00330 | 0.786 | 226.7 | 0.157 | 999.000 |
| LP 816-060 |  | - | 1 | 205233.0 | -165829 | 0.18215 | 0.00368 | 0.308 | 275.7 | 0.193 | 999.000 |
| GJ 169.1 | 21088 | Stein 2051 | 2 | 043111.8 | 585838 | 0.18063 | 0.00078 | 2.427 | 147.6 | 0.224 | 17.000 |
| GJ 169.1 |  | - | 2 | 043111.8 | 585838 | 0.18063 | 0.00078 | 2.427 | 147.6 | 0.500 | 17.000 |
| GJ 251 |  | - | 1 | 065449.0 | 331605 | 0.17958 | 0.00161 | 0.831 | 241.3 | 0.334 | 999.000 |
| 2MA1835+3259 |  | - | 1 | 183537.9 | 325954 | 0.17650 | 0.00050 | 0.759 | 186.1 | 999.000 | 999.000 |
| GJ 754 |  | - | 1 | 192048.0 | -453327 | 0.17520 | 0.01010 | 2.945 | 167.3 | 0.158 | 16.000 |
| GJ 205 | 25878 | Wolf 1453 | 1 | 053127.4 | -03 4038 | 0.17517 | 0.00105 | 2.228 | 160.0 | 0.566 | 8.500 |
| GJ 764 | 96100 | sigma Draconis | 1 | 193221.6 | 693940 | 0.17359 | 0.00041 | 1.839 | 161.0 | 0.892 | 28.200 |
| GJ 229 | 29295 | - | 2 | 061034.6 | -215153 | 0.17317 | 0.00110 | 0.727 | 190.9 | 0.556 | 5.200 |
| GJ 229 |  | - | 2 | 061034.6 | -215153 | 0.17317 | 0.00110 | 0.727 | 190.9 | 0.050 | 5.200 |
| GJ 693 |  | - | 1 | 174634.2 | -571909 | 0.17169 | 0.00214 | 1.756 | 219.6 | 0.262 | -115.000 |
| GJ 752 | 94761 | Wolf 1055 | 2 | 191655.3 | 051008 | 0.17101 | 0.00062 | 1.452 | 203.5 | 0.494 | 36.300 |
| GJ 752 |  | van Biesbroeck 10 | 2 | 191658.3 | 050901 | 0.17101 | 0.00062 | 1.461 | 203.1 | 0.073 | 36.300 |
| GJ 213 | 26857 | Ross 47 | 1 | 054209.3 | 122922 | 0.17037 | 0.00309 | 2.542 | 128.2 | 0.196 | 105.600 |
| GJ 300 |  | - | 1 | 081240.8 | -213310 | 0.16990 | 0.01500 | 0.707 | 177.5 | 0.166 | 999.000 |
| GJ 570 |  | - | 4 | 145728.0 | -2124 56 | 0.16985 | 0.00082 | 2.012 | 149.1 | 0.764 | 29.100 |
| GJ 570 |  | - | 4 | 145726.5 | -2124 41 | 0.16985 | 0.00082 | 1.937 | 149.4 | 0.548 | 27.900 |
| GJ 570 |  | - | 4 | 145726.5 | -212441 | 0.16985 | 0.00082 | 1.937 | 149.4 | 0.346 | 27.900 |
| GJ 570 |  | - | 4 | 145715.0 | -212150 | 0.16985 | 0.00082 | 2.012 | 149.1 | 0.050 | 27.900 |
| GJ 908 |  | - | 1 | 234912.5 | 022404 | 0.16851 | 0.00140 | 1.388 | 134.2 | 0.507 | -71.300 |
| GJ 34 | 3821 | eta Cassiopei A | 2 | 004906.3 | 574855 | 0.16838 | 0.00059 | 1.223 | 117.2 | 1.105 | 8.200 |
| GJ 34 |  | eta Cassiopei B | 2 | 004906.3 | 574855 | 0.16838 | 0.00059 | 1.223 | 117.2 | 0.604 | 10.500 |
| GJ 588 |  | - | 1 | 153212.9 | -411632 | 0.16836 | 0.00138 | 1.564 | 228.9 | 0.464 | 15.400 |
| GJ 285 | 37766 | Ross 882 | 1 | 074440.2 | 033309 | 0.16754 | 0.00228 | 0.568 | 217.4 | 0.225 | 26.800 |
| GJ 663 | 84405 | 36 Ophiuchi A | 3 | 171521.0 | -263610 | 0.16751 | 0.00075 | 1.238 | 202.5 | 0.850 | 0.500 |
| GJ 663 |  | 36 Ophiuchi B | 3 | 171521.0 | -263610 | 0.16751 | 0.00075 | 1.238 | 202.5 | 0.849 | 0.900 |
| GJ 664 | 84478 | 36 Ophiuchi C | 3 | 171613.4 | -26 3246 | 0.16751 | 0.00075 | 1.222 | 203.1 | 0.707 | -0.100 |
| GJ 783 | 99461 | - | 2 | 201111.9 | -360604 | 0.16533 | 0.00090 | 1.64 | 163.8 | 0.822 | -129.800 |
| GJ 783 |  | - | 2 | 201111.9 | -360604 | 0.16533 | 0.00090 | 1.64 | 163.8 | 0.202 | -129.800 |
| GJ 139 | 15510 | 82 Eridani | 1 | 031955.6 | -43 0411 | 0.16501 | 0.00055 | 3.124 | 76.6 | 0.971 | 86.700 |
| GJ 1221 |  | - | 1 | 174806.7 | 705229 | 0.16470 | 0.00240 | 1.651 | 311.0 | 0.500 | 999.000 |
| GJ 780 | 99240 | delta Pavonis | 1 | 200843.6 | -66 1055 | 0.16378 | 0.00065 | 1.656 | 133.0 | 1.095 | -21.700 |
| GJ 268 |  | QY Aurigae A | 2 | 071001.8 | 383146 | 0.16293 | 0.00177 | 1.045 | 204.9 | 0.170 | 37.900 |
| GJ 268 |  | QY Aurigae B | 2 | 071001.8 | 383146 | 0.16293 | 0.00177 | 1.045 | 204.9 | 0.156 | 37.900 |
| GJ 555 |  | HN Librae | 1 | 143416.8 | -123110 | 0.16286 | 0.00261 | 0.694 | 329.0 | 0.220 | 9.000 |
| GJ 338 |  | - | 2 | 091422.8 | 524112 | 0.16213 | 0.00237 | 1.634 | 249.8 | 0.601 | 13.700 |
| GJ 338 |  | - | 2 | 091424.7 | 524111 | 0.16213 | 0.00237 | 1.684 | 247.1 | 0.595 | 14.700 |
| GJ 2130 |  | - | 3 | 174612.6 | -320613 | 0.16177 | 0.01129 | 0.324 | 188.9 | 0.304 | 999.000 |
| GJ 2130 |  | - | 3 | 174614.4 | -320608 | 0.16177 | 0.01129 | 0.281 | 196.0 | 0.187 | 999.000 |
| GJ 2130 |  | - | 3 | 174614.4 | -320608 | 0.16177 | 0.01129 | 0.281 | 196.0 | 0.147 | 999.000 |
| GJ 784 |  | - | 1 | 201353.4 | -4509 50 | 0.16118 | 0.00107 | 0.794 | 101.6 | 0.577 | -31.100 |
| GJ 581 | 74995 | Wolf 562 | 1 | 151926.8 | -074320 | 0.15929 | 0.00210 | 1.229 | 265.4 | 0.300 | -9.400 |
| GJ 896 | 116132 | EQ Pegasi | 2 | 233152.2 | 195614 | 0.15772 | 0.00243 | 0.558 | 96.4 | 0.339 | 1.100 |
| GJ 896 |  | - | 2 | 233152.2 | 195614 | 0.15772 | 0.00243 | 0.558 | 96.4 | 0.160 | -1.200 |
| GJ 661 |  | - | 2 | 171207.9 | 453957 | 0.15632 | 0.00128 | 1.625 | 168.4 | 0.389 | -30.000 |
| GJ 661 |  | - | 2 | 171207.9 | 453957 | 0.15632 | 0.00128 | 1.625 | 168.4 | 0.330 | -30.000 |
| LHS 3003 |  | - | 1 | 145638.5 | -2809 51 | 0.15630 | 0.00300 | 0.965 | 210.1 | 0.077 | 999.000 |


| G 180-060 | - | 1 | 163118.4 | 405154 | 0.15600 | 0.00400 | 0.358 | 330.0 | 0.103 | 999.000 |  |
| :--- | :--- | :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| GJ 223.2 |  | WD 0552-041 | 1 | 055509.7 | -041017 | 0.15500 | 0.00210 | 2.377 | 166.6 | 0.500 | 999.000 |
| GJ 644 |  | Wolf 630 A | 5 | 165528.8 | -082011 | 0.15497 | 0.00056 | 1.208 | 223.3 | 0.425 | 12.100 |
| GJ 644 |  | Wolf 630 B | 5 | 165528.8 | -082011 | 0.15497 | 0.00056 | 1.208 | 223.3 | 0.309 | 12.100 |
| GJ 644 | van Biesbroeck 8 | 5 | 165535.8 | -082340 | 0.15497 | 0.00056 | 1.19 | 222.5 | 0.080 | 20.000 |  |
| GJ 644 |  | Wolf 630 C | 5 | 165528.8 | -082011 | 0.15497 | 0.00056 | 1.208 | 223.3 | 0.299 | 20.000 |
| GJ 643 | 82809 | Wolf 629 | 5 | 165525.2 | -081921 | 0.15497 | 0.00056 | 1.21 | 222.3 | 0.194 | 999.000 |
| GJ 892 | - | 1 | 231317.0 | 571006 | 0.15341 | 0.00054 | 2.095 | 81.9 | 0.812 | 999.000 |  |
| GJ 1156 |  | GL Virginis | 1 | 121900.3 | 110731 | 0.15290 | 0.00300 | 1.301 | 279.1 | 0.123 | 999.000 |
| GJ 625 | - | 1 | 162524.6 | 541815 | 0.15179 | 0.00101 | 0.465 | 111.5 | 0.372 | -12.600 |  |
| GJ 408 |  | Ross 104 | 1 | 110004.3 | 224959 | 0.15016 | 0.00149 | 0.51 | 236.7 | 0.389 | 999.000 |

Table 1: Our database of stars with parallax > 150 mas, as listed in the RECONS dataset. For each star the following entries are reported: Gliese index, Hipparcos index, common name (when available), number of components of the system, right ascension and declination (J2000.0), parallax and associated error, proper motion, position angle of proper motion, mass, radial velocity. All data come from the RECONS dataset, except the radial velocity measurements which have been taken from the Gliese Catalogue.


Figure 2: The number of stellar systems within 10 parsecs (234 as of 1998.5) with various errors in the measured trigonometric parallaxes (NStars Project): less than 20 parallax determinations are affected by errors larger than 10 mas which corresponds to a maximum relative error of $10 \%$ for stars as far as at 10 pc (i.e., at the edge of the selected volume).


Figure 3: The number of stellar systems within 10 parsecs (234 as of 1998.5) with various amounts of proper motion (NStars Project).

SYSTEMS TO BE DISCOVERED
WITHIN 10 PC


Figure 4: Assuming that the density of stars in a sphere of space surrounding the Sun with a 5 pc radius carries out to $10 \mathrm{pc}, 130$ systems in the larger sphere are anticipated to be missing from present catalogs (NStars Project). According to this figure within 6.7 pc of the Sun (i.e., parallaxes larger than 150 mas) only a few (of the order of 10) objects are missing.

MASS FUNCTION


Figure 5: The number of objects known within 10 parsecs (319 as of 1998.5) with various masses in units of the Sun's mass (NStars Project).

| name | distance from the Sun |  | name | distance from the Sun |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | pc | 1 y |  | pc | ly |
| Proxima Centauri | 1.2954 | 4.2229 | GJ 380 | 4.8589 | 15.8399 |
| alpha Centauri | 1.3383 | 4.3628 | GJ 388 | 4.8876 | 15.9335 |
| Barnard's Star | 1.8282 | 5.9600 | GJ 832 | 4.9315 | 16.0765 |
| Wolf 359 | 2.3861 | 7.7786 | GJ 682 | 5.0088 | 16.3286 |
| Lalande 21185 | 2.5418 | 8.2863 | omicron 2 Eri | 5.0251 | 16.3819 |
| Sirius | 2.6314 | 8.5785 | EV Lacertae | 5.0495 | 16.4613 |
| UV Ceti | 2.6759 | 8.7236 | 70 Ophiuchi | 5.1031 | 16.6360 |
| Ross 154 | 2.9682 | 9.6765 | Altair | 5.1290 | 16.7205 |
| Ross 248 | 3.1646 | 10.3165 | EI Cancri | 5.2301 | 17.0502 |
| epsilon Eri | 3.2259 | 10.5165 | GJ 445 | 5.3810 | 17.5420 |
| Lacaille 9352 | 3.2934 | 10.7364 | GJ 1005 | 5.3816 | 17.5439 |
| Ross 128 | 3.3476 | 10.9132 | GJ 526 | 5.4286 | 17.6972 |
| EZ Aquarii | 3.4542 | 11.2608 | Stein 2051 | 5.5362 | 18.0479 |
| Procyon | 3.4959 | 11.3966 | GJ 754 | 5.7078 | 18.6073 |
| 61 Cygni | 3.4960 | 11.3970 | Wolf 1453 | 5.7087 | 18.6105 |
| DM+59 1915 | 3.5336 | 11.5194 | sigma Draconi | 5.7607 | 18.7799 |
| GX Andromedae | 3.5639 | 11.6184 | GJ 229 | 5.7747 | 18.8254 |
| Eps Indi | 3.6253 | 11.8184 | GJ 693 | 5.8245 | 18.9877 |
| DX Cancri | 3.6258 | 11.8202 | Wolf 1055 | 5.8476 | 19.0632 |
| Tau Ceti | 3.6444 | 11.8809 | Ross 47 | 5.8696 | 19.1348 |
| RECONS 1 | 3.6765 | 11.9853 | GJ 570 | 5.8875 | 19.1934 |
| YZ Ceti | 3.7197 | 12.1262 | GJ 908 | 5.9344 | 19.3460 |
| Luyten's Star | 3.7913 | 12.3597 | eta Cassiopei | 5.9389 | 19.3610 |
| Kapteyn's Star | 3.9174 | 12.7708 | GJ 588 | 5.9397 | 19.3633 |
| AX Microscopium | 3.9459 | 12.8635 | Ross 882 | 5.9687 | 19.4580 |
| Kruger 60 | 4.0313 | 13.1420 | 36 Ophiuchi | 5.9698 | 19.4615 |
| Ross 614 | 4.0927 | 13.3421 | GJ 783 | 6.0485 | 19.7181 |
| Wolf 1061 | 4.2371 | 13.8130 | 82 Eridani | 6.0602 | 19.7564 |
| WD 0046+051 | 4.3126 | 14.0590 | delta Pavonis | 6.1058 | 19.9048 |
| GJ 1 | 4.3630 | 14.2234 | QY Aurigae | 6.1376 | 20.0086 |
| Wolf 424 | 4.3879 | 14.3045 | HN Librae | 6.1402 | 20.0172 |
| TZ Arietis | 4.4484 | 14.5018 | GJ 338 | 6.1679 | 20.1073 |
| GJ 687 | 4.5354 | 14.7853 | GJ 784 | 6.2042 | 20.2258 |
| LHS 292 | 4.5393 | 14.7980 | Wolf 562y | 6.2779 | 20.4658 |
| GJ 674 | 4.5403 | 14.8014 | EQ Pegasi | 6.3403 | 20.6695 |
| GJ 1002 | 4.6948 | 15.3052 | GJ 661 | 6.3971 | 20.8547 |
| Ross 780 | 4.7039 | 15.3347 | Wolf 630 | 6.4529 | 21.0363 |
| WX Ursae Maj | 4.8539 | 15.8237 | GJ 625 | 6.5880 | 21.4770 |

Table 2: Star distances from the Sun, expressed in parsecs (pc) and light years (ly).

### 2.2 Double and multiple stellar systems information

Of the $140+1$ (= the Sun) stars that constitute our database, 33 form multiple systems ( 24 binaries, 7 triples, 1 quadruple and 1 quintuple system). In many cases the source catalogues do not resolve the astrometric parameters of the system members and one must search for the required information in the specialized literature. Unfortunately, as we shall discuss later, many systems do not yet have accurate determinations of their astrometric parameters, and in some cases these cannot be distinguished from those of their companions.

The Gliese Catalogue does not always provide radial velocity determinations for the companions of the main star within a multiple system: under these circumstances we have assigned to the companions the radial velocity of the corresponding primary (and the value is coloured in blue in Table 1).
Orbital parameters for 235 binary systems are published in the Hipparcos Catalogue, 1811 in the Sixth Orbit Catalog of Visual Binary Stars of the U.S. Naval Observatory (Hartkopf, Mason \& Worley, 2001) which combines, merges and classifies data from various catalogues and authors. We have been able to extract from the latter catalogue orbital elements ${ }^{1}$ for 13 binaries of our database.
Table 3 reports the period $P$, the semi-major axis $a$, the inclination $i$ with respect to the tangent plane to the celestial sphere through the object, the position of the ascending node $\Omega$, the epoch $T$, the eccentricity $e$ and the argument of perigee $\omega$ of these systems. Individual values for the masses of the components are not provided; however, the total mass of the system, as derived by applying the third Kepler's law to the given period and semi-major axis (after transformation from angular to linear units by means of the parallax value contained in our database), in general is not consistent with the sum of the masses provided by NStars and included in our database. We removed this difficulty by ignoring the published value of the period and by computing a new one on the basis of the semi-major axis and our values of the masses (see
Table 4, which reports the semi-major axes in linear units, the masses of the system members as in our database and the derived values of the period).

| HIIP | Name | P | a | i | $\Omega$ | T | e | $\omega$ | SOURCE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | years | arcsec | deg | deg | year |  | deg |  |
| 71683 | alpha Centauri | 79.914 | 17.575 | 79.21 | 204.85 | 1875.663 | 0.5179 | 231.651 | 6th Orbit Catalogue |
| 32349 | Sirius | 50.090 | 7.500 | 136.53 | 44.57 | 1894.130 | 0.5923 | 147.270 | 6th Orbit Catalogue |
|  | UV Ceti $=$ L 726-8 | 26.520 | 1.950 | 127.30 | 150.50 | 1971.910 | 0.6200 | 285.300 | Geyer et al., 1988 |
| 37279 | Procyon | 40.820 | 4.271 | 31.10 | 97.30 | 1967.970 | 0.4070 | 92.200 | 6th Orbit Catalogue |
| 104214 | 61 Cygni | 4.900 | 0.140 | 134.00 | 94.00 | 1953.200 | 0.5000 | 295.000 | 6th Orbit Catalogue |
| 91768 | DM+59 1915 | 408.000 | 13.880 | 66.00 | 136.90 | 1775.000 | 0.5300 | 234.600 | 6th Orbit Catalogue |
| 1475 | GX Andromedae | 2600.000 | 41.150 | 61.40 | 45.30 | 1745.000 | 0.0000 | 0.000 | 6th Orbit Catalogue |
| 110893 | Kruger 60 | 44.670 | 2.383 | 167.20 | 154.50 | 1970.220 | 0.4100 | 211.000 | 6th Orbit Catalogue |
| 30920 | Ross 614 | 16.124 | 1.040 | 51.80 | 30.70 | 1999.380 | 0.3710 | 223.000 | 6th Orbit Catalogue |
| 88601 | 70 Ophiuchi | 88.380 | 4.554 | 121.16 | 302.12 | 1895.940 | 0.4992 | 14.000 | 6th Orbit Catalogue |
| 1242 | GJ 1005 | 4.566 | 0.304 | 146.00 | 62.60 | 1995.366 | 0.3640 | 346.400 | 6th Orbit Catalogue |
| 3821 | eta Cassiopei | 480.000 | 11.994 | 34.76 | 278.42 | 1889.600 | 0.4970 | 268.590 | 6th Orbit Catalogue |
| 116132 | EQ Pegasi | 359.000 | 6.870 | 123.50 | 82.10 | 2008.000 | 0.2000 | 354.000 | 6th Orbit Catalogue |

Table 3: Orbital elements of 13 binary systems present in our dataset. The source is the Sixth Orbit Catalog of Visual Binary Stars of the U.S. Naval Observatory, except for the case of UV Ceti (L 726-8) for which data have been obtained from the paper published by Geyer et al. (1988).

[^0]| Name | $\mathbf{m}_{1}$ | $\mathbf{m}_{\mathbf{2}}$ | $\mathbf{a}$ | $\mathbf{P}$ |
| :--- | :---: | :---: | ---: | ---: |
|  | $\mathrm{M}_{\text {sun }}$ | $\mathrm{M}_{\text {sun }}$ | AU | years |
| alpha Centauri | 1.144 | 0.916 | 23.52 | 79.475 |
| Sirius | 1.991 | 0.500 | 19.74 | 55.551 |
| UV Ceti = L 726-8 | 0.109 | 0.102 | 5.22 | 25.949 |
| Procyon | 1.569 | 0.500 | 14.93 | 40.297 |
| 61 Cygni | 0.703 | 0.630 | 0.50 | 0.297 |
| DM+59 1915 | 0.351 | 0.259 | 49.05 | 439.784 |
| GX Andromedae | 0.486 | 0.163 | 146.66 | 2204.571 |
| Kruger 60 | 0.279 | 0.160 | 9.61 | 44.939 |
| Ross 614 | 0.170 | 0.097 | 4.23 | 16.994 |
| 70 Ophiuchi | 0.924 | 0.701 | 23.24 | 87.884 |
| GJ 1005 | 0.177 | 0.105 | 1.64 | 3.940 |
| eta Cassiopei | 1.105 | 0.604 | 71.23 | 459.874 |
| EQ Pegasi | 0.339 | 0.160 | 43.56 | 406.963 |

Table 4: The masses of the members of the 13 binary systems of the previous table, the semi-major axes in linear units and the orbital periods as obtained by applying the third Kepler's law.

### 2.3 From catalogue data to space positions and velocities

Starting from the raw data of Table 1 and by means of basic astrometric formulas (Zagar, 1984; Smart, 1931), we computed the stellar distances from the Sun and the cartesian components of the heliocentric positions ( $\mathrm{x}_{E}, y_{E}, z_{E}$ ) and velocities ( $u_{E}, v_{E}, w_{E}$ ) in the J 2000.0 equatorial reference system expressed in parsecs and in $\mathrm{km} / \mathrm{s}$ respectively:

$$
\begin{gather*}
x_{E}=\frac{1}{\pi} \cos \delta \cos \alpha \\
y_{E}=\frac{1}{\pi} \cos \delta \sin \alpha  \tag{1}\\
z_{E}=\frac{1}{\pi} \sin \delta \\
u_{e}=-\frac{k}{\pi} \mu_{\alpha} \sin \alpha \cos \delta-\frac{k}{\pi} \mu_{\delta} \cos \alpha \sin \delta+v_{R} \cos \alpha \cos \delta \\
v_{e}=+\frac{k}{\pi} \mu_{\alpha} \cos \alpha \cos \delta-\frac{k}{\pi} \mu_{\delta} \sin \alpha \sin \delta+v_{R} \sin \alpha \cos \delta  \tag{2}\\
w_{e}=+\frac{k}{\pi} \mu_{\delta} \cos \delta+v_{R} \sin \delta
\end{gather*}
$$

$\mu_{\alpha}$ and $\mu_{\delta}$ are the proper motion in right ascension and declination respectively (in arcsec/yr), $\pi$ is the parallax ( $\operatorname{arcsec}$ ) and $v_{R}$ is the radial velocity $(\mathrm{km} / \mathrm{s}) . k$ (approximately equal to 4.74 ) is a conversion factor from $\mathrm{AU} / \mathrm{yr}$ to $\mathrm{km} / \mathrm{s}$.

Following the derivation made by Murray (1989), the direction to the galactic pole in the J2000.0 equatorial system is $\alpha_{G}=12^{h} 51^{m} 26.2755^{s} ; \delta_{G}=27^{\circ} 7^{\prime} 41.704 "$. By pre-multiplying the vector ( $\mathrm{x}_{E}, y_{E}, z_{E}$ ) of equatorial position by the matrix $N_{J 2000}$ of the direction cosines of the principal galactic axes in the equatorial system referred to equinox and equator of J2000

$$
N_{J 2000}=\left[\begin{array}{lll}
-0.054875539 & -0.873437105 & -0.483834992  \tag{3}\\
+0.494109454 & -0.444829594 & +0.746982249 \\
-0.867666136 & -0.198076390 & +0.455983795
\end{array}\right],
$$

we obtained the J2000.0 galactic components $\left(\mathrm{x}_{G}, y_{G}, z_{G}\right)$ of the star's position. In the same way we computed the J2000.0 galactic components $\left(u_{G}, v_{G}, w_{G}\right)$ of the star's velocity from ( $u_{E}, v_{E}, w_{E}$ ).
The results are summarized in Table 5, which gives the name, the mass and the cartesian heliocentric galactic components of position and velocity of each star. In this respect note that each multiple system has been treated as a single object (with the total mass of the system concentrated in its barycentre) in the context of the overall kinematics and dynamics of the solar neighbourhood; individual members of a stellar system are resolved only when dealing with the internal dynamics of the system.

| Star name | Mass | $\mathrm{X}_{\mathrm{G}}$ | $\mathrm{y}_{\mathrm{G}}$ | $\mathrm{Z}_{\mathrm{G}}$ | $\mathrm{u}_{\mathrm{G}}$ | $\mathrm{v}_{\mathrm{G}}$ | $\mathrm{w}_{\mathrm{G}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (Msun) | (pc) | (pc) | (pc) | (km/s) | (km/s) | (km/s) |
| Sun | 1.000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| Proxima Centauri | 0.107 | 0.8983 | -0.9322 | -0.0436 | -25.0535 | -2.5416 | 13.5058 |
| alpha Centauri | 2.060 | 0.9583 | -0.9340 | -0.0159 | -29.5921 | 1.7868 | 13.6440 |
| Barnard's Star | 0.166 | 1.5200 | 0.9136 | 0.4442 | -141.5593 | 4.5502 | 18.1865 |
| Wolf 359 | 0.092 | -0.5819 | -1.1961 | 1.9809 | -26.1342 | -44.2696 | -18.7476 |
| Lalande 21185 | 0.464 | -1.0526 | -0.0943 | 2.3117 | 46.0142 | -53.6332 | -73.9268 |
| Sirius | 2.491 | -1.7654 | -1.9085 | -0.4067 | 15.5544 | 0.9537 | -11.1752 |
| UV Ceti | 0.211 | -0.6589 | 0.0520 | -2.5930 | -44.1600 | -19.5149 | -20.5939 |
| Ross 154 | 0.171 | 2.8639 | 0.5726 | -0.5299 | -13.5685 | -1.3087 | -6.9666 |
| Ross 248 | 0.121 | -1.0348 | 2.8448 | -0.9222 | 32.9478 | -74.4376 | 0.0299 |
| epsilon Eri | 0.850 | -2.0745 | -0.5888 | -2.3993 | -3.8814 | 7.0210 | -21.0898 |
| Lacaille 9352 | 0.529 | 1.3365 | 0.1193 | -3.0076 | -93.5769 | -13.4950 | -52.5199 |
| Ross 128 | 0.156 | 0.0498 | -1.7663 | 2.8433 | 17.3102 | 6.1051 | -33.1272 |
| EZ Aquarii | 0.306 | 1.2822 | 1.3781 | -2.8963 | -69.3906 | -1.0633 | 40.3337 |
| Procyon | 2.069 | -2.8336 | -1.8899 | 0.7876 | 5.3590 | -8.4515 | -18.7556 |
| 61 Cygni | 1.333 | 0.4648 | 3.4468 | -0.3544 | -93.3822 | -53.7889 | -8.7272 |
| DM+59 1915 | 0.610 | 0.0400 | 3.2220 | 1.4502 | -24.8910 | -11.5070 | 26.3745 |
| GX Andromedae | 0.649 | -1.5178 | 3.0209 | -1.1277 | -49.1588 | -12.0400 | -3.4556 |
| Eps Indi | 0.838 | 2.2174 | -0.9784 | -2.6960 | -80.8710 | -40.7147 | 2.6005 |
| DX Cancri | 0.087 | -2.9267 | -0.8955 | 1.9440 | -5.8515 | -6.3244 | -21.0490 |
| Tau Ceti | 0.921 | -1.0312 | 0.1248 | -3.4933 | 18.8275 | 29.3881 | 13.2274 |
| RECONS 1 | 0.113 | -0.6900 | -2.1074 | -2.9324 | 3.4566 | -0.0283 | 24.2814 |
| YZ Ceti | 0.136 | -0.6260 | 0.3658 | -3.6483 | -28.4306 | -0.3083 | -23.7000 |
| Luyten's Star | 0.257 | -3.1507 | -1.9952 | 0.6827 | 15.9714 | -65.6236 | -17.0081 |
| Kapteyn's Star | 0.393 | -1.0562 | -2.9880 | -2.3027 | 19.8737 | -288.1694 | -52.8391 |
| AX Microscopium | 0.600 | 2.8196 | 0.1924 | -2.7537 | 63.7112 | -19.1513 | 23.4878 |
| Kruger 60 | 0.439 | -1.0221 | 3.8996 | -0.0002 | 26.5830 | -26.8544 | 1.0008 |
| Ross 614 | 0.267 | -3.4152 | -2.2118 | -0.4411 | -5.3850 | -23.5284 | 4.7228 |
| Wolf 1061 | 0.261 | 3.8737 | 0.2269 | 1.7017 | -5.4938 | -20.3976 | -17.1433 |
| WD 0046+051 | 0.500 | -1.2245 | 1.9688 | -3.6363 | -11.1414 | -28.1933 | -75.5553 |
| GJ 1 | 0.481 | 1.0192 | -0.3009 | -4.2316 | -75.5562 | -97.6697 | -34.8649 |
| Wolf 424 | 0.236 | 0.4503 | -1.3258 | 4.1585 | -91.2845 | 152.0808 | -525.8738 |
| TZ Arietis | 0.140 | -2.5876 | 1.6383 | -3.2263 | 14.4017 | -51.8465 | 4.8645 |
| GJ 687 | 0.390 | -0.5755 | 3.8044 | 2.4010 | 29.7659 | -20.7592 | -3.7954 |
| LHS 292 | 0.083 | -0.5338 | -3.3687 | 2.9953 | 28.8531 | -11.4821 | -18.3804 |
| GJ 674 | 0.361 | 4.3117 | -1.3179 | -0.5358 | -14.6958 | -5.0792 | -19.3314 |
| GJ 1002 | 0.109 | -0.0766 | 1.7778 | -4.3445 | 36.9629 | -41.0218 | 27.9485 |
| Ross 780 | 0.273 | 1.4640 | 1.8742 | -4.0584 | -12.4088 | -19.8262 | -11.8934 |
| WX Ursae Maj | 0.582 | -2.1541 | 0.4381 | 4.3276 | -123.4714 | -5.3758 | 16.2542 |
| GJ 380 | 0.642 | -2.8914 | 0.7281 | 3.8364 | -9.4993 | -20.4585 | -35.4461 |
| GJ 388 | 0.393 | -2.2783 | -1.6832 | 3.9830 | -14.8095 | -7.6173 | 3.4032 |
| GJ 832 | 0.503 | 3.3434 | -0.6394 | -3.5682 | 2.7508 | -19.3951 | 0.3865 |
| GJ 682 | 0.213 | 4.8271 | -1.2048 | -0.5787 | -64.2773 | -12.6363 | 9.4609 |
| omicron 2 Eri | 1.582 | -3.7005 | -1.4022 | -3.0971 | 92.4081 | -14.6632 | -44.9881 |
| EV Lacertae | 0.285 | -0.9054 | 4.8346 | -1.1418 | 19.8896 | 2.8337 | -1.5609 |
| 70 Ophiuchi | 1.625 | 4.3374 | 2.4934 | 1.0058 | 4.9236 | -19.4927 | -14.7022 |
| Altair | 1.710 | 3.4073 | 3.7504 | -0.7943 | -28.8439 | -10.0468 | -2.6361 |
| EI Cancri | 0.203 | -3.7292 | -1.9456 | 3.1084 | 10.3411 | 12.7053 | -36.8489 |
| GJ 445 | 0.240 | -2.5446 | 3.3956 | 3.3090 | 68.3978 | -54.8595 | -73.5618 |
| GJ 1005 | 0.282 | 0.1360 | 1.2764 | -5.2262 | -9.0405 | -29.0936 | 22.5213 |
| GJ 526 | 0.526 | 1.6226 | -0.2403 | 5.1748 | 61.2546 | -1.8119 | -2.4011 |
| Stein 2051 | 0.724 | -4.6620 | 2.9015 | 0.7046 | -48.6837 | -43.5563 | -9.1808 |
| GJ 754 | 0.158 | 5.1720 | -0.6937 | -2.3126 | -9.8112 | -69.8542 | -40.4774 |
| Wolf 1453 | 0.566 | -4.7991 | -2.4384 | -1.9007 | 22.2908 | -55.7710 | -10.2644 |


| sigma Draconi | 0.892 | -1.0478 | 5.2422 | 2.1465 | 31.2701 | 44.7722 | -18.3956 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| GJ 229 | 0.606 | -3.6219 | -4.1100 | -1.8265 | 11.4974 | -12.0743 | -12.0693 |
| GJ 693 | 0.262 | 5.1243 | -2.3564 | -1.4537 | -118.8336 | 2.3256 | 38.1066 |
| Wolf 1055 | 0.567 | 4.4428 | 3.7874 | -0.3349 | 53.5316 | -7.1941 | -5.0166 |
| Ross 47 | 0.196 | -5.6288 | -1.3730 | -0.9396 | -89.6115 | -89.7823 | 8.3586 |
| GJ 570 | 1.708 | 4.6027 | -1.8370 | 3.1787 | 48.8315 | -22.3839 | -30.9629 |
| GJ 908 | 0.507 | -0.2015 | 3.2363 | -4.9702 | -8.9380 | -70.4216 | 39.6402 |
| eta Cassiopei | 1.709 | -3.1890 | 4.9827 | -0.5233 | -29.7678 | -10.0696 | -16.7593 |
| GJ 588 | 0.464 | 5.1591 | -2.6657 | 1.2480 | -6.0376 | -46.2846 | -0.6094 |
| Ross 882 | 0.225 | -4.7048 | -3.4002 | 1.3891 | -19.8001 | -22.8652 | -7.8753 |
| 36 Ophiuchi | 2.406 | 5.9242 | -0.1780 | 0.7149 | 0.3522 | -34.1454 | -7.3472 |
| GJ 783 | 1.024 | 5.1671 | 0.4733 | -3.1084 | -118.7923 | -52.2212 | 47.1550 |
| 82 Eridani | 0.971 | -1.1153 | -3.1929 | -5.0287 | -78.7168 | -92.6964 | -28.1705 |
| delta Pavonis | 1.095 | 4.4533 | -2.5953 | -3.2731 | -48.6311 | -13.4271 | -15.0397 |
| QY Aurigae | 0.326 | -5.7700 | 0.1053 | 2.0896 | -43.2565 | -21.0019 | -7.0644 |
| HN Librae | 0.220 | 4.1654 | -1.6475 | 4.1997 | -6.6258 | 2.9830 | 20.9004 |
| GJ 338 | 1.196 | -4.3794 | 1.1787 | 4.1802 | -43.6621 | -15.1028 | -20.5324 |
| GJ 784 | 0.577 | 5.1834 | -0.4711 | -3.3768 | -38.7821 | 1.5610 | -2.6084 |
| Wolf 562y | 0.300 | 4.7821 | -0.4961 | 4.0369 | -25.0412 | -25.6807 | 11.8899 |
| EQ Pegasi | 0.499 | -0.7333 | 4.8625 | -4.0023 | -13.7274 | -7.0423 | -6.6151 |
| GJ 661 | 0.719 | 1.6569 | 4.9054 | 3.7570 | 39.7425 | -31.0176 | -28.1099 |
| Wolf 630 | 1.307 | 5.9071 | 1.1530 | 2.3273 | 15.5671 | -28.5408 | 9.5466 |
| GJ 625 | 0.372 | 0.5715 | 4.8011 | 4.4750 | 8.0238 | -2.0662 | -17.3578 |

Table 5: Initial conditions of the motion of the 77 stars of our database derived from the raw astrometric data: positions and velocities are referred to the heliocentric galactic reference frame (J2000.0).

With these data we have analysed various aspects of the stellar distribution in the solar neighbourhood: the mass distribution (Figure 6) shows that only a handful of objects are more massive than the Sun (with Sirius A+B showing the highest mass $=2.7 M_{\text {sun }}$ ) and that most stars occupy the mass range below 0.6 $M_{\text {sun }}$.


Figure 6: Stellar masses versus heliocentric distances.

The minimum relative distances among the stars (Table 6) range between 0.0661 parsecs (between Alpha Centauri and Proxima) and 2.8300 parsecs (between Stein 2051 and eta Cassiopeiae) with an average of 1.3873 parsecs.

| Star name | Closest star | d (pe) | Star name | Closest star | d (pe) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Sun | Proxima Centauri | 1.2954 | GJ 380 | WX Ursae Maj | 0.9322 |
| Proxima Centauri | alpha Centauri | 0.0661 | GJ 388 | EI Cancri | 1.7143 |
| alpha Centauri | Proxima Centauri | 0.0661 | GJ 832 | AX Microscopium | 1.2766 |
| Barnard's Star | Ross 154 | 1.6945 | GJ 682 | GJ 674 | 0.5295 |
| Wolf 359 | Ross 128 | 1.2116 | omicron 2 Eri | Wolf 1453 | 1.9266 |
| Lalande 21185 | Wolf 359 | 1.2429 | EV Lacertae | Kruger 60 | 1.4803 |
| Sirius | Procyon | 1.6023 | 70 Ophiuchi | Wolf 1055 | 1.8663 |
| UV Ceti | Tau Ceti | 0.9769 | Altair | Wolf 1055 | 1.1334 |
| Ross 154 | Barnard's Star | 1.6945 | EI Cancri | GJ 388 | 1.7143 |
| Ross 248 | GX Andromedae | 0.5537 | GJ 445 | GJ 687 | 2.2066 |
| epsilon Eri | UV Ceti | 1.5659 | GJ 1005 | GJ 1002 | 1.0363 |
| Lacaille 9352 | EZ Aquarii | 1.2649 | GJ 526 | Wolf 424 | 1.8936 |
| Ross 128 | Wolf 359 | 1.2116 | Stein 2051 | eta Cassiopei | 2.8300 |
| EZ Aquarii | Lacaille 9352 | 1.2649 | GJ 754 | GJ 784 | 1.0873 |
| Procyon | Luyten's Star | 0.3502 | Wolf 1453 | Ross 47 | 1.6574 |
| 61 Cygni | Kruger 60 | 1.5942 | sigma Draconi | GJ 687 | 1.5346 |
| DM+59 1915 | GJ 687 | 1.2736 | GJ 229 | Wolf 1453 | 2.0459 |
| GX Andromedae | Ross 248 | 0.5537 | GJ 693 | GJ 682 | 1.4765 |
| Eps Indi | AX Microscopium | 1.3178 | Wolf 1055 | Altair | 1.1334 |
| DX Cancri | Procyon | 1.5280 | Ross 47 | Wolf 1453 | 1.6574 |
| Tau Ceti | YZ Ceti | 0.4963 | GJ 570 | HN Librae | 1.1268 |
| RECONS 1 | Kapteyn's Star | 1.1429 | GJ 908 | GJ 1002 | 1.5919 |
| YZ Ceti | Tau Ceti | 0.4963 | eta Cassiopei | EV Lacertae | 2.3706 |
| Luyten's Star | Procyon | 0.3502 | GJ 588 | GJ 570 | 2.1734 |
| Kapteyn's Star | RECONS 1 | 1.1429 | Ross 882 | Luyten's Star | 2.2109 |
| AX Microscopium | GJ 832 | 1.2766 | 36 Ophiuchi | GJ 682 | 1.9827 |
| Kruger 60 | Ross 248 | 1.4009 | GJ 783 | GJ 784 | 0.9819 |
| Ross 614 | Luyten's Star | 1.1746 | 82 Eridani | RECONS 1 | 2.3987 |
| Wolf 1061 | 36 Ophiuchi | 2.3113 | delta Pavonis | GJ 693 | 1.9538 |
| WD 0046+051 | GJ 1002 | 1.3622 | QY Aurigae | GJ 338 | 2.7307 |
| GJ 1 | Lacaille 9352 | 1.3324 | HN Librae | GJ 570 | 1.1268 |
| Wolf 424 | Ross 128 | 1.4436 | GJ 338 | GJ 380 | 1.5923 |
| TZ Arietis | WD 0046+051 | 1.4613 | GJ 784 | GJ 783 | 0.9819 |
| GJ 687 | DM+59 1915 | 1.2736 | Wolf 562y | HN Librae | 1.3163 |
| LHS 292 | Ross 128 | 1.7122 | EQ Pegasi | GJ 908 | 1.9657 |
| GJ 674 | GJ 682 | 0.5295 | GJ 661 | GJ 625 | 1.3055 |
| GJ 1002 | GJ 1005 | 1.0363 | Wolf 630 | 36 Ophiuchi | 2.0909 |
| Ross 780 | EZ Aquarii | 1.2766 | GJ 625 | GJ 661 | 1.3055 |
| WX Ursae Maj | GJ 380 | 0.9322 |  |  |  |

Table 6: The minimum relative distances among the stars.

### 2.4 The local interstellar medium

For the sake of completeness, we wish to mention the constituents of the local interstellar medium: gas, dust and dark matter. The gas component is mainly dominated by neutral hydrogen atoms, with a typical number density of $0.10 \mathrm{~cm}^{-3}$ around the Sun (Spitzer, 1985). Recent mass density determinations based on Hipparcos data and observations of the line-of-sight velocities of stars suggest that dark matter does not contribute significantly to the local density in the solar neighbourhood (Creze et al., 1998; Kuijken \& Gilmore, 1991).
Table 7 summarizes the properties of the local interstellar medium.

| Component | Property | Value |
| :--- | :--- | :--- |
| Neutral component | Flow speed | $25 \pm 2 \mathrm{~km} / \mathrm{s}$ |
|  | Flow direction | $\lambda=75.4^{\circ} \beta=-7.5^{\circ}$ (ecliptic coordinates) |
|  | Hydrogen density | $0.10 \pm 0.01 \mathrm{~cm}^{-3}$ |
|  | Helium density | $0.010 \pm 0.003 \mathrm{~cm}^{-3}$ |
|  | Hydrogen temperature | $(7 \pm 2) \cdot 1000^{\circ} \mathrm{K}$ |
|  | Helium temperature | $(7 \pm 2) \cdot 1000^{\circ} \mathrm{K}$ |
| Ionized component | Electron density | $<0.3 \mathrm{~cm}^{-3}$ |
|  | Flow speed | assumed as neutral component |
|  | Flow direction | assumed as neutral component |
|  | Ion temperature | assumed as neutral component |
| Magnetic field | Magnitude | $0.1-0.5 \mathrm{nT}$ |
|  | Direction | Unknown |
| Cosmic rays | Total pressure | $(1.3 \pm 0.2) 10^{-12}$ dynes $\mathrm{cm}^{-2}$ |

Table 7: The main components of the local interstellar medium and their properties (from Axford \& Suess, http://web.mit.edu/space/www/helio.review/axford.suess.html).

## 3 THE DYNAMICS OF THE NEARBY STARS

### 3.1 N-body motion

The trajectories of the 77 stellar systems of our database were numerically integrated as an isolated system of $N$ bodies subject only to their mutual gravitational attractions. The data contained in Table 5 have been used as initial conditions for the numerical integration of the equations of motion. The gravitational effects of the Galaxy as a whole were not included. Computations were run at various step sizes ( $0.6,1.0,10,100,1000$ years) and over time intervals of variable length (from a few years to million years) . The results conistently show (Figure 7 and Figure 8) that all stars move with constant speed (relative to the Sun). This means that the nearby stars behave as a collisionless system of particles, as predicted by the theorems of galactic hydrodynamics: "[...] a star's galactic orbit is not appreciably disturbed by the gravitational attraction of individual stars [...]" (Roy, 1972); and " [...] the probability of close binary encounters ${ }^{2}$ is of the order of $10^{-6}$; multiple encounters hardly ever occur and can be neglected [...]".

[^1]$38=$ Ross 780
$39=$ WX Ursae Maj
$40=$ GJ 380
$41=$ GJ 388
$42=$ GJ 832
$43=$ GJ 682
$44=$ omicron 2 Eri
$45=$ EV Lacertae
$46=70$ Ophiuchi
$47=$ Altair
$48=$ El Cancri
$49=$ GJ 445
$50=$ GJ 1005
$51=$ GJ 526
$52=$ Stein 2051
$53=$ GJ 754
$54=$ Wolf 1453
$55=$ sigma Draconi
$56=$ GJ 229
$57=$ GJ 693
$58=$ Wolf 1055
$59=$ Ross 47
$60=$ GJ 570
$61=$ GJ 908
$62=$ eta Cassiopei
$63=$ GJ 588
$64=$ Ross 882
$65=36$ Ophiuchi
$66=G J 783$
$67=82$ Eridani
$68=$ delta Pavonis
$69=$ QY Aungae
$70=$ HN Librae
$71=$ GJ 338
$72=$ GJ 784
$73=$ Wolf $562 y$
$74=$ EQ Pegasi
$75=G J 661$
$76=$ Wolf 630
$77=G J$
4


2=Proxima Centauri 3=alpha Centauri 4=Barnard's Star $5=$ Wolf 359 6=Lalande 21185 $7=$ Sirius 8=UV Ceti $9=$ Ross 154

11=epsilon Eri
12=Lacaille 9352
14=EZ Aquarii
15=Procyon 16=61 Cygni 17=DM+59 1915 18=GX Andromedae 19=Eps Indi
$21=$ Tau Ceti 22=RECONS 1 $23=$ YZ Ceti

25=Kapteyn's Star
26=AXMicroscopium
28=Ross 614
$29=$ Wolf 1061 $30=W D 0046+051$
31=GJ 1
$32=$ Wolf 424
$33=$ TZ Arietis
34=GJ 687
35=LHS 292
36=G.J 674
37=GJ 1002

Figure 7: Stellar trajectories as obtained by integration of the N-body equations of motion over 15,000 years. Projected view on the galactic plane.

We did not push our integrations further (in terms of total integration time) because we know that (Binney \& Tremaine, 1988) one cannot neglect collisions in a globular cluster which contains $10^{5}$ stars, while for a galaxy of $10^{11}$ stars the collisional relaxation time turns out to be much larger than the age of the universe and collisions can be neglected.
The most common formalism to describe the large scale stellar dynamic properties in the Galaxy makes use of the collisionless Boltzmann equation which, by means of its moment equations (Jeans equations), approximates the density and velocity distribution of the stars (Binney \& Tremaine, 1988).
Figure 9 shows the distances of the nearby stars as a function of time over the next 15,000 years: in a few thousand years Proxima will be "overtaken" by Alpha Cen and for a short time by Barnard's Star and will cease to be the closest star to our Sun.

Stellar trajectories over 15,000 years in heliocentric galactic coordinates


Figure 8: Stellar trajectories as obtained by integration of the N-body equations of motion over 15,000 years. 3dimensional view in galactic coordinates.


Figure 9: Stellar distances from the Sun as a function of time as obtained from the integration of the N-body equations of motion over 15,000 years.

We determined the relative contributions of the $N$ stars to the gravitational acceleration at various positions in the volume of space of 6.7 pc radius around the Sun. We performed the computation over several planes parallel to the galactic plane and equally spaced by 0.5 pc . On each plane the computation grid is 0.05 pc . Figure 10 and Figure 11 show, in terms of a 2D contour map and 3D surface respectively, the acceleration field in the galactic plane $(z=0)$. The plots on several other parallel planes are placed in the Appendix to this report.


Figure 10: Contour map of the gravitational acceleration caused by the 77 stars on the galactic plane. The projected positions of the stars are also indicated.

Most ${ }^{3}$ graphs exhibit two common features: high sharp peaks (the top part of which has been cut in order to reduce the range of values and smooth the color range of the figure) over a smooth continuum below $10^{-11}-10^{-12} \mathrm{~m} / \mathrm{s}^{2}$. The peaks are centered at the locations of the stars (or near their projections onto the plane under evaluation), as can be seen by looking at the contour maps where the stars have been positioned according to their $x$ and $y$ coordinates. Each star exerts its gravitational attraction (i.e., the peak) over a small "region of influence" around it, the boundaries of which are identified by the speed of a test particle becoming constant (within a given tolerance). In the case of the Sun, the integration of the equations of motion of the $N$ bodies + a spacecraft leaving the Solar System toward Proxima Centauri has shown that the speed of the particle becomes constant at a distance of $45,000 \mathrm{AU}$ from the Sun, where the order of magnitude of the gravitational acceleration is approximately $10^{-11} \mathrm{~m} / \mathrm{s}^{2}$. Therefore we can conclude that when the 3D surface becomes smooth (blue in the example figure above and in most figures shown in the Appendix), interstellar space is reached and the motion is uniform and rectilinear. The regions of influence of the stars in general do not intersect each other. Note that these regions should not

[^2]be mistaken for "spheres of influence", the definition of which requires the presence of a dominant central body: at this stage the body of the Galaxy has been neglected and $N$ point-like bodies in empty space are being considered.


Figure 11: Surface of acceleration levels (in logarithmic scale) in the solar neighbourhood on the galactic plane. The three sharp peaks are due to Sun, Alpha Centauri and Kruger 60.

The outcome of this experiment yields further evidence that the nearby stars do not perturb each other, their gravitational acceleration peaks being well separated.
The original idea of plotting the gravitational hierarchies, defined as maps of the gravitational potential domains of the n stars, turned out not to be meaningful: the gradient of the gravitational potential (i.e., the acceleration) is the most appropriate means to measure the relative contributions of a system of $N$ bodies to the motion of a test particle. The acceleration domains are nothing but spherical regions surrounding each star, as suggested by plots like Figure 10 and Figure 11.

### 3.2 Motion in the field of the Galactic potential

Motions in the Milky Way are commonly expressed with respect to the

- FSR: the "fundamental" standard of rest with respect to the galactic center, or
- LSR: the "local" standard of rest with respect to a circular orbit at the Sun's radius.

The FSR is a non-rotating reference frame centered at the galactic center and is used when describing the Galaxy as a whole. The LSR is more useful for describing motions near the Sun. The usual notation for the velocity expressed in the Fundamental Standard of Rest is through a vector $(\Pi, \Theta, Z)$, where $\Pi$ is the velocity component directed radially away from the centre, $Z$ is the velocity component perpendicular to the galactic plane, taken as positive in the direction of the North Galactic Pole, and lastly $\Theta$ is the
tangential component normal to the other two, positive in the direction of galactic rotation (clockwise as seen from the North Galactic pole). Suppose now that the mass distribution in our Galaxy is axisymmetric, so that the gravitational forces at any position in the galactic plane are directed radially toward the centre and that the forces are independent of time. Then at each position in the galactic plane there will be a particular velocity vector with components $(\Pi, \Theta, Z)=\left(0, \Theta_{0}, 0\right)$ such that a star moving with this velocity follows a circular orbit around the centre of the Galaxy. A point moving with just this velocity defines the Local Standard of Rest (LSR) and $\Theta_{0}$ is called the circular velocity (Mihalas \& Binney, 1981). The relation between the LSR, the FSR and the heliocentric galactic reference frame is shown in Figure 12. Note that both the FSR and the LSR are left-handed systems, while the heliocentric galactic system is right-handed.


Figure 12: The three basic reference frames for describing stellar motions: the Heliocentric Galactic reference frame, the Local Standard of Rest and the Fundamental Standard of Rest.

The Sun's speed relative to the LSR is determined on the basis of the space motions (radial velocities and proper motions) of the stars relative to the Sun. The result depends on the types and numer of objects involved in the computation. In agreement with Carraro \& Chiosi (1994), we adopted the Standar Solar Motion ( $u_{S}, v_{S}, w_{S}$ ) defined to be the solar motion relative to the stars most commonly listed in general catalogues of radial velocity and proper motion, which are typically of spectral types A through G including dwarfs, giants and supergiants (Mihalas \& Binney, 1981): $u_{S}=-10.4 \mathrm{~km} / \mathrm{s}, v_{S}=14.8 \mathrm{~km} / \mathrm{s}, w_{S}$ $=7.3 \mathrm{~km} / \mathrm{s}$.

Direct measurements of $\Theta_{0}$ based on radial velocities of globular clusters or spheroidal-component stars in our Galaxy or of external galaxies in the Local Group, yield values in the range $200 \leq \Theta_{0} \leq 300 \mathrm{~km} / \mathrm{s}$. Following Allen \& Santillán (1991) and Carraro \& Chiosi (1994), we adopted the values $220 \mathrm{~km} / \mathrm{s}$ and 8.5 kpc respectively for $\Theta_{0}$ and for the distance $R_{0}$ of the Sun from the galactic centre.

A higher level of precision is reached when the motions of the stars are computed by taking into account the force field produced by Galaxy. A simple, yet realistic model of the potential of the Galaxy can be found in Allen \& Santillán (1991) and Carraro \& Chiosi (1994). This model is implemented in the

GRINTON software tool, kindly made available to us by Dr. Carraro. This galactic model consists of three mass components: a spherical central bulge, a flattened disk and a massive spherical halo. The total mass of the model is $2 \cdot 10^{11} M_{\text {sun }}$. Each component provides its own contribution to the analytical representation of the overall gravitational potential, the gradient of which provides the radial and vertical components of the gravitational force. The second order differential equations that describe the motion of a star are numerically integrated using the Everhardt Radau integrator.

We applied the model to the 77 selected stars and performed an integration over 200 million years with time steps of 1 My . As expected, the resulting orbits shown in Figure 13 are very different from the straight lines obtained from the $N$-body integrations. Figure 13 also shows the important fact that the configuration of stars currently constituting the Solar Neighborhood is bound to disrupt, not being gravitationally bound as a subsystem. The solar companions are thus totally accidental and vary dramatically on a timescale much shorter than the period of galactic rotation.


Figure 13: The orbits of the nearby stars during a period of 200 My driven by the galactic potential. The thick line indicates the orbit of the Sun.
The " $N$-body" approach presented in the previous section is obviously highly inadequate to describe stellar motions over time intervals longer than, say, 100 Ky . However, for shorter periods the isolated $N$ body scheme is a sufficient approximation which covers typical to extreme transfer times of interstellar travel. Figure 14 and Figure 15 show the orbits of the stars in the solar neighborhood over a period of 15,000 years as determined by numerical integration respectively of an isolated $N$-body system and the same system of non-interacting particles each moving under the driving acceleration of the galactic potential. No appreciable differences can be observed in the evolution of the system.

Stellar orbits over 15 thousand years (based on galactic potential)


Figure 14: Stellar orbits over 15,000 years as determined by integration of the equations of motion with respect to the galactic potential.


Figure 15: Stellar orbits over 15,000 years as determined by integration of the equations of motion of the N -body problem.

### 3.3 The spheres of influence

As a further comparison between the " $N$-body" and the "galactic potential" approaches, we computed the radii $R_{S I}$ of the spheres of influence for each star in the database according to the well-known formula (Roy, 1972):

$$
\begin{equation*}
R_{S I}=r\left(\frac{m_{*}}{M_{G}}\right)^{2 / 5} \tag{4}
\end{equation*}
$$

written for a star of mass $m_{*}$ orbiting at a distance $r$ from the galactic centre, $M_{G}$ being the total mass of the Galaxy set equal to $2 \cdot 10^{11} M_{\text {sun }}$. The results are reported in Table 8 and illustrated in Figure 16: the computations show (blue circles in the plot) that there are only two cases of intersection, i.e., Alpha Centauri with Proxima Centauri and Procyon with Luyten Star. As we shall discuss later, this observation is not sufficient to conclude, for example, that Proxima is bound to Alpha Cen.

| Name | M | $r$ | $\mathbf{R}_{\text {SI }}$ | Name | M | $r$ | $\mathbf{R}_{\text {SI }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Msun | Kpc | pc |  | Msun | Kpc | pc |
| Sun | 1.000 | 8.50000 | 0.25645 | GJ 380 | 0.642 | 8.50289 | 0.21487 |
| Proxima Centauri | 0.107 | 8.49910 | 0.10489 | GJ 388 | 0.393 | 8.50228 | 0.17656 |
| alpha Centauri | 2.060 | 8.49904 | 0.34238 | GJ 832 | 0.503 | 8.49666 | 0.19474 |
| Barnard's Star | 0.166 | 8.49848 | 0.12502 | GJ 682 | 0.213 | 8.49517 | 0.13807 |
| Wolf 359 | 0.092 | 8.50058 | 0.09875 | omicron 2 Eri | 1.582 | 8.50370 | 0.30823 |
| Lalande 21185 | 0.464 | 8.50105 | 0.18865 | EV Lacertae | 0.285 | 8.50091 | 0.15524 |
| Sirius | 2.491 | 8.50177 | 0.36953 | 70 Ophiuchi | 1.625 | 8.49566 | 0.31126 |
| UV Ceti | 0.211 | 8.50066 | 0.13764 | Altair | 1.710 | 8.49659 | 0.31771 |
| Ross 154 | 0.171 | 8.49714 | 0.12649 | EI Cancri | 0.203 | 8.50373 | 0.13558 |
| Ross 248 | 0.121 | 8.50104 | 0.11020 | GJ 445 | 0.240 | 8.50255 | 0.14495 |
| epsilon Eri | 0.850 | 8.50207 | 0.24037 | GJ 1005 | 0.282 | 8.49987 | 0.15456 |
| Lacaille 9352 | 0.529 | 8.49866 | 0.19876 | GJ 526 | 0.526 | 8.49838 | 0.19830 |
| Ross 128 | 0.156 | 8.49995 | 0.12197 | Stein 2051 | 0.724 | 8.50466 | 0.22550 |
| EZ Aquarii | 0.306 | 8.49872 | 0.15967 | GJ 754 | 0.158 | 8.49483 | 0.12252 |
| Procyon | 2.069 | 8.50283 | 0.34313 | Wolf 1453 | 0.566 | 8.50480 | 0.20435 |
| 61 Cygni | 1.333 | 8.49954 | 0.28768 | sigma Draconi | 0.892 | 8.50105 | 0.24502 |
| DM+59 1915 | 0.610 | 8.49996 | 0.21044 | GJ 229 | 0.606 | 8.50362 | 0.20998 |
| GX Andromedae | 0.649 | 8.50152 | 0.21577 | GJ 693 | 0.262 | 8.49488 | 0.14999 |
| Eps Indi | 0.838 | 8.49778 | 0.23889 | Wolf 1055 | 0.567 | 8.49556 | 0.20427 |
| DX Cancri | 0.087 | 8.50293 | 0.09660 | Ross 47 | 0.196 | 8.50563 | 0.13372 |
| Tau Ceti | 0.921 | 8.50103 | 0.24818 | GJ 570 | 1.708 | 8.49540 | 0.31752 |
| RECONS 1 | 0.113 | 8.50069 | 0.10722 | GJ 908 | 0.507 | 8.50020 | 0.19544 |
| YZ Ceti | 0.136 | 8.50063 | 0.11547 | eta Cassiopei | 1.709 | 8.50319 | 0.31788 |
| Luyten's Star | 0.257 | 8.50315 | 0.14898 | GJ 588 | 0.464 | 8.49484 | 0.18852 |
| Kapteyn's Star | 0.393 | 8.50106 | 0.17653 | Ross 882 | 0.225 | 8.50471 | 0.14129 |
| AX Microscopium | 0.600 | 8.49718 | 0.20899 | 36 Ophiuchi | 2.406 | 8.49408 | 0.36410 |
| Kruger 60 | 0.439 | 8.50102 | 0.18452 | GJ 783 | 1.024 | 8.49483 | 0.25874 |
| Ross 614 | 0.267 | 8.50342 | 0.15128 | 82 Eridani | 0.971 | 8.50112 | 0.25348 |
| Wolf 1061 | 0.261 | 8.49613 | 0.14978 | delta Pavonis | 1.095 | 8.49555 | 0.26579 |
| WD 0046+051 | 0.500 | 8.50123 | 0.19438 | QY Aurigae | 0.326 | 8.50577 | 0.16390 |
| GJ 1 | 0.481 | 8.49898 | 0.19134 | HN Librae | 0.220 | 8.49584 | 0.13988 |
| Wolf 424 | 0.236 | 8.49955 | 0.14393 | GJ 338 | 1.196 | 8.50438 | 0.27563 |
| TZ Arietis | 0.140 | 8.50259 | 0.11684 | GJ 784 | 0.577 | 8.49482 | 0.20569 |
| GJ 687 | 0.390 | 8.50058 | 0.17598 | Wolf 562y | 0.300 | 8.49522 | 0.15835 |
| LHS 292 | 0.083 | 8.50053 | 0.09477 | EQ Pegasi | 0.499 | 8.50074 | 0.19422 |
| GJ 674 | 0.361 | 8.49569 | 0.17053 | GJ 661 | 0.719 | 8.49835 | 0.22471 |
| GJ 1002 | 0.109 | 8.50008 | 0.10568 | Wolf 630 | 1.307 | 8.49409 | 0.28524 |
| Ross 780 | 0.273 | 8.49854 | 0.15254 | GJ 625 | 0.372 | 8.49943 | 0.17266 |
| WX Ursae Maj | 0.582 | 8.50216 | 0.20658 |  |  |  |  |

Table 8: Size of the sphere of influence, mass and distance from the galactic centre of the 77 stars in the solar neighbourhood.


Figure 16: 3D representation of the size of the spheres of influence of the 77 stars in the solar neighbourhood. The pairs of spheres coloured in blue (Alpha Centauri AB and Proxima Centauri) and cyan (Procyon and Luyten star) are the only cases of intersection in the whole system.

The analysis presented in this section shows that the motion of the stars is dominated by the galactic potential and not by local gravitational interactions, except in the case of multiple systems which have been determined to be closely bound or happening to interact due to fortuitous close encounters (intersecting influence spheres).
Admittedly, the analysis carried out through numerical simulations is rather unsophisticated, and more detailed and modern models of the galactic potential could be used, including the perturbations due to the compressional waves forming the spiral arms. However, it is felt that the purpose of the present research is well served even under such restrictions.

## 4 INTERNAL KINEMATICS AND DYNAMICS OF MULTI-STAR SYSTEMS

In this section we give an overview of the major findings concerning the internal dynamics of some of the closest double and triple systems and of two known planetary systems. This will serve as a background for the subsequent considerations on the trajectory design for a space mission to the nearby stars.

### 4.1 Is Proxima in orbit about Alpha Cen A/B?

Proxima Centauri is the closest star to the Sun. The similarity of its distance, angular coordinates and proper motion to those of the binary system Alpha Centauri A/B has always led to questions about the relationship between these two objects. The question of whether or not Proxima is gravitationally bound to Alpha Cen A/B has long been settled in the affirmative, which led to refer to Proxima as Alpha Cen C. Unfortunately, the available measurements of the kinematic properties of this two objects do not support this conclusion. Matthews \& Gilmore (1993) give a very clear view of the arguments in favour of one and the other hypothesis: the fact that Proxima Cen is located inside the sphere of influence of Alpha Cen $\mathrm{A} / \mathrm{B}$ does not necessarily mean that the two are bound, the alternative being that Proxima is following a hyperbolic trajectory relative to Alpha Cen. Besides, despite the close similarity between the proper motions, the radial velocities do differ significantly. The result of a numerical search performed by the same authors within a six-dimensional space of astrometric parameters would impose that, in order for the relative velocity of Proxima to be smaller than the escape speed from Alpha Cen, the difference in radial velocity between the two stars must not exceed $0.18 \mathrm{~km} / \mathrm{s}$. During an observing programme carried out at ESO Chile in 1984 a value of $-21.7 \pm 1.8 \mathrm{~km} / \mathrm{s}$ for the radial velocity of Proxima Cen was measured. This determination falls within the required range for the bound statement to be justified but has not yet been confirmed.

Anosova \& Orlov (1995) proposed the hypothesis that this system is part of a stellar moving group and that what we see is nothing but a slow passage of Proxima close to the $\mathrm{A} / \mathrm{B}$ pair.
We have performed the numerical integration of the equations of motion of the three stars with initial conditions taken from Table 5 and the relative motion of A and B derived from the orbital parameters listed in Table 3 and Table 4. According to our results (Figure 17), Proxima is performing a hyperbolic passage relative to Alpha Cen A/B. A further confirmation comes from evaluation of the gravitational energy per unit mass $E$ relative to the barycentre of Alpha Cen A/B:

$$
\begin{equation*}
E=\frac{v_{P A B}^{2}}{2}-\frac{G\left(m_{A B}+m_{P}\right)}{r_{P A B}}=117 \mathrm{~km}^{2} \mathrm{~s}^{-2} \tag{5}
\end{equation*}
$$

where $m_{A B}$ is the mass of the $\mathrm{A} / \mathrm{B}$ system, $m_{P}$ is the mass of Proxima, $r_{P A B}$ and $v_{P A B}$ are the relative distance and speed. The positive value of $E$ indicates that Proxima and Alpha Cen A/B are not bound. If this will be validated by future observations, then the Circular Restricted Three-Body Problem paradigm to the system composed by Alpha Cen A and Proxima cannot be applied.
Our computations show (Figure 17, Figure 18, Figure 19 and Figure 20) that the motion of Proxima is affected by perturbations which exhibit the same frequency as the orbital motion of B around A (Figure 21).

Proxima Cen: distance from Alpha Cen A


Figure 17: Distance between Proxima Centauri and Alpha Centauri $A$ as a function of time as resulting from integration of the equations of motion of the triple system over 500 years with integration step of 0.1 years.


Figure 18: Speed of Proxima Centauri relative to Alpha Centauri A as a function of time as resulting from integration of the equations of motion of the triple system over 500 years with integration step of 0.1 years. The perturbation is due to the relative orbital motion of stars $A$ and $B$. The perturbation is correlated with the relative orbital motion of stars $A$ and $B$ as indicated by the periodicity of the variations which is equal to the orbital period of the two stars.

Proxima Cen : distance from Alpha Cen A


Figure 19: Distance between Proxima Centauri and Alpha Centauri A as a function of time as resulting from integration of the equations of motion of the triple system over 5,000 years with integration step of 1 year. In 4,000 years Proxima will reach the point of closest approach to Alpha Cen A.


Figure 20: Speed of Proxima Centauri relative to Alpha Centauri A as a function of time as resulting from integration of the equations of motion of the triple system over 5,000 years with integration step of 1 year. The perturbation is due to the relative orbital motion of stars $A$ and $B$.


Figure 21: Relative distance between Alpha Cen $A$ and $B$ as a function of time as resulting from integration of the equations of motion of the triple system over 500 years with integration step of 0.1 years.

Since the results of our computations and the energy evaluation critically depend on the initial conditions determined from rather imprecise observations, at this stage we cannot make any final statement concerning the dynamical relationship between Proxima and Alpha Cen. The available measurements lead to controversial conclusions which can only be settled by further, more precise and accurate determinations of the their kinematic properties.
From precise radial velocities (Figure 22) obtained of both Alpha Cen A and B, the mass ratio of the double system was determined by Murdoch \& Hearnshaw (1993) to be $m_{B} / m_{A}=0.75 \pm 0.09$, which agrees with the estimate of 0.80 adopted in the present study.

## The Alpha Cen Mass Ratio



Figure 22: Radial velocities $v_{A}$ of Alpha Cen A plotted versus radial velocities $v_{B}$ of Alpha Cen $B$ in order to derive the mass ratio of the two stars (Murdoch \& Hearnshaw, 1993).

### 4.2 Binary systems

Sirius: Sirius has been known as a double star for about 140 years. However, since the beginning of the $20^{\text {th }}$ century observational, physical and dynamical indications have led to the hypothesis of the existence of a third body in the system. This fact has been reported and discussed by Benest \& Duvent (1995): the authors present an orbital analysis, supported by numerical simulations, of the binary Sirius A/B, whose perturbed motion is better explained by introducing a tiny star revolving around Sirius A.

Van de Bos (1960) reported the details of the reduction procedure to obtain the orbital parameters of Sirius A/B from observations distributed over more than two orbital periods of the system (i.e., more than 100 years).
Thanks to some recent observations made by the Extreme Ultraviolet Explorer (EUVE) satellite, Holberg et al. (1998) have produced new results concerning the physical (temperature and surface gravity) parameters of Sirius B. By combining the Hipparcos parallax of the Sirius system with the new spectroscopic data, the authors obtained a refined mass estimate of $1.034 \pm 0.026 M_{\text {sun }}$ for the white dwarf secondary.

UV Ceti: The orbital elements of the M dwarf binary system L 726-8 composed by UV Ceti and BL Ceti listed in Table 3 and adopted in the course of this study were published by Geyer, Harrington \& Worley (1988). By merging observations made at the U.S. Naval Observatory since 1964 with photographic and visual observations of the relative positions of the two components collected since 1948, the authors obtained a parallax of $0.3711 \pm 0.0040$ arcsec, a proper motion of $3.3299 \pm 0.0006$ arcsec/yr towards $79.78 \pm 0.01$ degrees and a mass ratio of $0.4938 \pm 0.0031$. Then taking $0.375 \pm 0.004$ arcsec as the absolute parallax, the total mass of the system is $0.200 M_{\text {sun }}$ yielding individual masses for the two components of $0.101 M_{\text {sun }}$ and $0.099 \mathrm{M}_{\text {sun }}$.
Procyon: Several orbit determinations for this double system have been published in recent years. Girard et al. (2000) have made a thorough comparison between their own orbital elements and those published by Strand in 1951 and more recently by Irwin et al. (1992) (Table 9). Together with the redetermined astrometric orbit and parallax, Girard et al. provide new estimates for the component masses: the derived masses are $1.497 \pm 0.037 \mathrm{M}_{\text {sun }}$ for the primary and $0.602 \pm 0.015 \mathrm{M}_{\text {sun }}$ for the white dwarf secondary.

| Element | Strand (1951) | Irwin et al. (1992) | Girard et al. (2000) |
| :---: | :---: | :---: | :---: |
| Semi-major axis <br> (arcsec) | $1.217 \pm 0.002$ | $1.179 \pm 0.011$ | $1.232 \pm 0.008$ |
| Eccentricity | 0.40 | $0.365 \pm 0.008$ | $0.407 \pm 0.005$ |
| Inclination <br> (degrees) | $35.7 \pm 0.2$ | $31.9 \pm 0.9$ | $31.1 \pm 0.6$ |
| Angle of node <br> (degrees) | $104.3 \pm 0.3$ | $104.8 \pm 1.5$ | $97.3 \pm 0.3$ |
| Longitude of periastron <br> (degrees) | $89.8 \pm 0.3$ | $88.8 \pm 2.0$ | $92.2 \pm 0.3$ |
| Period <br> (years) | 40.65 | $40.38 \pm 0.15$ | $40.82 \pm 0.06$ |
| Periastron passage <br> (year) | 1927.6 | $1967 \pm 0.16$ | $1967.97 \pm 0.05$ |

Table 9: Astrometric orbital elements of Procyon (Girard et al., 2000): comparisons among the data published by Girard et al. (2000) and those determined by Irwin et al. (1992) and Strand (1951).

### 4.3 Triple systems

We have collected information about the nearest two triple systems listed in our database: Epsilon Indi and EZ Aquarii.
EZ Aquarii: according to the new Sixth Orbit Catalog of Visual Binary Stars, the orbit of stars A and B has a semi-major axis of about 1.22 AU . The orbit has an eccentricity of 0.437 , a period of about 2.25
years and an inclination from the perspective of an observer on Earth of about $112.4^{\circ}$ (Woitas et al., 2000). In addition, star A is a spectroscopic binary (whose companion has been designated as star C) with an orbit period of only 3.8 days (Delfosse et al., 1999).

Epsilon Indi: this star is the title member of the Epsilon Indi stellar moving group (Kovacs \& Foy, 1978). Scholz et al. (2003) identified a brown dwarf as a common proper motion companion (separation of 1459 AU ) to $\varepsilon$ Indi: as such, $\varepsilon$ Indi B is one of the highest proper motion sources outside the Solar System ( $\sim 4.7$ $\operatorname{arcsec} / \mathrm{yr}$ ) and the nearest brown dwarf to the Sun. The separation between the primary and the companion is 402.3 arcsec in the plane of the sky while the separation along the line-of-sight is unknown. Using the age of $\varepsilon$ Indi $A$ as a first estimate for the age of $\varepsilon$ Indi $B$, the authors obtained a mass range of $40-60 \mathrm{M}_{\mathrm{Jup}}$ for this dwarf. In August 2003, the same as well as another team of astronomers found that the brown dwarf had its own brown dwarf companion (McCaughrean et al., 2004). Since then the two brown dwarfs have been called $\varepsilon$ Indi Ba and $\varepsilon$ Indi Bb . By analysing optical and IR survey data, McCaughrean and his collaborators determined a more refined proper motion for the combined $\varepsilon$ Indi $\mathrm{Ba}, \mathrm{Bb}$ system (Table 10). The same authors attribute an orbital period of $\sim 15$ years to the system, thus estimating that a determination of its orbital parameters will be available within a fairly short time.

| Object | $\mu_{\alpha} \cos \delta$ | $\mu_{\delta}$ | Source |
| :---: | :---: | :---: | :---: |
| $\varepsilon$ Indi $\mathrm{Ba}, \mathrm{Bb}$ | $+4131 \pm 71$ | $-2489 \pm 25$ | Scholz et al. (2003) |
| $\varepsilon$ Indi $\mathrm{Ba}, \mathrm{Bb}$ | $+3976 \pm 13$ | $-2500 \pm 14$ | McCaughrean et al. (2004) |
| $\varepsilon$ Indi A | $+3961.41 \pm 0.57$ | $-2538.33 \pm 0.40$ | ESA (1997) |

Table 10: Proper motions for $\varepsilon$ Indi $\mathrm{Ba}, \mathrm{Bb}$ and $\varepsilon$ Indi A . The units are mas/year (McCaughrean et al., 2004).

### 4.4 Planetary systems

Two known planetary systems are present in our star ensemble:

- $\varepsilon$ Eridani: the detection of a planet (called "planet b") was first announced by Campbell et al. (1988) after noting a periodicity in the Doppler measurements of the star. Later (Hatzes et al., 2000; Quillen \& Thorndike, 2002) modelling of dust ring clumping patterns and RV measurements suggested the presence of a relatively smaller planet ("planet c") with about a tenth of a Jupiter mass. Table 11 summarizes the most widely quoted values for the orbital and physical parameters of the two planets.
- Gliese 876: two planets have recently been discovered around this star with the radial velocity method. The basic orbital data are reported in Table 12 (Marcy et al., 1998 ; Marcy et al., 2001).

|  | semimajor axis | period | eccentricity | inclination | mass | diameter |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | AU | years |  | degrees | Earths | Earths |
| $\varepsilon$ Eridani | 0.0 | $\ldots$ | $\ldots$ | $\ldots$ | 280,000 | $94-98$ |
| planet b | 3.3 | 6.85 | 0.61 | $46 ?$ | 381 | $\ldots$ |
| planet c | 40.0 | 280.00 | 0.30 | $46 ?$ | 30 | $\ldots$ |

Table 11: Orbital elements of the planets orbiting Epsilon Eridani (Marcy et al., 1998 ; Marcy et al., 2001).

| name | M•sini | semi-major axis | period | eccentricity | inclination | long. ascend. node | Epoch |
| :---: | :---: | ---: | :---: | ---: | ---: | ---: | ---: |
|  | $\mathrm{M}_{\mathrm{J}}$ | AU | days |  | $\sin \mathrm{i}$ | degrees | JD 2450000 |
| Gl 876 b | 1.89 | 0.21 | 61.02 | 0.10 | $0.6 ?$ | 333 | 106.2 |
| Gl 876 c | 0.56 | 0.13 | 30.10 | 0.27 | $0.6 ?$ | 330 | 31.4 |

Table 12: Orbital elements of the planets orbiting GL 876.

### 4.5 Conclusions

The literature on the nearby stellar systems often contains complementary information and interesting discussions on the dynamical and kinematic properties of these objects. However, our knowledge of the solar neighbourhood remains remarkably sketchy, as often demonstrated by the large uncertainties affecting the determination of many astrometric and physical parameters. In some cases the observations are so imprecise that we are unable to establish the dynamical relationships within stellar systems. Since uncertainties of this kind affect our knowledge of even our nearest stellar system, then the current description of the dynamical evironment that an exploration probe will experience at any other stellar system can only be a very preliminary one.

## 5 SPACE MISSIONS TO THE NEARBY STARS

From the previous investigations we have learnt that the dynamical envronment in which a spacecraft would travel on an exploration mission to the nearby stars is simpler than expected. Outside the sphere of influence of the departure system, i.e., the Solar System, the S/C is entirely under the influence of the galactic potential, whose gradient is however so small as to let the $\mathrm{S} / \mathrm{C}$ travel for a small fraction of the galaxy revolution time as if in the presence of no forces at all.

The S/C interacts with other stars, or star systems, only when it enters their spheres of influence. Therefore no Circular Restricted Three-Body Problem (CR3BP) or Two-Fixed Centers (TFC) dynamical paradigms can be sensibly applied to the $\mathrm{S} / \mathrm{C}$ dynamics during cruise from one star to another. Only when the $\mathrm{S} / \mathrm{C}$ gets close to a star system is it possible to employ such dynamical schemes.

A remarkable consequence of this peculiar dynamical situation is that, by properly imparting velocity impulses, the S/C can be stably positioned anywhere outside the spheres of influence of the nearby stars, irrespective of whether such positions are identifiable with critical points in any of the known dynamical paradigms, like the CR3BP or the TFC paradigms.
It is also worth noting that Lambert-type targeting is also inapplicable. Lambert targeting refers to the determination of the initial velocity of a transfer orbit within the force field of a single primary body. Now, although this role could be played by the axisymmetric galactic potential, the extremely short distance to the nearby stars compared to the typical dimension of our Galaxy makes this approach impracticable. The proper approach to interstellar transfer seems to be a simple straight line orbit.

The fundamental problem of interstellar flight, however, is of course distance (Figure 23). Compressing the time of flight of the transfer journey into the scale of human lifetime requires high speeds and these, in turn, require very energetic means of propulsion. Propulsion can be applied as an initial impulse, but more likely as continuous thrust, as will be considered shortly.


Figure 23: Perspective view of the interstellar distances including the locations of the planets, the boundary between the heliosphere and the interstellar medium, the Oort Cloud and the nearest stars.

In the following subsections we present in summary the outcome of the major past and on-going investigations in the field of interstellar trajectory design. Then we discuss the main issues related to the kinematics of relativistic flight under constant thrust.

### 5.1 Past and on-going studies

### 5.1.1 The Daedalus Project

One of the first detailed design studies of an interstellar spacecraft was conducted between 1973 and 1978 by a group of a dozen scientists and engineers of the British Interplanetary Society, led by Alan Bond (Bond et al., 1978): it demonstrated that high-speed, unmanned travel to the stars is a practical possibility. Certain guidelines were adopted: the Daedalus spacecraft had to use current or near-future technology, be able to reach its destination within a human lifetime and be flexible enough in its design that it could be sent to any of a number of target stars. The selected target was Barnard's Star, a red dwarf lying 5.9 lightyears from the Sun. Although the Alpha Centauri system is closer, evidence available at the time (now considered unreliable) suggested that Barnard's Star might be orbited by at least one planet. To reach Barnard's Star in 50 years (the flight time allotted in the study), a spacecraft would need to cruise at about $12 \%$ of the speed of light, or $36,000 \mathrm{~km} / \mathrm{s}$. This being far beyond the reach of a chemical rocket, the Daedalus team had to consider less conventional alternatives. The design they chose was a form of nuclear-pulse rocket, a propulsion system that had already been investigated during Project Orion. However, whereas Orion would have employed nuclear fission, the Daedalus engineers opted to power their starship by nuclear fusion-in particular, by a highly-efficient technique known as internal confinement fusion: the desired cruising speed could be reached during an acceleration phase lasting four years. Since the design made no provision for deceleration upon arrival, Daedalus would carry 18 autonomous probes, equipped with artificial intelligence, to investigate the star and its environs. En route, Daedalus would make measurements of the interstellar medium.

### 5.1.2 Starwisp

Robert Foward (1985) presented a solution to the interstellar transport problem: an interstellar flyby probe (Starwisp) of wire mesh sail with microcircuits at each intersection. The probe was to be accelerated to near-relativistic speeds by beamed microwave power produced by a solar-power satellite (a Fresnel lens of wire mesh). After a first phase of constant acceleration (as long as the lens can focus on a spot smaller in size than the sail), followed by a phase of decreasing acceleration. In the case of a 4.3 ly transfer (to Alpha Cen), the requirement that Starwisp reaches the target within 21.5 years translates into the following characteristics of the system: sail diameter 1 km , sail weight 16 g , lens mass 50,000 tons, transmitted power 10 GW , maximum spacecraft speed 0.2 c reached within one week after launch.
Forward treats the motion of the spacecraft in interstellar space by neglecting the gravitational attractions of the stars. This is correct, since we know that the probe experiences the gravitational accleration caused by the stars only in their immediate proximity. However, the newtonian formalism by which he describes the motion is not adequate when dealing with relativistic speeds. In a later section we shall discuss the rectilinear motion of a relativistic particle subject to costant acceleration in the framework of the theory of Special Relativity.

### 5.1.3 The Realistic Interstellar Explorer study

The Realistic Interstellar Explorer is a recent feasibility study performed at the NASA Institute for Advanced Concepts (NIAC) by a team led by Dr. Ralph McNutt. The study, documented in a Phase I and a Phase II Final Report (McNutt, 1999; 2003) and in a recent paper by McAdams \& McNutt (2002) designed some strategies and considered some propulsion modes for reaching significant penetration into the interstellar medium (> 1000 AU ) by considering a variety of science goals and orbital mechanics constraints.

A search for the candidate targets (shown in Table 13) for Solar System escape direction was made by taking into account a number of issues: distance from the Sun, spectral characteristics of the target star, habitable planet probability (according to the criteria proposed by Dole, 1964).

| Star name | distance | spectral type | halbitable planet probability |
| :--- | ---: | :--- | :--- |
|  | (light years) |  |  |
| Alpha Cen B | 4.3 | K1 | 0.057 |
| Epsilon Eridani | 10.8 | K2 | 0.033 |
| Tau Ceti | 11.8 | G8 | 0.036 |
| 70 Ophiuchi A | 16.6 | K1 | 0.057 |
| 36 Ophiuchi A | 18.2 | K2 | 0.023 |
| Sigma Draconis | 18.8 | G9 | 0.036 |
| Eta Cassiopeiae A | 19.4 | K9 | 0.057 |
| Delta Pavonis | 19.9 | G7 | 0.057 |
| 82 Eridani | 20.9 | G5 | 0.057 |
| Beta Hydri | 24.4 | G1 | 0.037 |

Table 13: Candidate stars for launch directions including distance, spectral type and habitable planet probability (McNutt, 1999). We reported in grey colour the data concerning Beta Hydri as this star does not belong to our sample, being more than 7 parsecs far from the Sun.

In the typical solar-sail mission design strategy the sail is used first to remove the angular momentum of the Earth and probe about the Sun; the sail is then maneuvered face-on into the Sun at 0.1 to 0.25 AU and solar acceleration pressure accelerates the probe away from the Sun until the sail is jettisoned (at about 5 AU). The approach investigated and proposed by McNutt starts with a Jupiter gravity assist that removes the Earth's angular momentum; then the spacecraft is sent back to the Sun where it reaches a minimum distance of 4 solar radii; there a large propulsive maneuver is applied which puts the probe in a highenergy ballistic escape trajectory from the Solar System. Computations showed that a limiting ecliptic
latitude for the target must be imposed (within $\pm 32.7^{\circ}$ ) in order to reduce the hyperbolic trajectory turn angle at perihelion. This constraint changes and shortens the list of candidate targets (Table 14). A perihelion $\Delta V$ of $14.801 \mathrm{~km} / \mathrm{s}$ in the spacecraft velocity direction delivers the spacecraft to Solar-Systemescape conditions of $20 \mathrm{AU} / \mathrm{y}$ yar for $32.7^{\circ}$ ecliptic latitude of the target star.

The author investigated mission trajectories toward a variety of targets matching the desired characteristics. As an example, a probe could be launched toward Epsilon Eridani in 2011 (Figure 24), pass within $653,300 \mathrm{~km}$ of Jupiter at $23.527 \mathrm{~km} / \mathrm{s}$ with a $24.7^{\circ}$ approach phase angle and perform a $15.431 \mathrm{~km} / \mathrm{s}$ perihelion $\Delta \mathrm{V}$.


Figure 24: Solar System escape trajectory for a mission toward Epsilon Eridani (from McNutt, 1999).

The Jupiter flyby lowers perihelion from 1.02 AU to 0.02 AU , lowers aphelion from 11.88 AU to 5.04 AU and increases orbital inclination in order to provide the proper orientation for the perihelion burn. Two years later a $15.31 \mathrm{~km} / \mathrm{s}$ perihelion $\Delta \mathrm{V} 4.6^{\circ}$ from the spacecraft velocity drection sends the spacecraft toward Epsilon Eridani at 20.2 AU/year.

A closer look at several technology advances needed for this interstellar precursor mission includes consideration of solar thermal propulsion for the near-Sun maneuvre, although this as well as other solutions require more study.

| Star name | spectral type | ecliptic longitude | ecliptic latitude |
| :--- | :---: | ---: | ---: |
|  |  | $\operatorname{deg}$ | deg |
| Epsilon Eridani | K2 | 48.29 | -27.76 |
| Tau Ceti | G8 | 17.66 | -24.77 |
| Van Maanen 2 | DG | 13.40 | 0.11 |
| Procyon 61421 | F5 | 115.79 | -16.02 |
| 191408 | K3 | 297.06 | -15.68 |
| 131977 A | K5 | 237.13 | -1.95 |
| 36 Ophiuchi | K1 | 259.96 | -3.54 |

Table 14: Candidate stars for launch directions with ecliptic latitude limits (McNutt, 1999).

### 5.2 Transfer phase: relativistic interstellar flight under constant thrust

After travelling through space for more than 26 years, Voyager 1 reached 90 AU from the Sun at the end of 2003. With its Solar-System escape speed of 3.6 AU/yr it would take almost 74,000 years to reach the
distance of Proxima Cen. Even at the much higher speed of $20 \mathrm{AU} / \mathrm{yr}$ planned by McNutt to bring a spacecraft to 1000 AU in 50 years, Proxima Cen would be approached in more than 13,000 years. In summary, the investigations made so far indicate that interstellar missions with launch in the near future and ending within a few decades can only be targeted to destinations between a few hundred to one thousand AU of the Sun, unless dramatic technological developments enabling relativistic flight occur.
With this in mind and for the sake of completeness we have made some computations based on the assumption that the probe can attain relativistic speeds. Following Banfi (2000), we have computed the characteristics of the flight made by a starship under constant thrust on a rectilinear trajectory: the path $s$ is divided into two equal parts of length $s / 2$; in the first half the motion takes place under constant acceleration $a$, during the second half the spacecraft is subject to a constant and opposite deceleration equal to $-a$. According to the theory of Special Relativity, the relationship between the distance $s / 2$ and the coordinated time $t$ measured by an inertial observer is given by

$$
\begin{equation*}
\frac{s}{2}=\frac{c^{2}}{a}\left\{\left[1+\left(\frac{a t}{c}\right)^{2}\right]^{1 / 2}-1\right\} \tag{6}
\end{equation*}
$$

where $c$ is the speed of light. The speed $u$ at time $t$ can be determined by

$$
\begin{equation*}
u=\frac{a t}{\left[1+\left(\frac{a t}{c}\right)^{2}\right]^{1 / 2}} . \tag{7}
\end{equation*}
$$

The speed reaches a maximum at $s / 2$ and then decreases to the initial value at the end of the flight. The proper time $\tau$ (i.e., the time measured by an onboard observer) at mid-course is related to the distance $s / 2$ as

$$
\begin{equation*}
\tau=\frac{c}{a} \cosh ^{-1}\left(1+\frac{a s}{2 c^{2}}\right) . \tag{8}
\end{equation*}
$$

The relationship between proper time $\tau$ and coordinated time $t$ is:

$$
\begin{equation*}
\sinh \left(\frac{a \tau}{c}\right)=\frac{a t}{c} \tag{9}
\end{equation*}
$$

With the above formulas and assuming various acceleration levels (between 0.5 and $10 \mathrm{~m} / \mathrm{s}^{2}$ ), we determined the coordinated and proper time of flight and the maximum ratio $\beta=u / c$ for transfers to the selected 77 stars. The results are illustrated in Figure 25 and in Figure 26. For three acceleration levels the results are also listed in Table 15. By travelling under a constant thrust of $0.5 \mathrm{~m} / \mathrm{s}^{2}$, it takes 17.8 years to the nearest star (Proxima Centauri), 38.7 years to the furthest (GJ 625) according to an on-board clock, while for an observer on Earth the same transfers would last 18.4 years and 45.8 years, respectively. Under a much higher acceleration ( $10 \mathrm{~m} / \mathrm{s}^{2}$ ) these values become much shorter: 3.5 years of on-board time (or 5.8 of coordinated time) to get to Proxima Centauri, 6.1 years ( 23.3 years) to GJ 625 and the speed of the spacecraft at mid-flight would be very close to the speed of light ( $u / \mathrm{c}>0.9$ ). The total mission duration is obtained by adding the time necessary for the data to be transmitted to Earth, which amounts to 4.3 years for a mission to Proxima and 21.5 years for a journey to GJ 625.

Coordinate and proper time vs. target distance


Figure 25: Coordinated and proper time of flight for transfers to the selected 77 stars according to various acceleration levels. Computations have been performed assuming relativistic speed under constant thrust.


Figure 26: Maximum $u / c$ for transfers to the selected 77 stars according to various acceleration levels. Computations have been performed assuming relativistic speed under constant thrust.

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| Name | $\mathrm{a}=0.5 \mathrm{~m} \mathrm{~s}^{-2}$ |  |  | $\mathrm{a}=3 \mathrm{~m} \mathrm{~s}^{-2}$ |  |  | $\mathrm{a}=6 \mathrm{~m} \mathrm{~s}^{-2}$ |  |  | $\mathrm{a}=10 \mathrm{~m} \mathrm{~s}^{-2}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\tau$ (years) | t (years) | $\beta$ | $\tau$ (years) | t (years) | $\beta$ | $\tau$ (years) | t (years) | $\beta$ | $\tau$ (years) | t (years) | $\beta$ |
| Proxima Centauri | 17.76 | 18.41 | 0.436 | 6.96 | 8.45 | 0.800 | 4.72 | 6.68 | 0.903 | 3.49 | 5.82 | 0.951 |
| alpha Centauri | 18.04 | 18.73 | 0.442 | 7.06 | 8.62 | 0.806 | 4.79 | 6.83 | 0.907 | 3.54 | 5.97 | 0.953 |
| Barnard's Star | 21.02 | 22.11 | 0.503 | 8.12 | 10.54 | 0.857 | 5.45 | 8.56 | 0.938 | 3.99 | 7.63 | 0.970 |
| Wolf 359 | 23.92 | 25.53 | 0.557 | 9.12 | 12.61 | 0.894 | 6.06 | 10.48 | 0.957 | 4.39 | 9.49 | 0.981 |
| Lalande 21185 | 24.67 | 26.43 | 0.571 | 9.37 | 13.18 | 0.901 | 6.21 | 11.01 | 0.961 | 4.49 | 10.01 | 0.982 |
| Sirius | 25.08 | 26.94 | 0.578 | 9.51 | 13.50 | 0.905 | 6.29 | 11.31 | 0.963 | 4.55 | 10.30 | 0.983 |
| UV Ceti | 25.29 | 27.19 | 0.582 | 9.58 | 13.66 | 0.907 | 6.33 | 11.46 | 0.964 | 4.57 | 10.45 | 0.984 |
| Ross 154 | 26.58 | 28.80 | 0.604 | 10.00 | 14.70 | 0.918 | 6.58 | 12.45 | 0.969 | 4.74 | 11.42 | 0.986 |
| Ross 248 | 27.41 | 29.85 | 0.617 | 10.27 | 15.40 | 0.925 | 6.74 | 13.11 | 0.972 | 4.84 | 12.07 | 0.988 |
| epsilon Eri | 27.66 | 30.17 | 0.622 | 10.35 | 15.61 | 0.927 | 6.79 | 13.31 | 0.973 | 4.87 | 12.27 | 0.988 |
| Lacaille 9352 | 27.94 | 30.52 | 0.626 | 10.44 | 15.85 | 0.929 | 6.84 | 13.54 | 0.974 | 4.91 | 12.49 | 0.989 |
| Ross 128 | 28.16 | 30.80 | 0.629 | 10.51 | 16.04 | 0.930 | 6.88 | 13.72 | 0.974 | 4.93 | 12.67 | 0.989 |
| EZ Aquarii | 28.58 | 31.35 | 0.636 | 10.65 | 16.42 | 0.933 | 6.96 | 14.07 | 0.976 | 4.99 | 13.02 | 0.990 |
| Procyon | 28.75 | 31.57 | 0.639 | 10.70 | 16.56 | 0.934 | 6.99 | 14.21 | 0.976 | 5.01 | 13.16 | 0.990 |
| 61 Cygni | 28.75 | 31.57 | 0.639 | 10.70 | 16.56 | 0.934 | 6.99 | 14.21 | 0.976 | 5.01 | 13.16 | 0.990 |
| DM+59 1915 | 28.90 | 31.76 | 0.641 | 10.75 | 16.69 | 0.935 | 7.02 | 14.34 | 0.976 | 5.02 | 13.28 | 0.990 |
| GX Andromedae | 29.01 | 31.91 | 0.643 | 10.78 | 16.80 | 0.936 | 7.04 | 14.44 | 0.977 | 5.04 | 13.38 | 0.990 |
| Eps Indi | 29.25 | 32.22 | 0.646 | 10.86 | 17.01 | 0.937 | 7.08 | 14.65 | 0.977 | 5.07 | 13.58 | 0.990 |
| DX Cancri | 29.25 | 32.22 | 0.647 | 10.86 | 17.01 | 0.937 | 7.08 | 14.65 | 0.977 | 5.07 | 13.59 | 0.990 |
| Tau Ceti | 29.32 | 32.32 | 0.648 | 10.88 | 17.08 | 0.938 | 7.10 | 14.71 | 0.978 | 5.07 | 13.65 | 0.990 |
| RECONS 1 | 29.45 | 32.48 | 0.649 | 10.92 | 17.19 | 0.938 | 7.12 | 14.82 | 0.978 | 5.09 | 13.75 | 0.991 |
| YZ Ceti | 29.61 | 32.70 | 0.652 | 10.97 | 17.34 | 0.939 | 7.15 | 14.96 | 0.978 | 5.11 | 13.90 | 0.991 |
| Luyten's Star | 29.88 | 33.05 | 0.656 | 11.06 | 17.59 | 0.941 | 7.20 | 15.20 | 0.979 | 5.14 | 14.13 | 0.991 |
| Kapteyn's Star | 30.35 | 33.68 | 0.663 | 11.20 | 18.02 | 0.943 | 7.28 | 15.62 | 0.980 | 5.19 | 14.55 | 0.992 |
| AX Microscopium | 30.45 | 33.82 | 0.665 | 11.24 | 18.12 | 0.944 | 7.30 | 15.71 | 0.980 | 5.21 | 14.64 | 0.992 |
| Kruger 60 | 30.77 | 34.23 | 0.669 | 11.33 | 18.42 | 0.946 | 7.36 | 16.00 | 0.981 | 5.24 | 14.92 | 0.992 |
| Ross 614 | 30.99 | 34.53 | 0.672 | 11.40 | 18.63 | 0.947 | 7.40 | 16.20 | 0.981 | 5.27 | 15.12 | 0.992 |
| Wolf 1061 | 31.50 | 35.23 | 0.680 | 11.56 | 19.12 | 0.949 | 7.49 | 16.68 | 0.982 | 5.33 | 15.60 | 0.993 |
| WD 0046+051 | 31.76 | 35.59 | 0.683 | 11.64 | 19.38 | 0.950 | 7.53 | 16.93 | 0.983 | 5.36 | 15.84 | 0.993 |
| GJ 1 | 31.94 | 35.83 | 0.686 | 11.69 | 19.56 | 0.951 | 7.56 | 17.10 | 0.983 | 5.38 | 16.01 | 0.993 |
| Wolf 424 | 32.02 | 35.95 | 0.687 | 11.72 | 19.64 | 0.952 | 7.58 | 17.18 | 0.983 | 5.39 | 16.09 | 0.993 |
| TZ Arietis | 32.23 | 36.23 | 0.690 | 11.78 | 19.85 | 0.953 | 7.62 | 17.38 | 0.984 | 5.41 | 16.29 | 0.993 |
| GJ 687 | 32.53 | 36.64 | 0.694 | 11.87 | 20.15 | 0.954 | 7.67 | 17.67 | 0.984 | 5.44 | 16.57 | 0.993 |
| LHS 292 | 32.54 | 36.66 | 0.694 | 11.88 | 20.16 | 0.954 | 7.67 | 17.68 | 0.984 | 5.44 | 16.59 | 0.993 |
| GJ 674 | 32.54 | 36.67 | 0.694 | 11.88 | 20.16 | 0.954 | 7.67 | 17.69 | 0.984 | 5.44 | 16.59 | 0.993 |
| GJ 1002 | 33.06 | 37.39 | 0.701 | 12.04 | 20.69 | 0.956 | 7.76 | 18.20 | 0.985 | 5.50 | 17.10 | 0.994 |
| Ross 780 | 33.09 | 37.43 | 0.702 | 12.04 | 20.72 | 0.956 | 7.76 | 18.23 | 0.985 | 5.50 | 17.13 | 0.994 |
| WX Ursae Maj | 33.58 | 38.12 | 0.708 | 12.19 | 21.23 | 0.958 | 7.85 | 18.72 | 0.986 | 5.56 | 17.62 | 0.994 |
| GJ 380 | 33.60 | 38.15 | 0.708 | 12.20 | 21.25 | 0.958 | 7.85 | 18.74 | 0.986 | 5.56 | 17.64 | 0.994 |
| GJ 388 | 33.69 | 38.28 | 0.709 | 12.22 | 21.35 | 0.959 | 7.87 | 18.83 | 0.986 | 5.57 | 17.73 | 0.994 |
| GJ 832 | 33.84 | 38.48 | 0.711 | 12.27 | 21.50 | 0.959 | 7.89 | 18.98 | 0.986 | 5.58 | 17.87 | 0.994 |
| GJ 682 | 34.08 | 38.83 | 0.715 | 12.34 | 21.76 | 0.960 | 7.93 | 19.23 | 0.987 | 5.61 | 18.13 | 0.995 |
| omicron 2 Eri | 34.14 | 38.91 | 0.715 | 12.36 | 21.81 | 0.960 | 7.94 | 19.29 | 0.987 | 5.62 | 18.18 | 0.995 |
| EV Lacertae | 34.21 | 39.02 | 0.716 | 12.38 | 21.90 | 0.961 | 7.95 | 19.37 | 0.987 | 5.62 | 18.26 | 0.995 |
| 70 Ophiuchi | 34.38 | 39.26 | 0.718 | 12.43 | 22.08 | 0.961 | 7.98 | 19.55 | 0.987 | 5.64 | 18.44 | 0.995 |
| Altair | 34.46 | 39.38 | 0.719 | 12.45 | 22.17 | 0.961 | 8.00 | 19.63 | 0.987 | 5.65 | 18.52 | 0.995 |
| EI Cancri | 34.78 | 39.84 | 0.723 | 12.55 | 22.51 | 0.963 | 8.05 | 19.97 | 0.988 | 5.68 | 18.85 | 0.995 |
| GJ 445 | 35.25 | 40.51 | 0.729 | 12.68 | 23.02 | 0.964 | 8.13 | 20.46 | 0.988 | 5.73 | 19.35 | 0.995 |
| GJ 1005 | 35.25 | 40.52 | 0.729 | 12.68 | 23.02 | 0.964 | 8.13 | 20.47 | 0.988 | 5.73 | 19.35 | 0.995 |
| GJ 526 | 35.39 | 40.73 | 0.731 | 12.73 | 23.18 | 0.965 | 8.15 | 20.62 | 0.988 | 5.75 | 19.50 | 0.995 |
| Stein 2051 | 35.72 | 41.21 | 0.735 | 12.82 | 23.54 | 0.966 | 8.20 | 20.97 | 0.989 | 5.78 | 19.85 | 0.995 |
| GJ 754 | 36.23 | 41.96 | 0.741 | 12.97 | 24.12 | 0.967 | 8.29 | 21.54 | 0.989 | 5.84 | 20.42 | 0.996 |
| Wolf 1453 | 36.23 | 41.97 | 0.741 | 12.97 | 24.13 | 0.967 | 8.29 | 21.54 | 0.989 | 5.84 | 20.42 | 0.996 |
| sigma Draconi | 36.38 | 42.20 | 0.743 | 13.02 | 24.30 | 0.968 | 8.31 | 21.71 | 0.990 | 5.85 | 20.59 | 0.996 |
| GJ 229 | 36.43 | 42.26 | 0.743 | 13.03 | 24.35 | 0.968 | 8.32 | 21.76 | 0.990 | 5.86 | 20.64 | 0.996 |
| GJ 693 | 36.57 | 42.47 | 0.745 | 13.07 | 24.52 | 0.968 | 8.34 | 21.92 | 0.990 | 5.87 | 20.80 | 0.996 |
| Wolf 1055 | 36.64 | 42.58 | 0.746 | 13.09 | 24.59 | 0.968 | 8.35 | 22.00 | 0.990 | 5.88 | 20.87 | 0.996 |
| Ross 47 | 36.70 | 42.67 | 0.747 | 13.11 | 24.67 | 0.969 | 8.36 | 22.07 | 0.990 | 5.88 | 20.95 | 0.996 |
| GJ 570 | 36.75 | 42.75 | 0.747 | 13.12 | 24.73 | 0.969 | 8.37 | 22.13 | 0.990 | 5.89 | 21.00 | 0.996 |
| GJ 908 | 36.89 | 42.95 | 0.749 | 13.16 | 24.89 | 0.969 | 8.39 | 22.29 | 0.990 | 5.90 | 21.16 | 0.996 |
| eta Cassiopei | 36.90 | 42.97 | 0.749 | 13.17 | 24.90 | 0.969 | 8.40 | 22.30 | 0.990 | 5.90 | 21.17 | 0.996 |
| GJ 588 | 36.90 | 42.98 | 0.749 | 13.17 | 24.90 | 0.969 | 8.40 | 22.30 | 0.990 | 5.90 | 21.18 | 0.996 |
| Ross 882 | 36.99 | 43.10 | 0.750 | 13.19 | 25.00 | 0.969 | 8.41 | 22.40 | 0.990 | 5.91 | 21.27 | 0.996 |
| 36 Ophiuchi | 36.99 | 43.11 | 0.750 | 13.19 | 25.00 | 0.969 | 8.41 | 22.40 | 0.990 | 5.91 | 21.27 | 0.996 |


| GJ 783 | 37.22 | 43.45 | 0.753 | 13.26 | 25.27 | 0.970 | 8.45 | 22.66 | 0.990 | 5.94 | 21.53 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 82 Eridani | 37.25 | 43.50 | 0.753 | 13.27 | 25.31 | 0.970 | 8.45 | 22.70 | 0.990 | 5.94 | 21.57 |
| delta Pavonis | 37.38 | 43.70 | 0.754 | 13.30 | 25.46 | 0.970 | 8.47 | 22.85 | 0.991 | 5.95 | 21.72 |
| QY Aurigae | 37.47 | 43.84 | 0.755 | 13.33 | 25.57 | 0.971 | 8.49 | 22.96 | 0.991 | 5.96 | 21.82 |
| HN Librae | 37.48 | 43.85 | 0.755 | 13.33 | 25.58 | 0.971 | 8.49 | 22.96 | 0.991 | 5.96 | 21.83 |
| GJ 338 | 37.56 | 43.97 | 0.756 | 13.35 | 25.67 | 0.971 | 8.50 | 23.06 | 0.991 | 5.97 | 21.92 |
| GJ 784 | 37.66 | 44.12 | 0.758 | 13.38 | 25.79 | 0.971 | 8.52 | 23.17 | 0.991 | 5.98 | 22.04 |
| Wolf 562y | 37.86 | 44.44 | 0.760 | 13.44 | 26.04 | 0.972 | 8.55 | 23.42 | 0.991 | 6.00 | 22.28 |
| EQ Pegasi | 38.04 | 44.71 | 0.762 | 13.49 | 26.25 | 0.972 | 8.58 | 23.62 | 0.991 | 6.02 | 22.49 |
| GJ 661 | 38.19 | 44.95 | 0.763 | 13.53 | 26.44 | 0.972 | 8.60 | 23.81 | 0.991 | 6.03 | 22.67 |
| Wolf 630 | 38.35 | 45.19 | 0.765 | 13.58 | 26.63 | 0.973 | 8.63 | 23.99 | 0.991 | 6.05 | 22.85 |
| GJ 625 | 38.72 | 45.76 | 0.769 | 13.68 | 27.08 | 0.974 | 8.68 | 24.44 | 0.992 | 6.09 | 23.30 |

Table 15: Coordinated time, proper time of flight and maximum $u / c$ for transfers to the selected 77 stars according to three acceleration levels. Computations have been performed assuming relativistic speed under constant thrust.

### 5.3 Exploration phase: orbits around binary systems

For the present case of in situ observations of stars near our Sun, the following privileged locations should be considered when designing the orbit:
a) libration points-and periodic orbits around them-within binary star systems (possibly formed by a star and a planetary companion);
b) (periodic) orbits around stars (and their planetary companions);
c) transfer orbits between any two of the previous sets.

A variety of dynamical acrobatics can be envisioned in relation to these locations. In particular, orbits, possibly of a periodic nature, can be designed around the libration points. Transfers can also be contemplated between the libration points and between orbits around the component bodies and the critical points. Scientific investigation goals will of course determine the desirability of simple or more complicated tours to be designed. Naturally, transfers requiring near null input energy are to be preferred and should be the main goal of the designer.

### 5.3.1 Lagrange points

The Circular Restricted Three-Body Problem (CR3BP hereinafter) describes the motion of a body with negligible mass under the gravitational influence of two massive bodies, called the primaries, which move in circular orbits about their barycentre. Let $(x, y, z)$ denote the position of the negligible-mass body in a rotating coordinate system with the origin at the barycentre where the $x$-axis points from the larger to the smaller primary, the $z$-axis points along the normal to the orbit plane of the primaries and the $y$-axis completes the right-handed orthogonal triad. The quantity $\mu$ represents the ratio of the mass of the smaller primary to the total mass. The units are chosen so that the distance between the primaries, the sum of the masses of the primaries and the angular velocity of the primaries are all equal to one. Therefore the larger and smaller primaries are located at $(-\mu, 0,0)$ and $(1-\mu, 0,0)$ respectively. The equations of motion for the CR3BP (see also Danby, 1962) are

$$
\begin{align*}
& \ddot{x}=2 \dot{y}+x-(1-\mu)(x+\mu) r_{1}^{-3}-\mu(x-1+\mu) r_{2}^{-3} \\
& \ddot{y}=-2 \dot{x}+y-(1-\mu) y r_{1}^{-3}-\mu y r_{2}^{-3}  \tag{10}\\
& \ddot{z}=-(1-\mu) z r_{1}^{-3}-\mu z r_{2}^{-3}
\end{align*}
$$

where $r_{1}$ and $r_{2}$ are the distances between the third body and the primaries:

$$
\begin{align*}
& r_{1}=\sqrt{(x+\mu)^{2}+y^{2}+z^{2}} \\
& r_{2}=\sqrt{(x-1+\mu)^{2}+y^{2}+z^{2}} \tag{11}
\end{align*}
$$

The well-known integral of motion (i.e., the Jacobi integral) associated to this dynamical system is

$$
\begin{equation*}
J=2 U(x, y, z)-\left(v_{x}^{2}+v_{y}{ }^{2}+v_{z}^{2}\right) \tag{12}
\end{equation*}
$$

where

$$
\begin{equation*}
U(x, y, z)=\frac{1}{2}\left(x^{2}+y^{2}\right)+\frac{1-\mu}{r_{1}}+\frac{\mu}{r_{2}} \tag{13}
\end{equation*}
$$

is the sum of the centrifugal and gravitational potential at the position of the massless body.
In the barycentric rotating reference system the $x$ coordinates of the three collinear equilibrium points $\left(\mathrm{L}_{1}\right.$, $L_{2}$ and $L_{3}$ ) are determined by solving the following fifth order equations:

$$
\begin{equation*}
u^{2}\left[\left(1-s_{1}\right)+3 u+3 u^{2}+u^{3}\right]=\mu\left[s_{0}+2 s_{0} u+\left(1+s_{0}-s_{1}\right) u^{2}+2 u^{3}+u^{4}\right] \tag{14}
\end{equation*}
$$

in which $u$ measures the distance from the second primary in normalized units (i.e., in units of the distance between the two primaries), $s_{0}=\operatorname{sign}(u)$ and $s_{1}=\operatorname{sign}(u+1):\left(s_{0}, s_{1}\right)$ are equal to $(-1,1),(1,1)$ and $(-1,-1)$, respectively for $\mathrm{L}_{1}, \mathrm{~L}_{2}$ and $\mathrm{L}_{3}$. (Cornish \& Goodman, lagrange.ps, document available at http://spiff.rit.edu/classes/phys440/lectures/lagrange/ ).
The positions of the two equilateral libration points $\mathrm{L}_{4}$ and $\mathrm{L}_{5}$ are:

$$
\begin{align*}
& L_{4}:\left(\frac{1-2 \mu}{2}, \frac{\sqrt{3}}{2}\right) \\
& L_{5}:\left(\frac{1-2 \mu}{2},-\frac{\sqrt{3}}{2}\right) \tag{15}
\end{align*}
$$

The 13 binary systems of Table 3 are almost all characterized by a large value of the orbital eccentricity. To such systems the CR3BP does not apply. The problem is better modelled as an Elliptical Restricted Three-Body Problem (ER3BP hereinafter). In the ER3BP the Lagrange critical points still exist, but instead of being fixed (in barycentric rotating coordinates), they pulsate with the distance between the two primaries.

We determined the positions of the five equilibrium points of systems composed by each pair of stars and a third massless body (the spacecraft) at the time when the distance $r$ between the primaries equals the semi-major axis $a$ and assuming zero eccentricity. We solved the fifth-order Lagrange equations (14) by an iterative technique starting from the initial guess $u_{0}$ suggested by Brouwer and Clemence (1961):

$$
\begin{array}{ll}
L_{1}: & u_{0}=-\alpha\left(1-\alpha / 3-\alpha^{2} / 9\right) \\
L_{2}: & u_{0}=\alpha\left(1+\alpha / 3-\alpha^{2} / 9\right)  \tag{16}\\
L_{3}: & u_{0}=\beta-2
\end{array}
$$

where $\alpha=\left[\frac{\mu}{3(1-\mu)}\right]^{1 / 3}, \beta=-v\left(1+\frac{23}{84} v^{2}\right)$ and $v=\frac{7}{12} \mu$. Results for the selected 13 binary systems are shown in barycentric rotating coordinates and physical units in the plots of Figure 27.
The non negligible eccentricity of all the systems (apart from GX Andromedae) causes the three collinear equilibrium points to pulsate along the $x$-axis around their mean values (i.e., those obtained for $r=$ a) with amplitude $\pm a e$; the two triangular points move both in the $x$ and $y$ directions according to the law:

$$
\begin{align*}
& L_{4}:\left(\frac{1-2 \mu}{2} r, \frac{\sqrt{3}}{2} r\right) \\
& L_{5}:\left(\frac{1-2 \mu}{2} r,-\frac{\sqrt{3}}{2} r\right) \tag{17}
\end{align*}
$$

where again $a(1-e) \leq r \leq a(1+e)$ as a function of time.



Lagrange points of Sirius






Lagrange points of EQ Pegasi


Figure 27: The 13 selected binary systems with their Lagrange points, computed by solving the Lagrange quintic equation under the assumption of zero eccentricity and relative distance between the stars equal to the observed semi-major axis. The plots are drawn in physical units relative to the barycentric rotating reference frame.

Figure 28 shows the orbits of the Lagrangian points for the Alpha Cen A/B system $(e=0.5179)$ as viewed in an inertial reference frame. All critical points follow elliptical orbits whose foci coincide with the center of mass of the system.


Figure 28: The elliptical paths followed by the Lagrangian points of the Alpha Cen $A / B$ system viewed from an inertial reference frame (two snapshots are shown for true anomalies of $0^{\circ}$ and $150^{\circ}$ ).

### 5.3.2 Computation of periodic orbits using AUTO2000

AUTO2000 is a software tool for continuation and bifurcation problems in ordinary differential equations developed by R. Paffenroth, E. Doedel and collaborators (Dichmann, Doedel \& Paffenroth, 2002; Paffenroth, 2002). The software is free and publicly available from http://auto2000.sourceforge.net/. The problems that may be addressed by numerical continuation methods are those which can be solved as a parameter-dependent system of nonlinear equations. The algorithm starts from a known solution at given parameter values; then a solution is computed at a nearby set of parameter values to generate an initial guess to feed an iterative scheme to compute the solution at a new set of parameter values. Therefore a parameter continuation algorithm can be described as a numerical implementation of a homotopy between solutions of different problems.

Driven by suitable user-defined scripts, AUTO2000 computes families of periodic solutions of conservative systems. In particular, specific scripts, prepared and distributed by the authors, allow to obtain several families of periodic solutions emanating from the libration points.
AUTO2000 uses numerical continuation methods to explore families of three-dimensional periodic solutions of this system that emanate from any of the five libration points. This is done by rewriting Eq. (10) as a six-dimensional first-order system, adding boundary conditions to impose unit periodicity of the solutions and introducing the period $T$ of the orbit as an unknown to be solved for as part of the numerical procedure; finally, a so-called unfolding parameter $\lambda$ is added and treated as an unknown. The resulting system of differential equations is

$$
\begin{align*}
& \dot{x}=T v_{x}+\lambda \frac{\partial J}{\partial x} \\
& \dot{y}=T v_{y}+\lambda \frac{\partial J}{\partial y} \\
& \dot{z}=T v_{z}+\lambda \frac{\partial J}{\partial z} \\
& \dot{v}_{x}=T\left[2 v_{y}+x-(1-\mu)(x+\mu) r_{1}^{-3}-\mu(x-1+\mu) r_{2}^{-3}+\lambda \frac{\partial J}{\partial v_{x}}\right]  \tag{18}\\
& \dot{v}_{y}=T\left[-2 v_{x}+y-(1-\mu) y r_{1}^{-3}-\mu y r_{2}^{-3}+\lambda \frac{\partial J}{\partial v_{y}}\right] \\
& \dot{v}_{z}=T\left[-(1-\mu) z r_{1}^{-3}-\mu z r_{2}^{-3}+\lambda \frac{\partial J}{\partial v_{z}}\right]
\end{align*}
$$

with the following boundary conditions:

$$
\begin{array}{lll}
x(1)=x(0), & y(1)=y(0), & z(1)=z(0) \\
v_{x}(1)=v_{x}(0), & \mathrm{v}_{y}(1)=v_{y}(0), & \mathrm{v}_{z}(1)=v_{z}(0) \tag{19}
\end{array}
$$

### 5.3.3 The case of GX Andromedae $(e=0)$

The binary system made up by the two stars GX and GQ Andromedae is characterized by zero orbital eccentricity and therefore is suitable for computation of the periodic orbits in the CR3BP with AUTO2000.

For this mass ratio ( $\mu=0.25116$ ) AUTO2000 has generated about 15,000 orbits emanating from the three collinear equilibrium positions $\left(L_{1}, L_{2}, L_{3}\right)$ : each orbit is represented by 201 points and for each point 7 quantities are output (time, 3 position coordinates, 3 velocity components); then, for each orbit the period and the Jacobi integral are also given. The amount of data is huge and therefore difficult to handle. Figure 29, Figure 30 and Figure 31 illustrate a selection (roughly 4\%) of the periodic orbits obtained.
The periods of the orbits thus obtained are always a non-negligible fraction of the system's period, equal to 2,200 years; therefore, it would take a very long time to follow the full revolution of any of the periodic orbits associated with the libration points of this system. We regard this as a test case for the exploration of a type of low-cost trajectories within a binary system.
In practice, the revolution period of the primaries is probably long enough to allow application of the Two-Fixed Centers paradigm.

GX Andromedae: periodic orbits emanating from L1


GX Andromedae: periodic orbits emanating from L1


Figure 29: Two sets of periodic orbits emanating from $L_{1}$ in barycentric rotating coordinates and physical units. The most meaningful projection of the displayed orbits is shown in grey.


GX andromedae: periodic orbits emanating from L2


Figure 30: Two sets of periodic orbits emanating from $\mathrm{L}_{2}$ in barycentric rotating coordinates and physical units. The most meaningful projection of the displayed orbits is shown in grey.

GX Andromedae: periodic orbits emanating from L3


GX Andromedae: periodic orbits emanating from L3


Figure 31: Two sets of periodic orbits emanating from $L_{3}$ in barycentric rotating coordinates and physical units. The most meaningful projection of the displayed orbits is shown in grey.

We made a preliminary investigation on the possibility of exploiting this category of natural trajectories in the CR3BP to accomplish low-cost transfers from the first primary to the second primary by travelling through some Lagrange point of the system (most noticeably $\mathrm{L}_{1}$, which could ensure minimum energy transfers). We selected the periodic orbits by imposing position constraints (maximum distance from $\mathrm{L}_{1}$, inner and outer radius of a ring of circular orbits around $m_{1}$, inner and outer radius of a ring of circular orbits around $m_{2}$ ) and a position tolerance for the intersections. The intersections thus obtained have been graded according to the magnitude of the velocity differences (maneuvres) between the intersecting orbits, the lowest grade being assigned to the most expensive maneuvres. We investigated various sets of constraints and we ended up with two low-cost transfer strategies, shown in Figure 32 and Figure 33.
The first (case A) illustrates 2 solutions, each involving 2 maneuvres, that take the spacecraft from the region around $m_{1}$ to the region around $m_{2}$ through 3 periodic orbits of the system; the total cost of the transfer is $4.12 \mathrm{~km} / \mathrm{s}$ and $3.06 \mathrm{~km} / \mathrm{s}$ respectively.
Case B shows the transfer from a circular orbit around $m_{1}$ (13 AU radius) to a circular orbit around $m_{2}$ (24 AU radius) through three branches of periodic orbits (the total cost of the maneuvre is $3.27 \mathrm{~km} / \mathrm{s}$ ).

The selection constraints that characterize each strategy are reported in the legends of the two plots.

## GX Andromedae: intersections among periodic orbits through $L_{1}$ (case $A$ )



Figure 32: Planar intersecting periodic orbits (black curves) and their intersection points (cyan dots, the intersection tolerance $\varepsilon$ equals 1 AU ) in the GX Andromedae binary system represented in physical units in the barycentric rotating reference frame. Also shown are the positions of the 5 equilibrium points and the two stars $\left(m_{1}\right.$ and $\left.m_{2}\right)$. Four orbits are coloured in magenta, blue, orange and green, indicating one orbit through $m_{1}$ (magenta), two orbits through $L_{1}$ (orange and blue) and one orbit through $m_{2}$ (green) respectively. These intersecting orbits satisfy the position selection criteria described in the legend, namely: the orbits through either of the two stars cross a ring of 1 AU internal radius and 5 AU external radius around the corresponding primary; the orbits through $L_{1}$ pass within 5 $A U$ from $L_{1}$. A trajectory from the region around $m_{1}$ to the region around $m_{2}$ through the 1-2-4 chain requires two maneuvres of 0.79 and $3.33 \mathrm{~km} / \mathrm{s}$ (total $\Delta \mathrm{V}=4.12 \mathrm{~km} / \mathrm{s}$ ); a trajectory of the same kind through the 1-3-4 connection costs $(2.82+0.24) \mathrm{km} / \mathrm{s}=3.06 \mathrm{~km} / \mathrm{s}$. The lower part of the legend provides the orbital periods of the four orbits in units of the binary system's orbital period and the values of the Jacobi integral.


Figure 33: Planar intersecting periodic orbits (black curves) (the intersection tolerance $\varepsilon$ equals 1.5 AU ) in the GX Andromedae binary system represented in physical units in the barycentric rotating reference frame. Also shown are the positions of the 5 equilibrium points and the two stars ( $m_{1}$ and $m_{2}$ ). Three orbits are coloured in magenta, blue and orange, indicating one orbit through $m_{1}$ (magenta), one orbit through $L_{1}$ (blue) and one orbit through $m_{2}$ (orange) respectively. These intersecting orbits satisfy the position selection criteria described in the legend, namely: the orbits through either of the two stars cross a ring of 3 AU internal radius and 25 AU external radius around the corresponding primary; the orbits through $L_{1}$ pass within 5 AU from $L_{1}$. A trajectory from a circular orbit around $m_{1}$ (cyan circle) to a circular orbit around $m_{2}$ (cyan circle) through the C-1-2-3-C chain requires four maneuvres; the total $\Delta \mathrm{V}$ is $3.27 \mathrm{~km} / \mathrm{s}$. The lower part of the legend provides the orbital periods of the three selected orbits in units of the binary system's orbital period and the values of the Jacobi integral.
Other transfer cases can also be contemplated, for instance between two Lagrangian points. Orbits of this type have been investigated in (Gómez \& Masdemont, 2000).

### 5.3.4 Binary systems with eccentric orbits

The remaining binary systems of our sample are characterized by large orbital eccentricities (between 0.2 and 0.6). In these situations the CR3BP paradigm can only be applied over small fractions of the system's orbital period (Szebehely, 1967). Since the orbits that AUTO2000 computes occupy a significant fraction of the system's orbital period, their use as branches of natural transfers is severely limited in the elliptic case.

The most appropriate framework for studying transfers within elliptic systems is the already mentioned Elliptic Restricted Three-Body Problem (ER3BP). The subject is much less investigated, as indicated by the smaller amount of dedicated papers. The main difference with the circular problem is that the dynamical system is non-autonomous (the Jacobi integral is missing). Then the equations of motion of the third body are coupled with the differential equations describing the pulsation of the distance between the primaries and the independent variable is usually taken to be the true anomaly rather than the time.

Finally, the problem contains two parameters - the eccentricity $e$ and the mass ratio $\mu$ of the primaries in contrast to the single-parameter $\mu$ of the circular problem. The extra parameter $e$ adds one degree of freedom to the problem of finding periodic orbits. For given $e$ and $\mu$, only isolated periodic orbits (symmetric with respect to the $x$-axis) possibly exist in the elliptic problem because the periodicity criterion imposes that the $x$-axis crossing occurs when the two primaries are at an apse, thus leading to periods which are necessarily integer (hence discrete) multiples of the systems's orbital period (Broucke, 1972).

The computation of periodic orbits emanating from the equilibrium points of the ER3BP with AUTO2000 is not straightforward. Alternative techniques (like that adopted by Broucke (1972): numerical integration with recurrent power series) require nontrivial software development. Some examples of symmetric periodic orbits belonging to a mass-ratio of $\mu=0.5$ and to various eccentricity levels as obtained by Broucke (1972) are illustrated in Figure 34.


Figure 34: Some examples of symmetric periodic orbits belonging to a mass-ratio of $\mu=0.5$ and to various eccentricity levels (Broucke, 1972).

Benest (1988) made extensive numerical simulations within the frame of the ER3BP in order to search if stable orbits exist for planets around one of the two components in binary stars. In particular, he showed some results for the Alpha Centauri A/B system (Figure 35 and Figure 36). The existence of such stable orbits could be also exploited to place a spacecraft in orbit around one of the two stars.


Figure 35: A nearby planetary orbit around Alpha Cen B, represented during one revolution of the binary; A: fixed axes with origin in the binary's barycentre, where the little and large ellipses are the orbits of Alpha Cen $A$ and $B$; $B$ : rotating frame with origin in Alpha Cen B. (Benest, 1988)


Figure 36: A remote planetary orbit around Alpha Cen A, represented during 5 revolutions of the binary; same notations as for the previous figure, same frame as for Figure 35 B.

### 5.4 Exploration phase: orbits within triple systems

The following privileged locations should be considered when designing a spacecraft trajectory for in-situ observation of triple systems:
a) trajectories connecting libration points of individual CR3BP or ER3BP-depending on the eccentricity values - known as Weak Stability Boundary transfers (WSB);
b) orbits around one of the component stars (or planetary companion);
c) transfers between solutions of the two types.

### 5.4.1 Weak Stability Boundary (WSB) transfers

In recent years a new impulse has been given to the design of interplanetary trajectories by the discovery of the so-called "Interplanetary Superhighway System" (IPS) (Lo \& Ross, 2001), a system of natural routes that pervade interplanetary space and that can be exploited to accomplish transfers from one planet to another or to one of its moons at low cost. The idea has been already successfully applied to the lunar transfer of the Japanese spacecraft Hiten (1991) thanks to the design and optimization work performed by Miller \& Belbruno (1991).

The dynamics of this class of trajectories (also called Weak Stability Boundary (WSB) transfers) has been well explained in the works by Koon et al. (2001) and by Circi \& Teofilatto (2001): in principle, the transfer from the Earth to the Moon takes place in the framework of the Sun-Earth-Moon-Spacecraft 4Body Problem, but can be explained on the basis of two coupled Circular Restricted Three-Body Problems (i.e., Sun-Earth-Spacecraft and Earth-Moon-Spacecraft). Within each CR3BP system invariant manifold structures (surfaces of constant energy in phase space) are associated with each libration point. In particular the $\mathrm{L}_{1}, \mathrm{~L}_{2}$ and $\mathrm{L}_{3}$ libration points are each characterized by one stable and one unstable manifold, respectively leading to, and originating from the periodic Lyapunov orbit (Koon et al., 2001).
Weak Stability Boundary transfers to the Moon exploit the existence of intersections in space and time between invariant manifolds of the two CR3BP problems, allowing the design of low-cost trajectories through the region of the Earth's $\mathrm{L}_{1}$ and the region of the lunar $\mathrm{L}_{2}$. Considerable fuel savings (up to 200 $\mathrm{m} / \mathrm{s}$ ) with respect to the classical Hohmann or bielliptic transfers can be obtained with lunar transfer trajectories of this new type because the energy levels of the Earth's $L_{1}$ and $L_{2}$ differ by little from the energy levels of the lunar counterparts. The price is a longer time of flight: 60-100 days vs. 6-7 days of Hohmann trajectories (Circi \& Teofilatto, 2001; Miller \& Belbruno, 1991).


Figure 37: (a) The plane of the Earth's orbit in Sun-Earth synodic coordinates showing the stable and unstable manifolds respectively around $L_{1}$ and $L_{2}$ and the corresponding halo orbits; the forbidden region cannot be reached with the energy pertaining to the halo orbits. (b) A Poincarè cut passing through Earth in the y-direction: switching from one manifold to another is possible at their intersections.

Further studies have shown that WSB transfers can be found leading to other destinations within our planetary system: to Mars, to the outer planets, to transfers between Jupiter and Saturn. "Petit Grand Tour" (Lo, 2001) is the name given by Martin Lo and collaborators to a system of itineraries that serially tour the satellite system of any planet, to capture into orbit, depart or land onto the various satellites. An example is the transfer from Ganymede to capture around Europa. The trajectory of the Genesis spacecraft, launched in 2001, has used this kind of strategy (Howell et al., 1997) to reach a halo orbit around the Sun-Earth libration point $\mathrm{L}_{1}$ (Figure 37).
Furthermore, the IPS may constitute a new tool to understand many aspects of the dynamical behaviour of the Solar System (Lo \& Ross, 2001): resonance properties of WSB transfers have interesting applications to the motions of Kuiper Belt objects outside the orbit of Neptune. Other studies have shown that comets closely follow IPS paths and, in particular, the temporary capture phenomenon of Jupiter comets seems to be controlled by Jupiter's IPS generated by its Lagrange points. The IPS may also play an important role in the control of the motions of the Asteroid Belt, the Kuiper Belt, the planetary rings and the zodiacal dust tori.

In principle, using one of the periodic orbits computed by AUTO2000 as starting point, the invariant manifolds associated to the corresponding equilibrium position could be found by applying small variations in phase space (position, velocity) to it and by numerically integrating backward and forward in time from the resulting initial conditions. Then, intersections in phase space between invariant manifolds connecting different boundary regions could be searched for and their characteristics investigated with an aim at designing low-cost transfer trajectories.

### 5.4.2 Are WSB transfers applicable to star systems in the Solar Neighbourhood?

In Section 4 we have presented and discussed the available information on the orbital characteristics of the closest known triple systems of our dataset, namely EZ Aquarii and Epsilon Indi ${ }^{4}$. The list could be extended to include the two known cases of planetary systems (Epsilon Eridani and Gliese 876), since they are both made up of three objects each. The question of the applicability of the WSB orbit design technique to these systems must take into account that their orbits are highly eccentric, while the present WSB paradigm has only been applied to coupled Circular R3B problems.
It is not clear that this technique is adequate to the cases at hand. It is likely that it must be properly extended to the Elliptic R3BP along lines which are yet to be identified.

## 6 CONCLUSIONS AND IDEAS FOR FUTURE WORK

The investigations performed in this study have clarified a number of issues pertaining to the dynamics of the stars in the Solar Neighbourhood and the design of the trajectories to first reach them and then tour their environs. We have seen that

1. The stars behave as non-interacting particles, subject only to the force exerted by the Galaxy as a whole. We have verified this by direct numerical integration of the motion of an ensemble of stars subject only to their mutual gravitational interactions and then subject only to the galactic potential. Over several thousand years (a small fraction of the galactic rotation period which at solar position is about 250 My ) their trajectories are effectively identical and with respect to the Sun can be modeled as straight-line orbits.

[^3]2. The configuration of stars currently constituting the Solar Neighbourhood is bound to disrupt, not being gravitationally bound as a subsystem. Therefore, the picture of the Solar Neighbourhood changes completely over timescales much shorter than the Sun's galactic rotation period.
3. Intersections among stellar spheres of influence are extremely rare events and do not imply that stars that happen to be close to one another are gravitationally bound. As an example, the available measurements suggest that the long-debated relationship between Proxima Centauri and Alpha Centauri $\mathrm{A} / \mathrm{B}$ is nothing but a hyperbolic passage of the former in the gravitational field of the latter.
4. An exploration probe interacts with the stars only when it enters their spheres of influence, allowing to conclude that the known dynamical paradigms like the Circular Restricted Three-Body Problem (CR3BP) or the Two Fixed Centers (TFC) do not apply to the cruise phase of interstellar flight: this implies that no critical points exist between nearby stars.
5. The absence of interactions between nearby stars and between either star and a probe travelling between them has two important consequences: a) that by properly imparting velocity impulses, a spacecraft can be stably positioned anywhere outside the spheres of influence of these stars, and b) that travel between the stars can occur on rectilinear orbits.
6. Limiting the time of flight of the transfer journey to the scale of human lifetime requires high speeds and these, in turn, require high energy propulsion, most likely by means of continuous thrust: under a constant acceleration of $0.5 \mathrm{~m} / \mathrm{s}^{2}$ it takes 18.4 years of (terrestrial) coordinated time (or 17.8 years of proper time) to arrive at Proxima Centauri with a rocket reaching relativistic speeds of the order of $0.4 c$; adding the 4.3 years necessary for the data to be transmitted back to Earth gives a total mission duration of less than 23 years. As noted above, the transfer trajectory is a rectilinear orbit.
7. Our knowledge of the internal dynamics of the stellar systems that populate the Solar Neighbourhood remains incomplete, as demonstrated by the large uncertainties often affecting the determination of many astrometric and physical parameters. This is especially important when trying to identify the dynamical evironment that an interstellar exploration probe will find when reaching the destination star system.
8. The exploration phase can be separately addressed for single, binary and triple systems.

8a. In the case of a single star the only option is to put the spacecraft into an orbit around the star. While on the transfer orbit, the star could also be observed, so there appears to be no need to stop in the far distance before proceeding to the rendez-vous, which could be energetically demanding. It is also possible to perform a flyby of the star while on route to another target.

8b. Binary systems offer several options: orbits around the consituent stars, orbits around the Lagrangian points, transfer orbits between these. For the case of binaries in circular relative orbits the problem can be addressed drawing from a large knowledge base which includes the design of periodic orbits (also by continuation methods) and of transfer orbits between critical points. We made a preliminary design of low-cost ( $\Delta \mathrm{V} \approx 3 \mathrm{~km} / \mathrm{s}$ ) transfers between circular orbits around the two primaries of the GX Andromedae system following branches of periodic orbits connecting through the (intermediate) Lagrangian point $\mathrm{L}_{1}$. The more general and ubiquitous case of non-zero eccentricity requires further development under the Elliptic Restricted Three-Body Problem.

8c. Triple systems are characterized by highly eccentric orbits and, except for periodic orbits around each of the bodies, other options remain unexplored due to the unavailability of applicable dynamical paradigms.
The analysis carried out within this study has also identified a number of items that deserve further investigation from the viewpoint of trajectory design:

- Solar System escape strategy including attainment of relativistic speed with special regard to the acceleration phase (relationship between proper and coordinated time);
- Verification by simulation of attainability of generic positions (considered wither as final targets of more likely as intermediate stops of longer missions) outside stellar spheres of influence and associated energy consumption;
- In-depth study of the Elliptical Restricted Three-Body Problem in connection with the identification of transfer orbit design between its pulsating critical points. In this respect, new software tools need to be developed due to the inadequacy of those currently, freely available.


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[^0]:    ${ }^{1}$ The Sixth Orbit Catalog of Visual Binaries lists orbital parameters of binary stars according to their HIP index. The relation with indices of other catalogues is also provided but the link to the Gliese Catalogue (of which RECONS adopts the numbering) does not appear. Therefore the identification of the binary systems which appear in our database depends on the existence (and availability) of a correspondence between HIP and Gliese numbers.

[^1]:    ${ }^{2}$ Roy (1972) defines "close encounters" those which cause a deflection larger than 90 degrees to the initial direction of motion of the two stars. By introducing average values for the star density and peculiar velocity in the Galaxy of $10^{-1}$ stars per cubic parsec and $20 \mathrm{~km} / \mathrm{s}$, he finds that the average time interval between encounters of this type is $3 \cdot 10^{14}$ years, 4 orders of magnitude larger than the age of the Galaxy.

[^2]:    ${ }^{3}$ The plots drawn at the boundaries of the region occupied by the N stars (i.e., at $\mathrm{z}= \pm 7.0 \mathrm{pc}$ ) do not exhibit peaks but a very low continuum as if there were no stars. This is a selection effect because the stars outside the volume are excluded from the computations while the effect of stars within the region gets weaker and weaker.

[^3]:    ${ }^{4}$ Following the discussion made in Section 4.1, we prefer to treat Alpha Centauri as a double star experiencing a hyperbolic encounter with Proxima Centauri.

