

THANK YOU

Nachum Dershowitz



Dziękuję

Nachum Dershowitz





*I want to  
thank you  
folks*

JASMINE

PC

WDE

Inc.

23





*I want to  
thank you  
folks*

JASMINE



WDE

Inc.

23

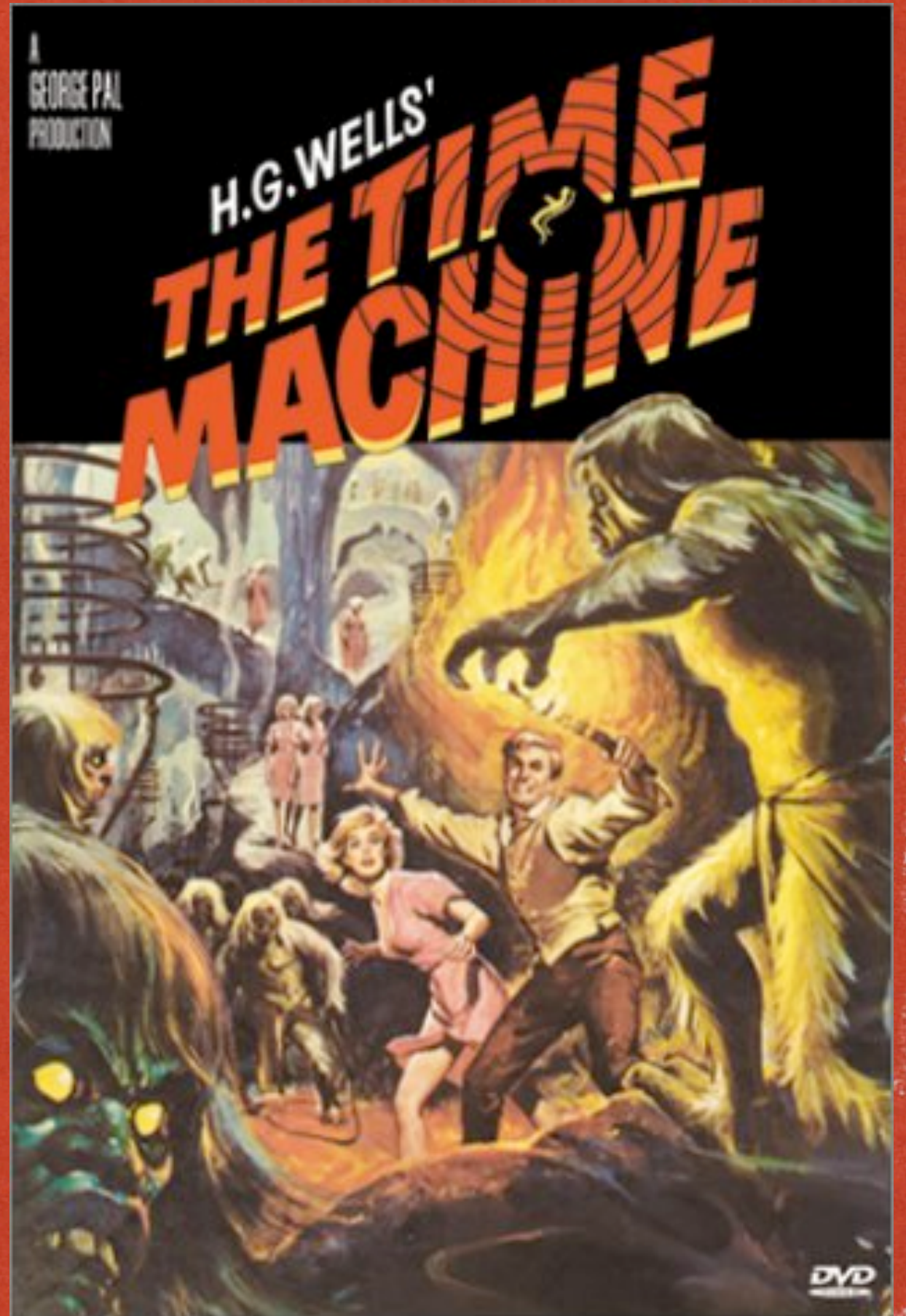


# Shakespeare

- I can no other answer make but thanks/  
And thanks...
- What's to do? Shall we go see the reliques  
of this town?
- To-morrow, sir: best first go see your  
lodging.
- I am not weary, and 'tis long to night: I  
pray you, let us satisfy our eyes/  
With the memorials and the things of fame/  
That do renown this city.



# History

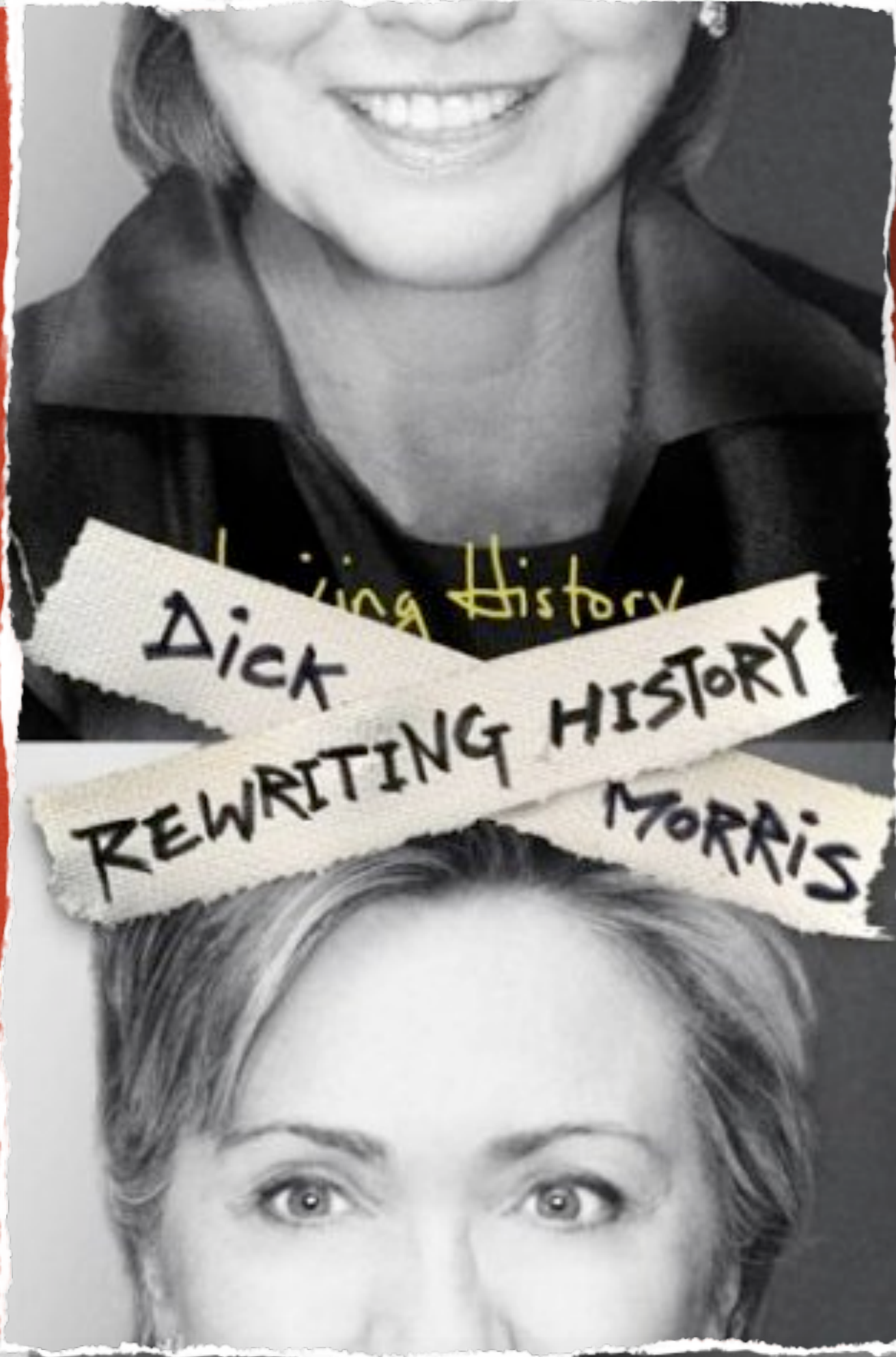




# Histories

- Martin Davis
- Wolfgang Bibel
- Peter Andrews
- Ewing Lusk
- ...





Writing History  
Dick  
REWRITING HISTORY  
MORRIS





# GOALS



# Agenda

- Much have I learned from my teachers,
- more so from my colleagues,
- but most of all from my students.

- Talmud



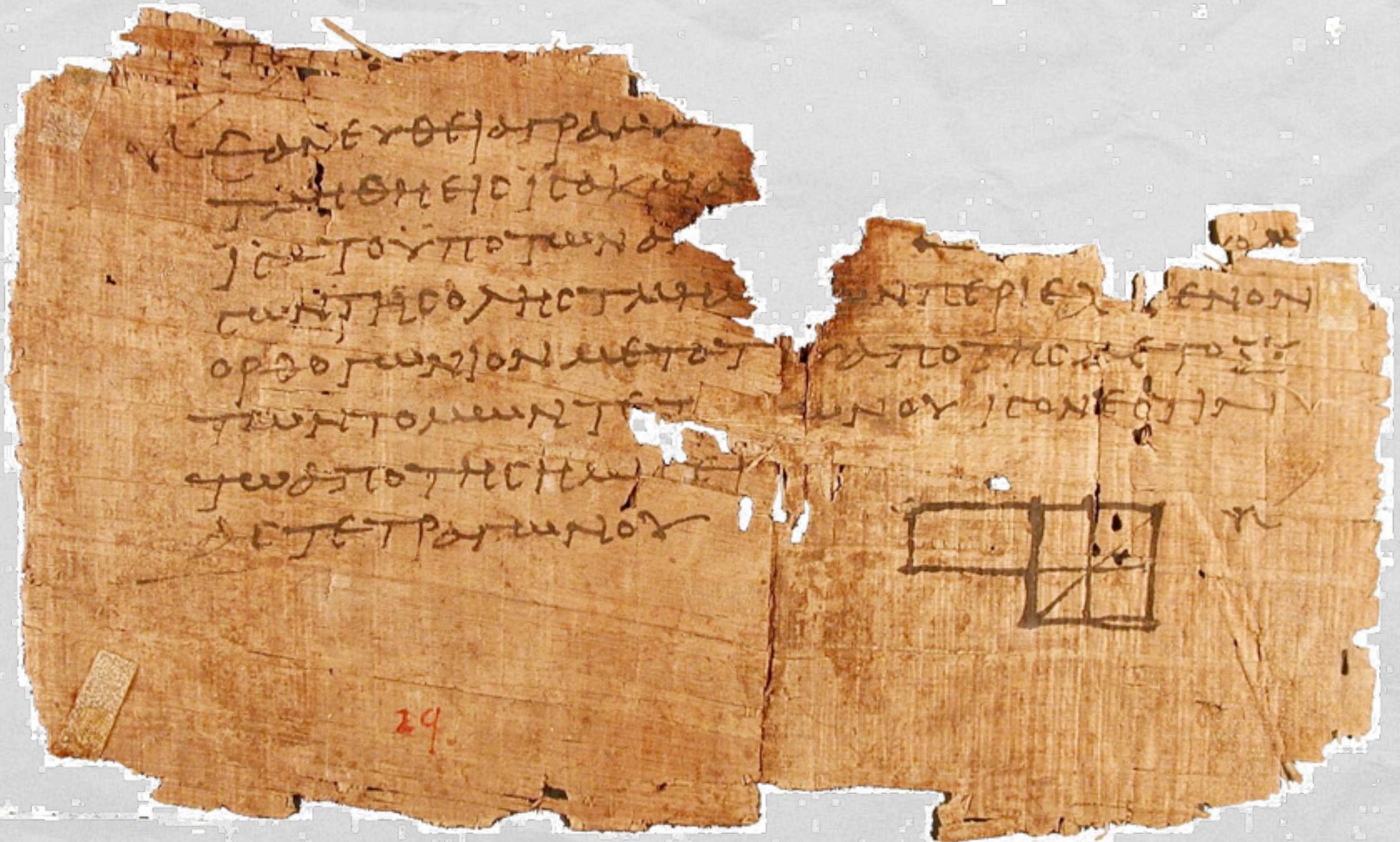
My Teachers



Natural Deduction



# Euclid (-400)



29

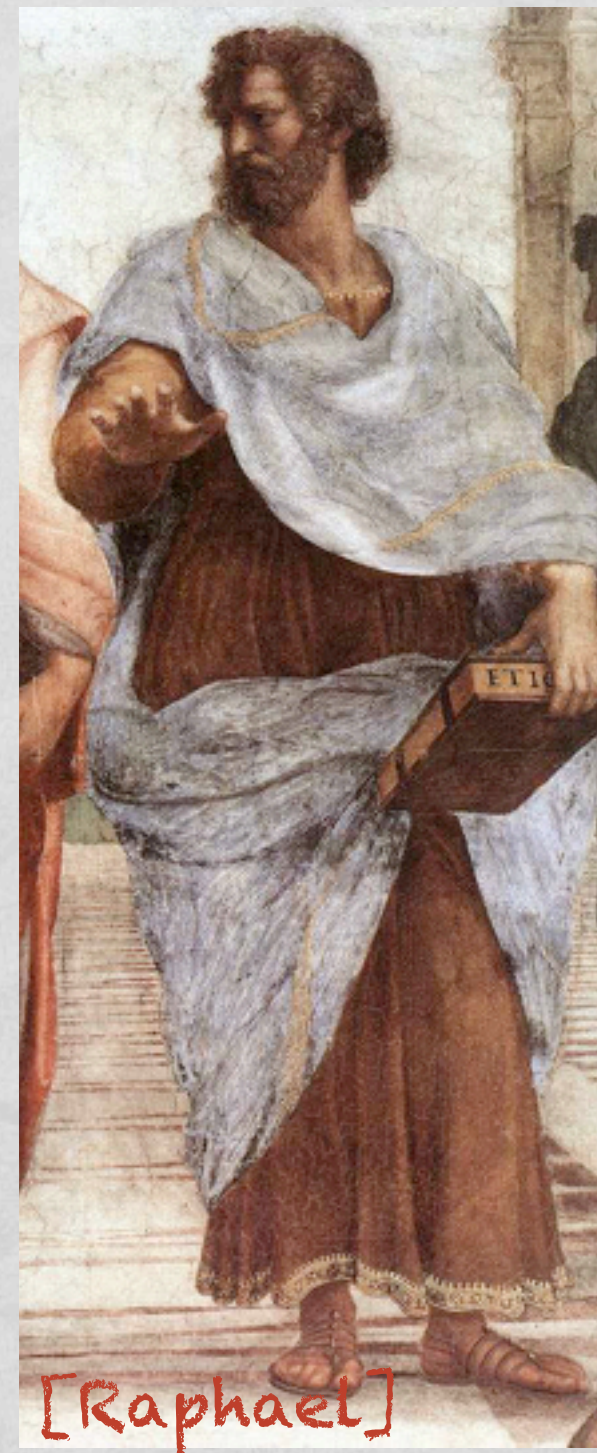


# Aristotle (-350)

PENGUINS ARE BLACK AND WHITE.  
SOME OLD TV SHOWS ARE BLACK AND WHITE.  
THEREFORE, SOME PENGUINS ARE OLD TV SHOWS.



**Logic: another thing that  
penguins aren't very good at.**



[Raphael]



Human Deduction



# Zeroth-Order Logic





# First-Order Logic

"Everybody Loves My  
Baby  
(But My Baby Loves  
Nobody But Me)"

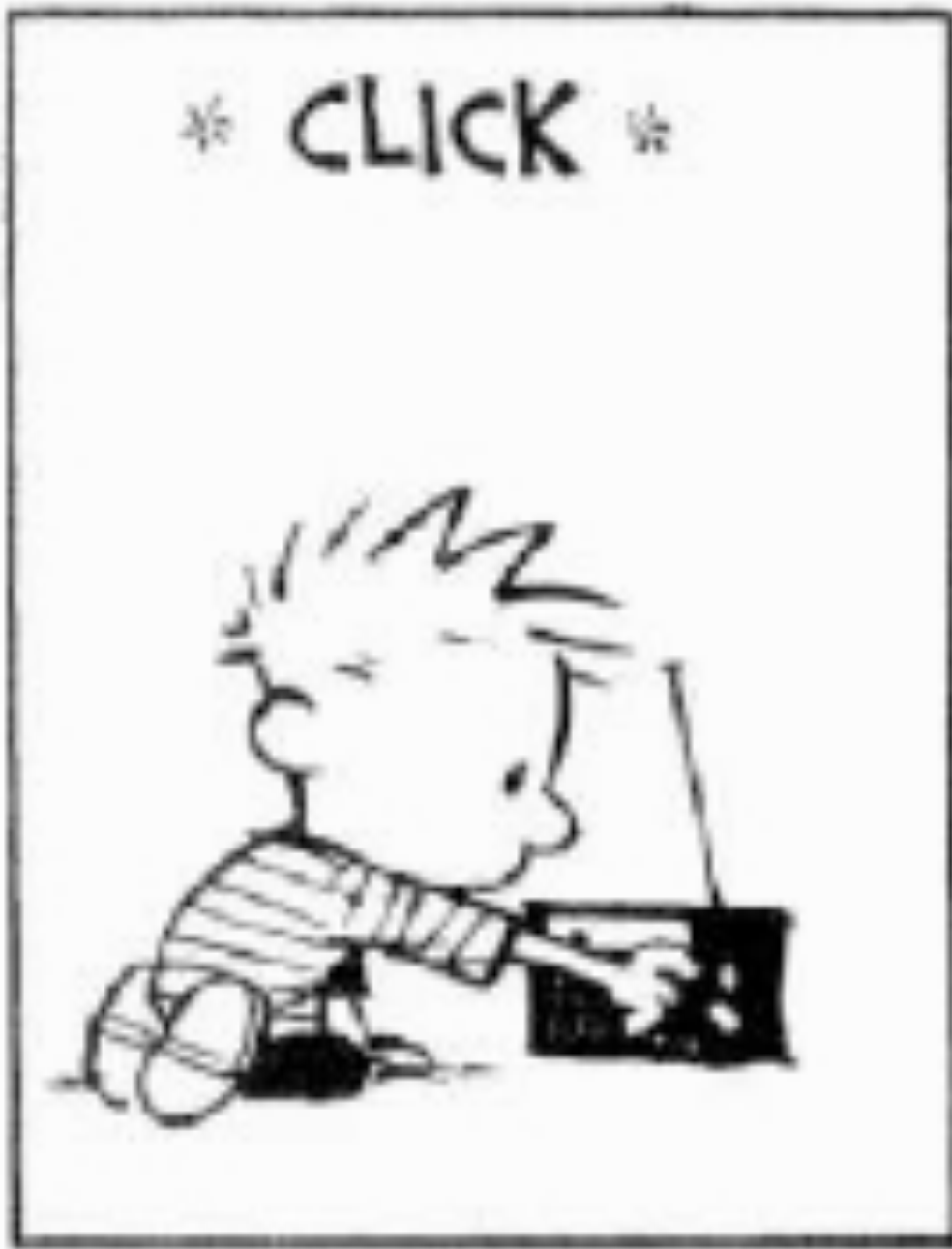
-- Jack Palmer  
& Spence Williams,  
1924







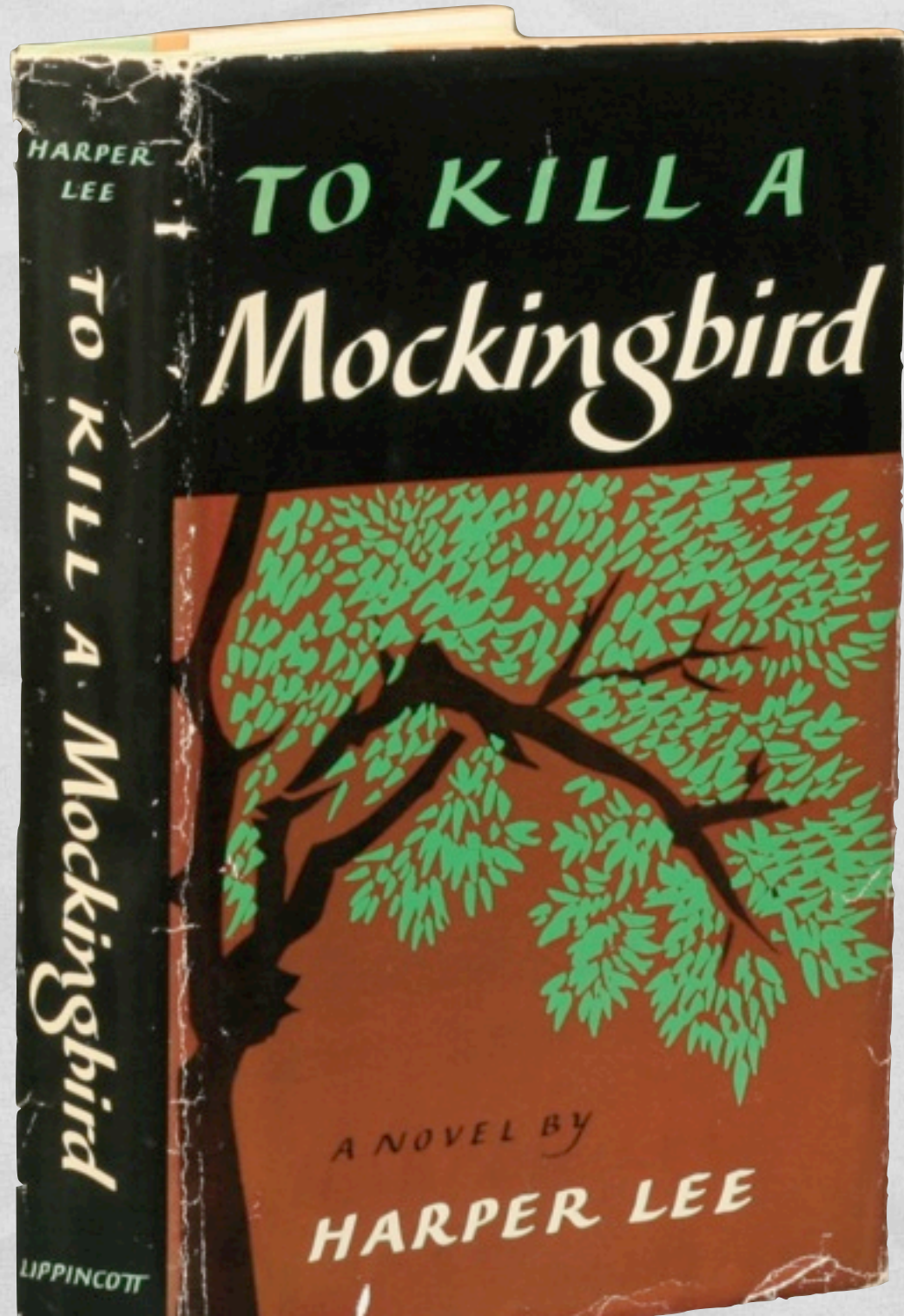




MSM

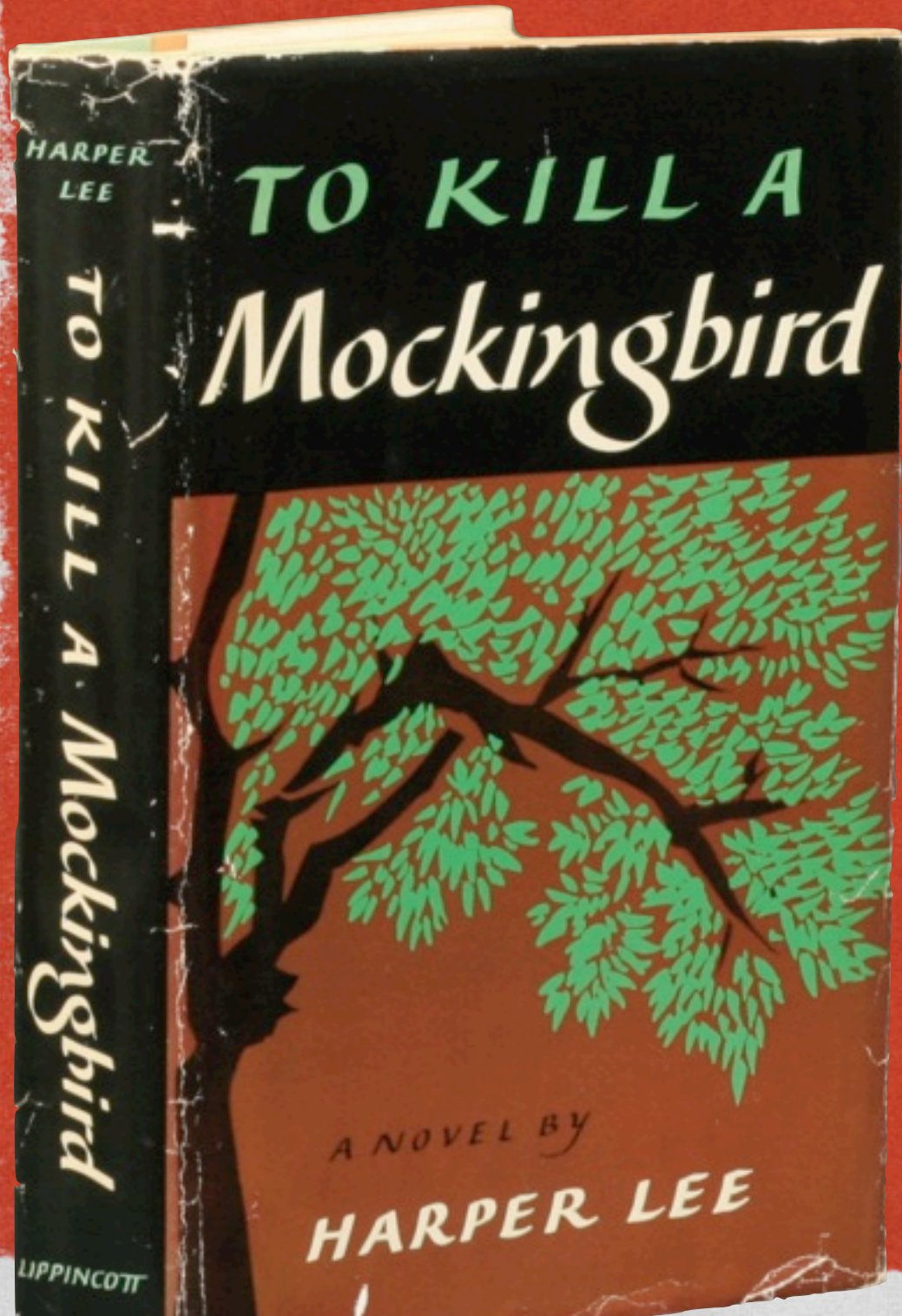


# Higher Logic



There is no man  
living who has  
never looked  
upon a woman  
without desire.





There is no man  
living who has  
never looked  
upon a woman  
without desire.



Robert Lowth  
1762

abolished double negatives in English  
as "illogical"



# BEYONCÉ

*BEST THING I NEVER HAD*



You turned  
out to be  
the best  
thing I  
never had.

And I will  
always be  
the best  
thing you  
never had.



Polish:

Nikogo nie widzialem  
(I didn't see nobody)

Serbian:

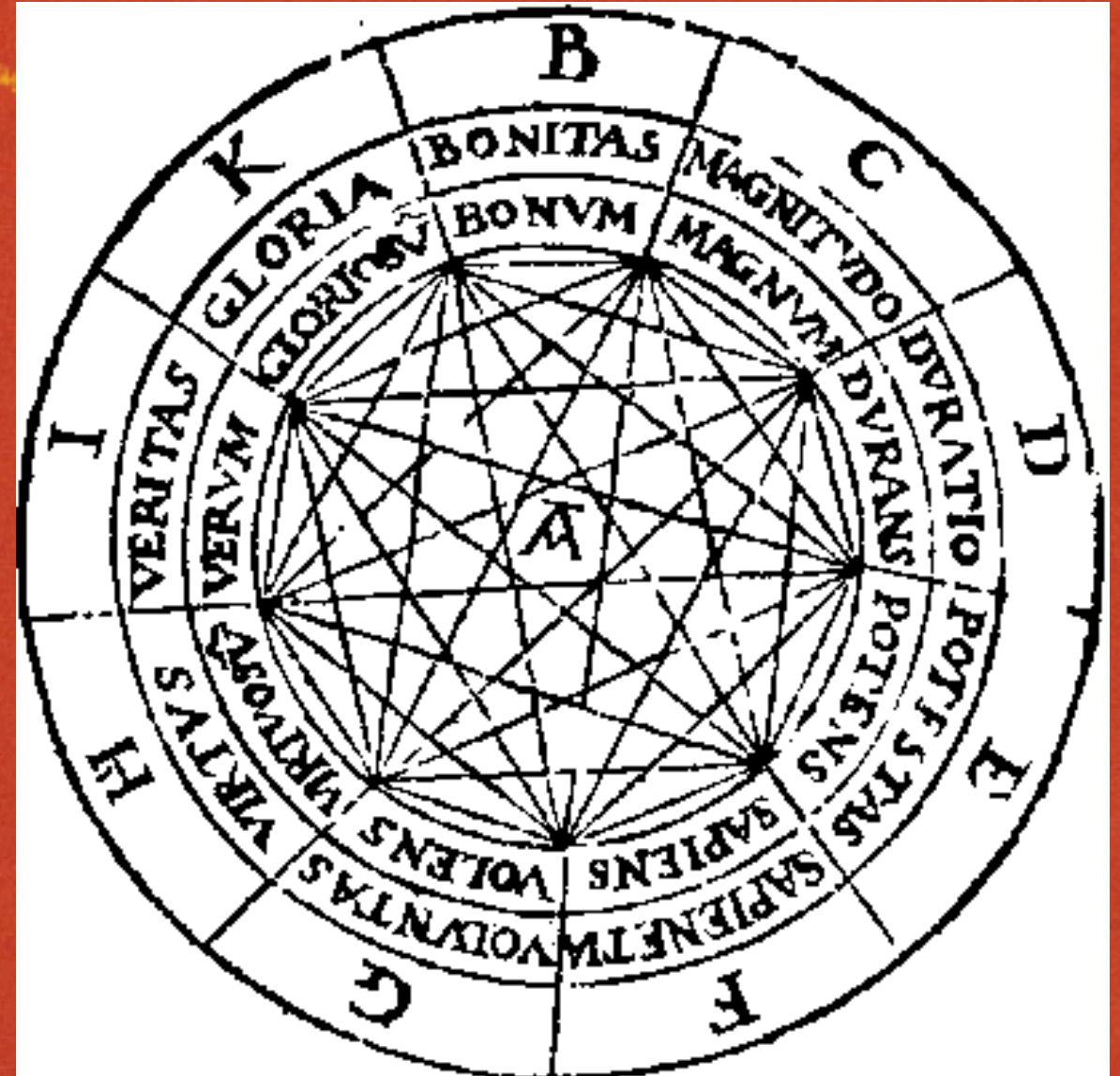
Niko nikada nigde ništa nije uradio  
(Nobody never didn't do nothing nowhere)



# Automated Deduction



# Ramon Lull (1274)



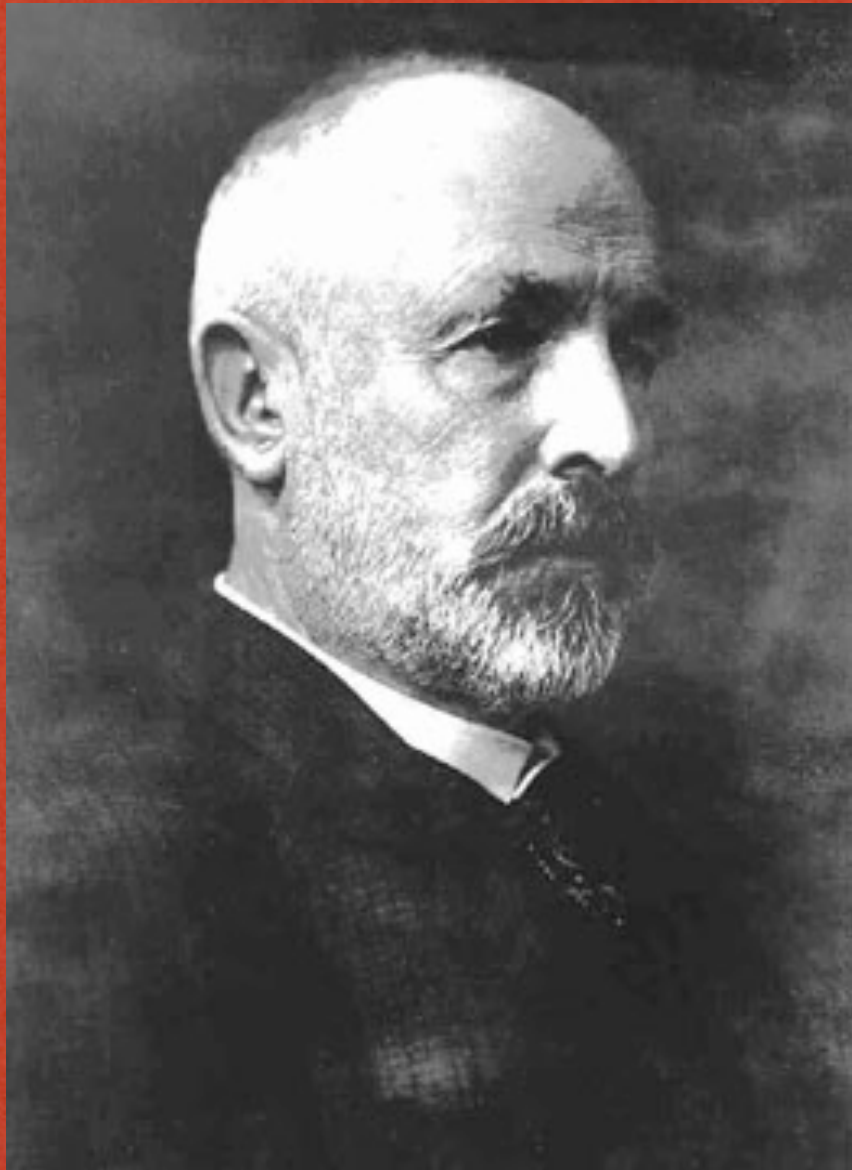
Raymondus Lullus  
Ars Magna et Ultima



# Georg Ferdinand Ludwig

## Philipp Cantor

on Lull



Eine Gemenge von  
Logik, kabbalistischer  
und eigener Tollheit,  
unter welches, man  
weiss nicht wie einige  
Körner gesunden  
Menschenverstandes  
geraten sind.



# Gottfried Wilhelm Leibniz (1666)



The only way to rectify our reasonings is to make them as tangible as those of the Mathematician, so that we can find our error at a glance, and when there are disputes among persons, we can simply say: Let us calculate, without further ado, in order to see who is right.



# Ada Lovelace



Many persons ... imagine  
that because [Babbage's  
Analytical Engine]

give[s] its results in numerical  
notation, the nature of its processes  
must ... be arithmetical and numerical  
rather than algebraical and analytical.

This is an error!



# David Hilbert's Entscheidungsproblem

#2. Provide an effective method to determine whether a formula is valid.





# David Hilbert's "Lost" Problem

#24. Criteria of  
simplicity, or  
proof of the  
greatest  
simplicity of  
certain proofs.





# Jules Henri Poincaré



We might imagine a machine where we should put in axioms at one end and take out theorems at the other, like that legendary machine in Chicago where pigs go in alive and come out transformed into hams and sausages.





Jacques Herbrand

1908 - 1931





UNIwersYTET WARSZAWSKI

DOWÓD OSOBISTY  
AKADEMICKI

Student *Presburger* Wydz. *matemat.*

*Presburger Mojżesz*

jest zapisan. w Albumie Uniwersytetu  
Warszawskiego pod L. *10495*

t. cz.

REKTOR

Mojżesz Presburger

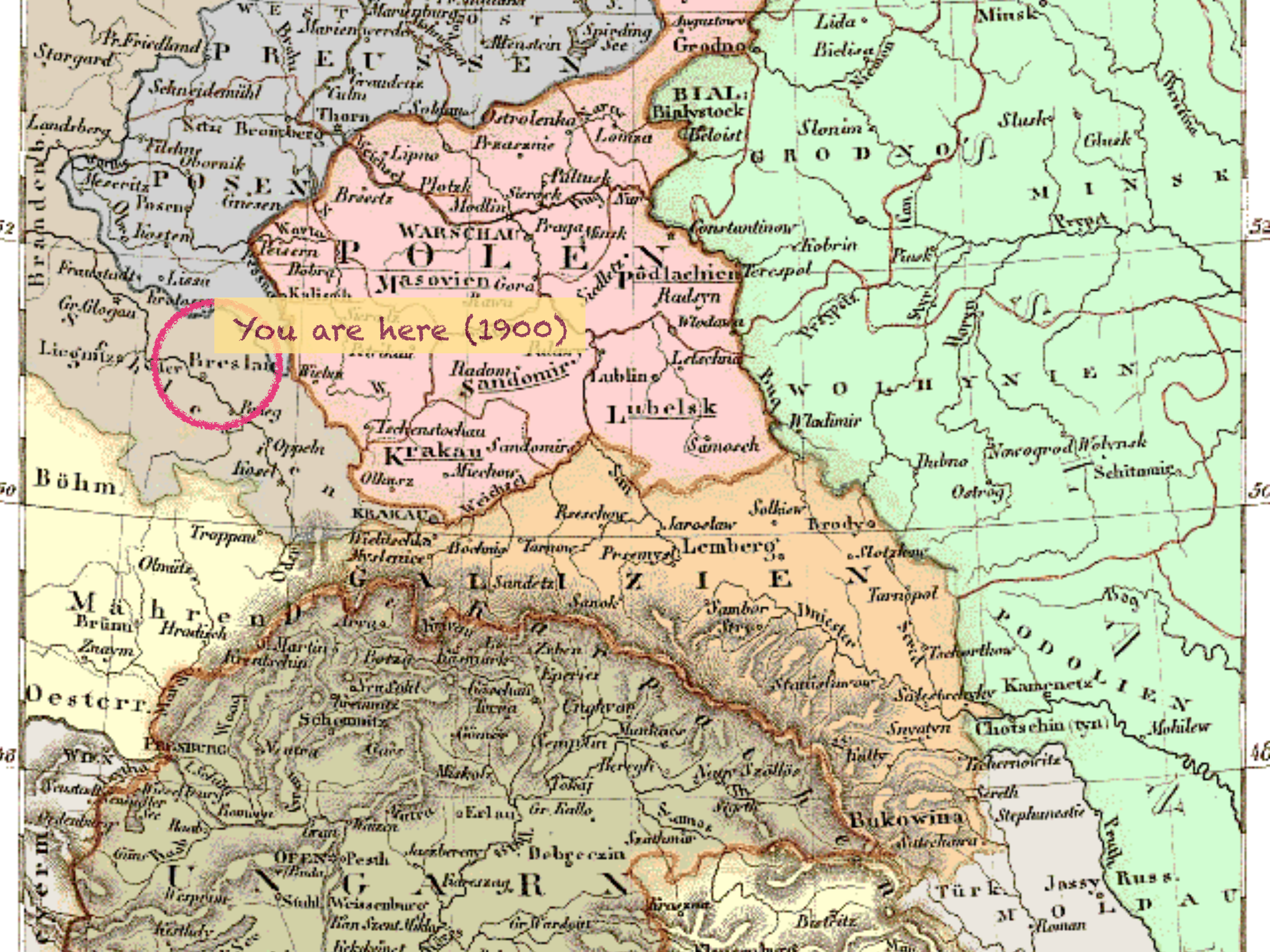
1904 - 1943



My Family



You are here (1900)







# Galicia

c. 1880

LEMBERG

Przemysl

Sambor

Boryslaw

Stanislawow

Monasterzysk

Husiatyn

MISKOLCZ

R

Y

N. Sziget

R. Suczawa

Radauz







45-90 " " " "  
90 & over " " " "

IN 1900  
English Miles

Cities with over 8000 inhab are shown in solid colour  
in circles proportionate to their population.  
The centre of population at each  
decennial census shown thus +1890.



1925-

ic of Cancer

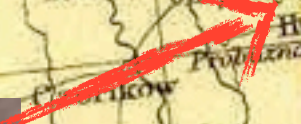
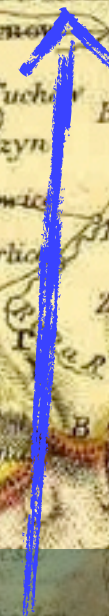




1903-1980



1897-1986







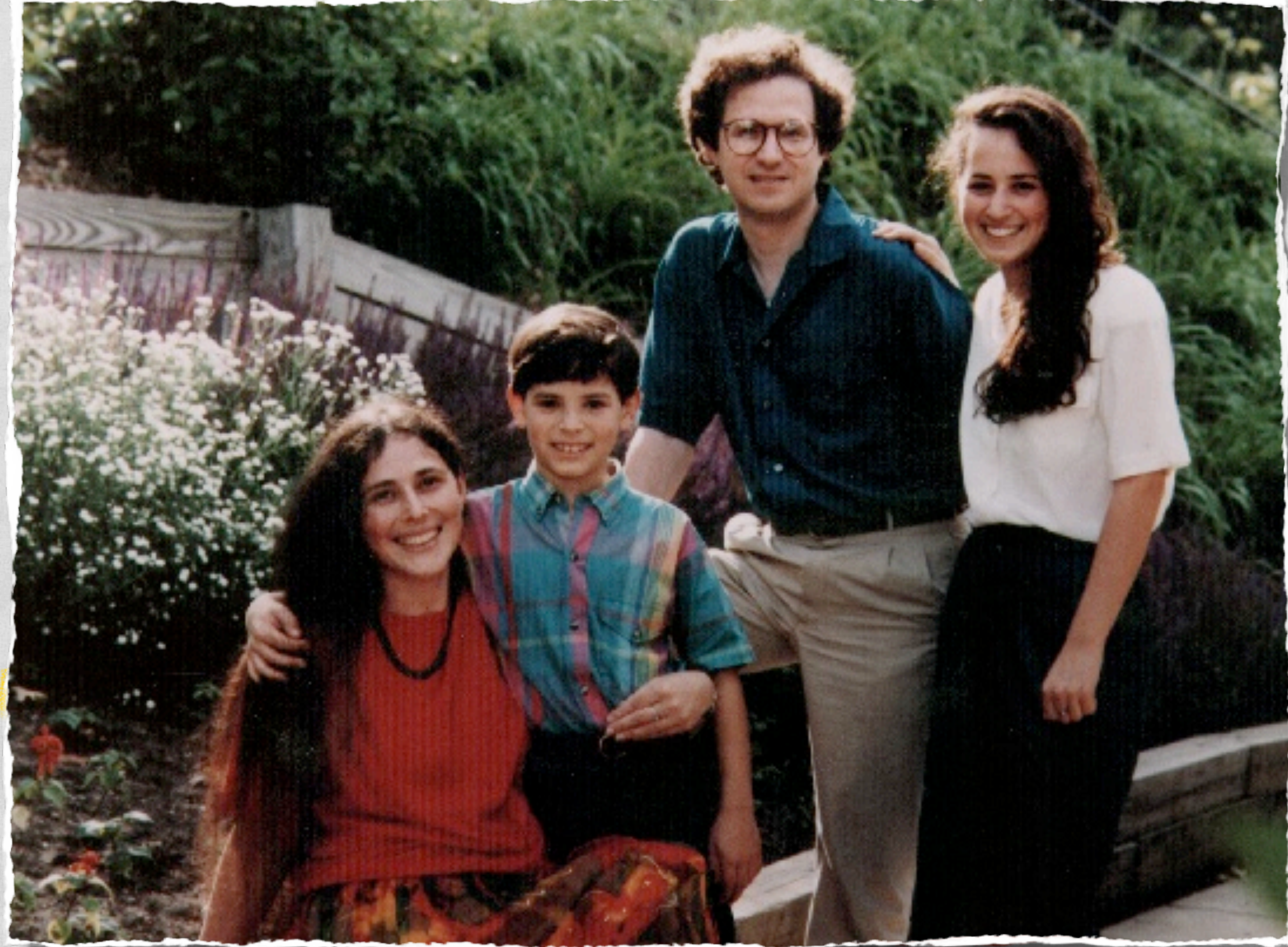
1932-





1951







My Teachers





[Uribe]



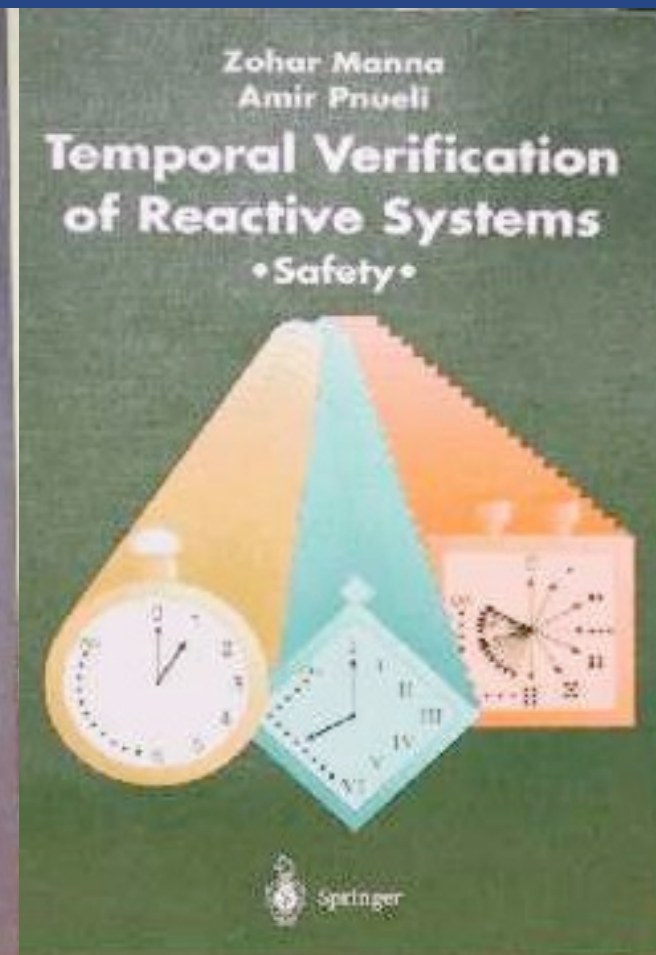
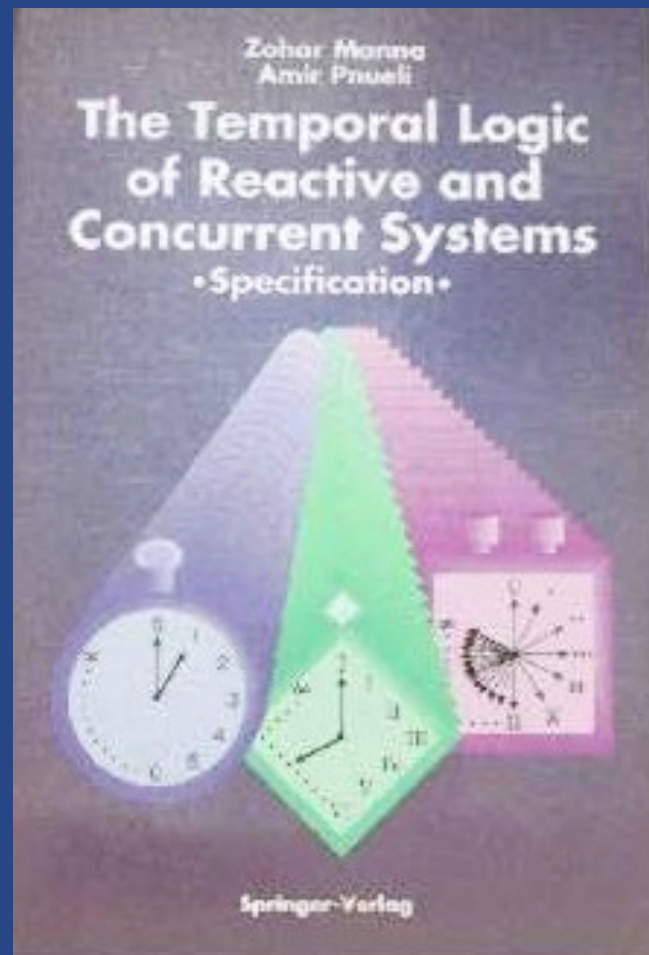
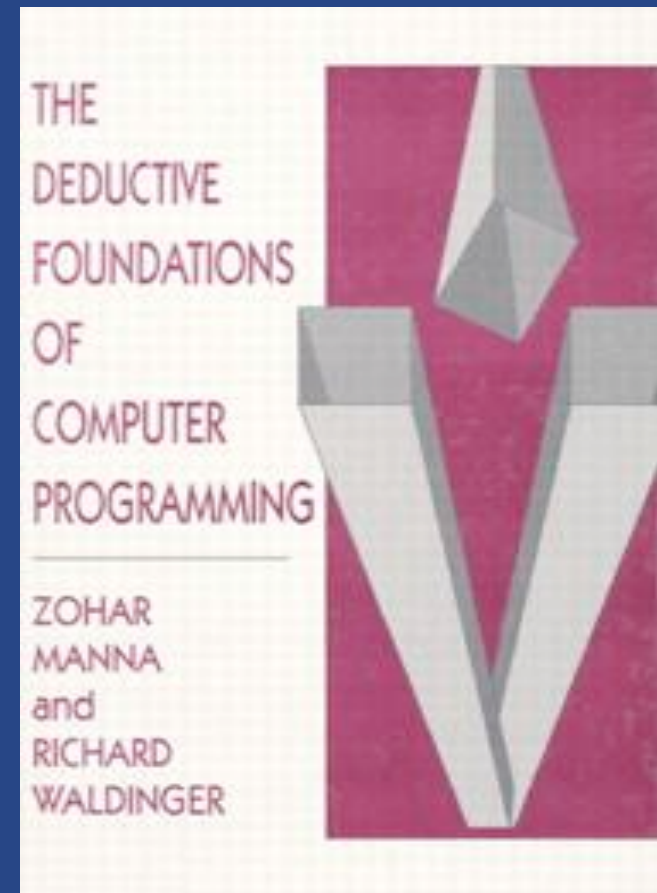
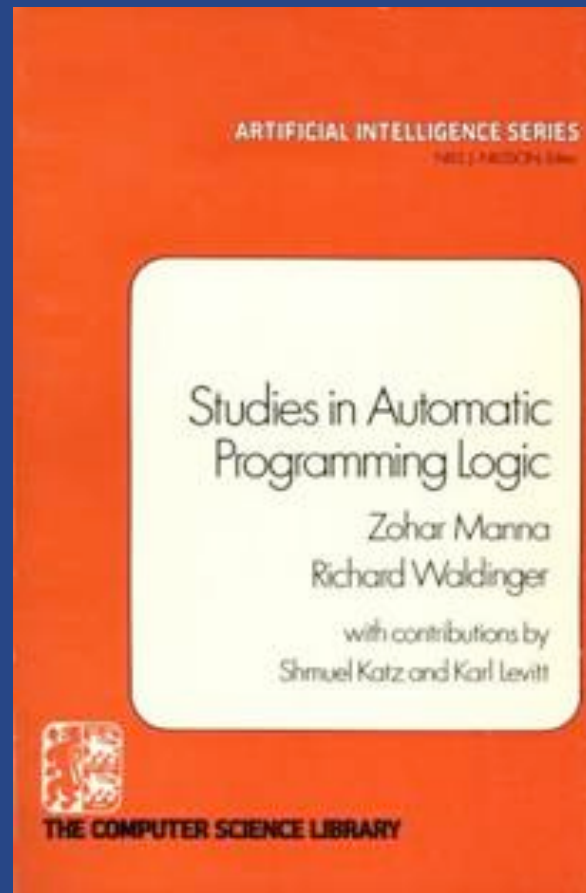




# Zohar Manna









Amir Pnueli  
Richard Waldinger



termination ideas



automated deduction



John McCarthy  
Don Knuth



AI Lab



completion



My Teacher's Teachers



Zohar Manna

CMU 1968



"Termination of  
Algorithms"

Manna & Pnueli

STeP



# Robert W Floyd

## Chicago

Zohar's advisor

Loop invariants

Termination

Dave Plaisted was his student





# Saul GORN

U Penn



Bob Floyd

Zohar Manna

Steve Ness

Amir Pnueli

Renato Iturriaga

- addressed termination of rewriting



# Gorn's Termination Question On Floyd's CMU Qual Exam

$$Dx \rightarrow 1$$

$$Dy \rightarrow 0$$

$$D(\alpha + \beta) \rightarrow (D\alpha + D\beta)$$

$$D(\alpha \cdot \beta) \rightarrow ((\beta \cdot D\alpha) + (\alpha \cdot D\beta))$$



# Alan Jay Perlis

MIT 1950

Zohar's advisor



One man's constant  
is another man's  
variable.

A Lisp programmer  
knows the value of  
everything, but the  
cost of nothing.



CONTRIBUTIONS TO MECHANICAL MATHEMATICS

by

Renato Iturriaga

May 27, 1967

DIGITAL COMPUTE  
LABORATORY  
LIBRARY

Perlis' student

Carnegie-Mellon University  
Pittsburgh, Pennsylvania



A MARKOV ALGORITHM FOR TRANSFORMING LOGICAL  
 FORMULAE INTO DISJUNCTIVE NORMAL FORM

```

001: 11002 BEGIN FORM A, B, C, R, X;
002: 11016 SYMBOL S, Y1;
003:
004: 11023 Y1 ← / [ OPERATOR: ^ ] [ COMMIT TRUE ];
005: 11053 A ← A: ANY; B ← B: ANY; C ← C: ANY;
006:
007: 11104 S ← [ [
008: 11107 ¬ ( A ^ B ) → ¬.A v ¬.B,
009: 11144 ¬ ( A v B ) → ¬.A ^ ¬.B,
010: 11202 ¬ A = B → .A = .3,
011: 11234 ¬ A = B → .A = .3,
012: 11266 ¬ A < B → .A < .3,
013: 11320 ¬ A < B → .A < .3,
014: 11352 ¬ A > B → .A > .3,
015: 11404 ¬ A > B → .A > .3,
016: 11417 ],
017: 11440 ( A v B ) | Y1 | C → .A ^ .C v .3 ^ .C ] ;
018:
019: 11517 R ← ¬( ¬( X < 8 ^ X > - 10 ) ^ X = 5 ) ^ ¬( X < 15 );
020: 11576 PRINT( R, R . S );
021: 11606 END

```

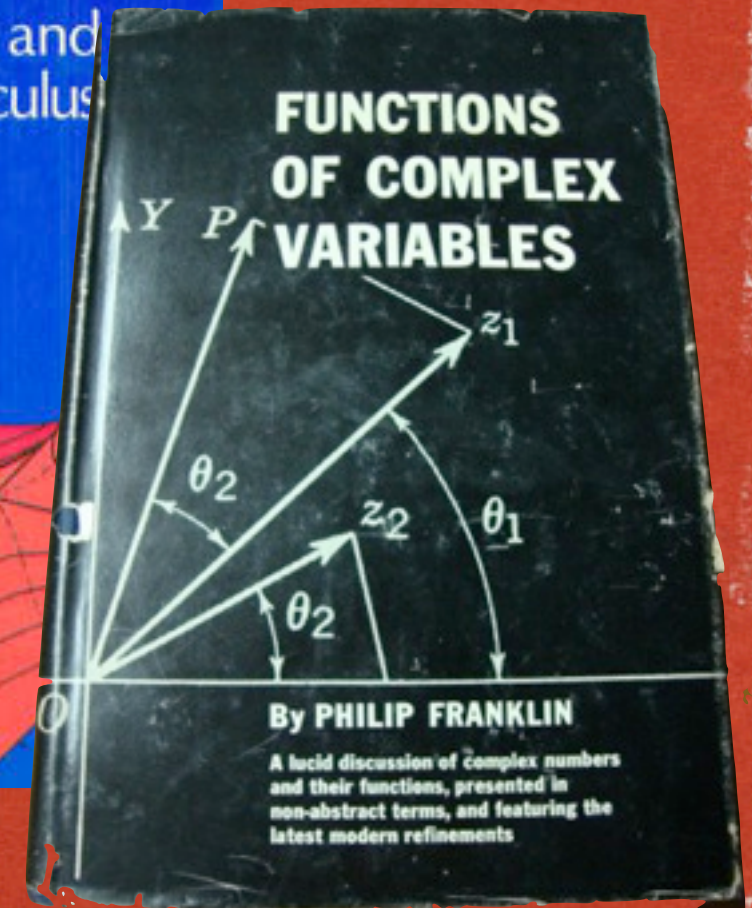
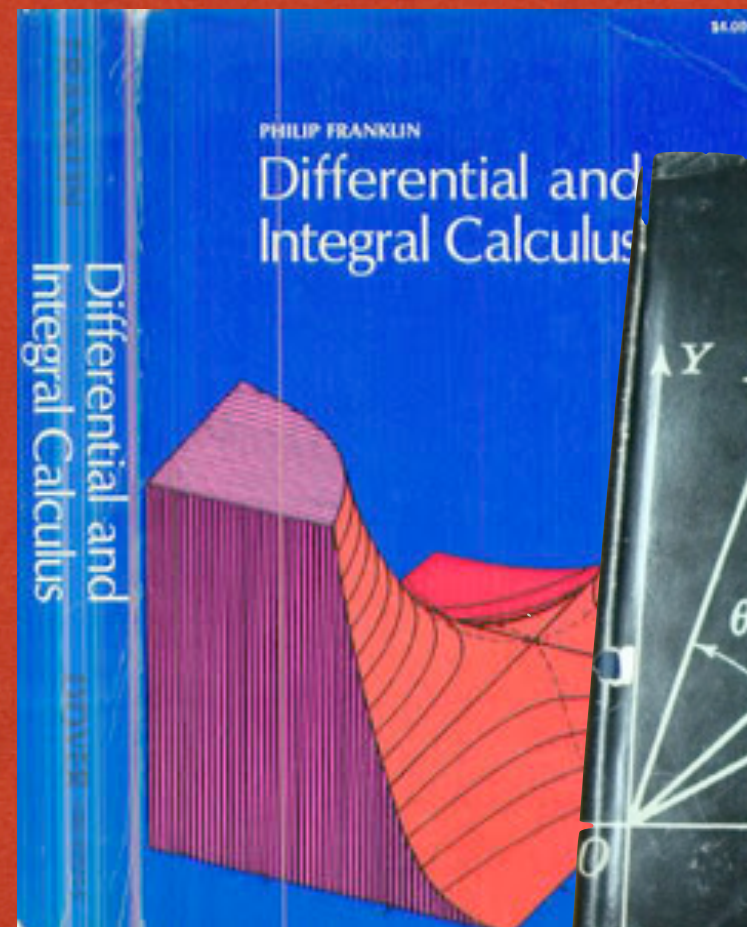


# Philip Franklin

## Princeton 1921

Pertis' advisor

"The four color  
problem"





# Oswald Veblen

## Chicago 1903



"A system of axioms  
for geometry"

Veblen ordinals



# Alonzo Church

student of Veblen



Peter Andrews  
Martin Davis  
Leon Henkin  
Stephen Kleene  
Michael Rabin  
Hartley Rogers  
John Rosser  
Dana Scott  
Raymond Smullyan  
Alan Turing

...



# Eliakim Hastings Moore

Yale 1885

Veblen's advisor

"Extension of certain theorems of Clifford and Cayley in the geometry of  $n$  dimensions"



George Birkhoff was his student



# Hubert Anson Newton

Yale 1850

Mathematician

Astronomer

Meteors

Comets





# Michel Chasles

## Polytechnique 1814

"Historical view of the origin and development of methods in geometry"

Acquired thousands of forged letters from Aristotle, etc.





# Chasles' Descendants

H. A. Newton

E. H. Moore

Oswald Veblen

Philip Franklin

Alan Perlis

Zohar Manna

\*

Gaston Darboux

C. Emile Picard

Ernest Vessiot

Herbrand



# Simeon Denis Poisson

## Polytechnique 1800



Poisson's equation

Definite integrals

Poisson spot

Poisson distribution



# Joseph Louis Lagrange

Giuseppe Lodovico  
Lagrangia

Mathematics

Mechanics

Astronomy

Lagrange inversion





# Leonhard Euler

Basel 1726

Mathematics

Function

Calculus

Astronomy

Graph theory

Logic

Euler diagrams





# Johann Bernoulli

Basel 1694

Catenary





# Jacob Bernoulli

## Basel



e



# Gottfried Leibniz

Alltdorf 1666



Calculemus!





# Christiaan Huygens

Leiden 1655

Discovered Titan

Invented pendulum  
clock

Wave theory of light





# Frans van Schooten

Leiden 1635

Popularized  
Descartes





# Jacobus Golius

Leiden 1621



Arabic and Persian  
lexicons

Taught math to  
Descartes



# Willebrord Snell van Royen

Leiden 1607

Willebrord Snellius

Mathematician

Discoveries by telescope

Rediscovered law of refraction





# Rudolph Snellius

Ruprecht Karls, Heidelberg 1572



Humanist

Taught Logic

Professor of Hebrew



# Valentine Naibod

## Luther U., Halle-Wittenberg

Mathematician

died on account of his  
astrological prediction of his  
own demise





# ERASMUS REINHOLD

Luther U., Halle-Wittenberg 1535



Gerhard Gerhards

Satirist

Renaissance scholar



# Jakob Millich

Wien 1524



Professor of math

Commentator on  
Pliny the Elder



# Desiderius Erasmus

Turin 1506

"Prince of the  
humanists"

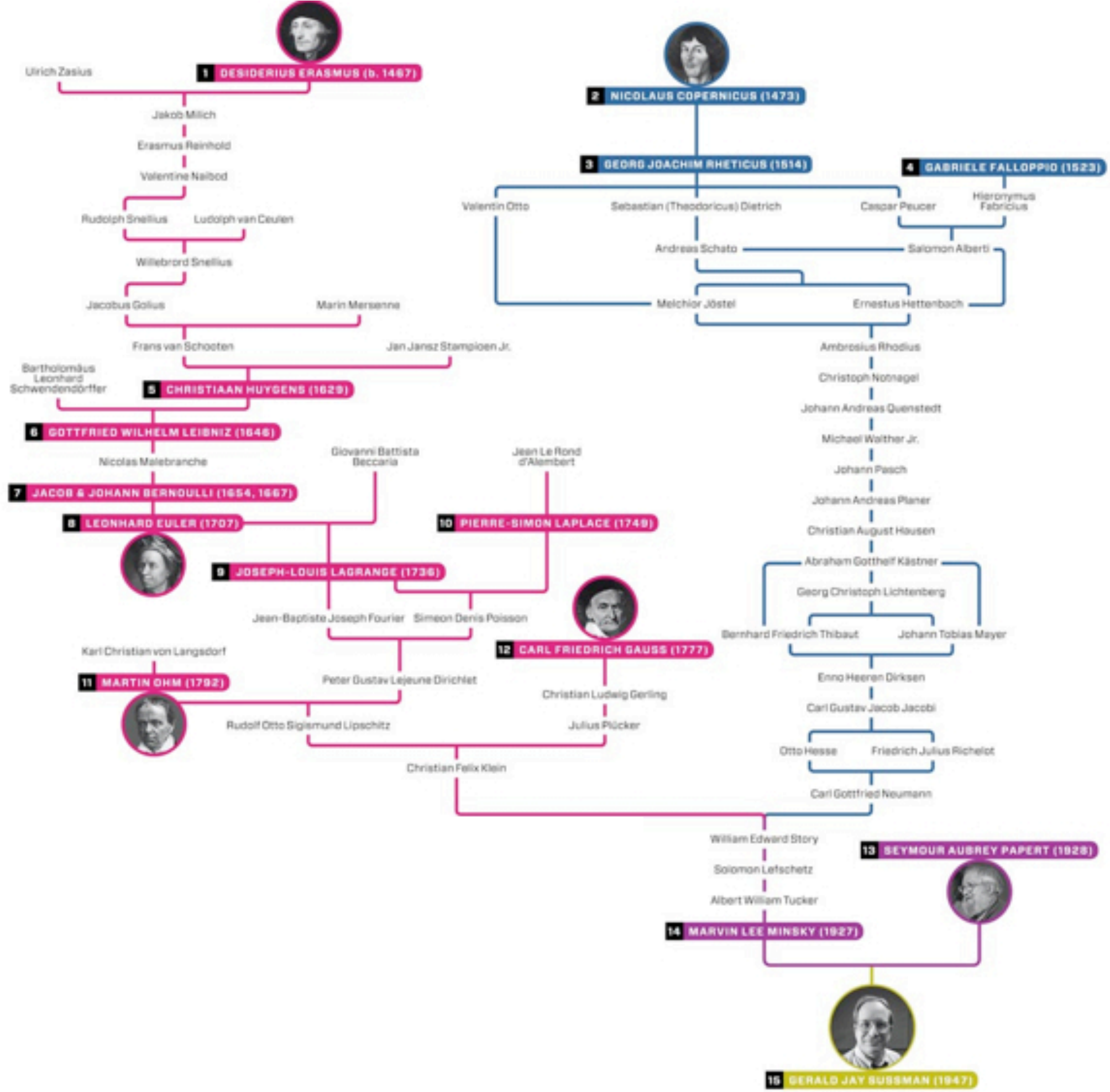
Encomium Moriae  
(The Praise of Folly)



[Holbein]









# Alexander Hegius

1474

Humanist

Generous to a fault





# Rudolph Agricola

Ferrara 1478



Introduced dialectics

Humanist

Hebrew scholar

Pioneer in teaching  
the deaf



# Theodoros Gazes

Mantova 1433

Translated Aristotle





# Vittorino da Feltrè

## Padova 1416

Educator

School field trips





# Guarino da Verona

Rome 1408



Collected  
manuscripts



# Manuel Chrysoloras

~1390

Μανουήλ Χρυσολωρᾶς

Translated Greek  
classics





# Demetrius Cydones

~1340



When someone comes along and says the Pope is in error and everyone ought to abjure such error, we really have been given no proof for such an allegation, and it makes no sense for anyone to pass judgment on what has first to be proven.



# Nilus Cabasilas

Salonika ~1320



Νεῖλος Καβάσιλας

90,373 descendants



# Nilus Cabasilas

Salonika ~1320

Νεῖλος Καβάσιλας

90,373 descendants



Read about him in Polish



My Peers



# Larry Wos (1992)



Resolution proofs

Set of support

"We don't just prove theorems. We look at conjectures, we design circuits, we solve puzzles, we prove properties of other programs."



# Woody Bledsoe (1994)

Non-resolution theorem-  
proving

Inequalities

"It taught me that 'if we have to do it, then we DO IT.' Nothing seems to have delayed me much since that day, even some very challenging times when we crossed the Rhine River."





# Alan Robinson (1996)



Resolution principle

Unification

"Part of the point... of the logical analysis of deductive reasoning has been to reduce complex inferences, which are beyond the capacity of the human mind to grasp as single steps, to chains of simpler inferences, each of which is within the capacity of the human mind to grasp as a single transaction."



# Wen-Tsun Wu (1997)



## Geometry as algebra

"During the cultural revolution I was sent to a factory manufacturing computers. I was initially struck by the power of the computer.... I began to understand what Chinese ancient mathematics really was.... It was under such influence that I investigated the possibility of proving geometry theorems in a mechanical way."



# G rard Huet (1998)



Rewriting theory

Higher-order unification

"Le traitement de la langue naturelle, ce qu'on nomme linguistique computationnelle, se situe au carrefour entre la linguistique, la logique et l'informatique."



# Bob Boyer & J Moore (1999)

Induction

Generalization



"With the aid of automatic theorem-provers, it is now often practical to do mathematics formally."



# Bill McCune (2000)



Otter & EqP

Indexing

Robbins' Conjecture

"In a sense, I have a feeling that the computer has been creative."



# Don Loveland (2001)



DPLL

Model elimination

"The most grandiose applications, such as full program synthesis, the mechanized mathematician, or the general reasoning machine, are not yet within view.... However, such automated deduction applications clearly can and will be developed, and they will be enormously beneficial."



# Mark Stickel (2002)

Unification

Indexing

PTTP

"Automated deductive program synthesis has been studied for many years but has never been used in practice."





# Peter Andrews (2003)

Higher-order

TPS

Mating



"Logical reasoning plays such a fundamental role in the spectrum of intellectual activities that advances in automating logic will inevitably have a profound impact on many intellectual disciplines."



# Harald Ganzinger (2004)

Superposition

Conditional rewriting

"Developers of state-of-the-art SAT solvers would need relatively little work to turn their solvers into DPLL(X) engines."





# Martin Davis (2005)



## Davis-Putnam

"How can we ever exclude the possibility of our being presented, some day (perhaps by some extraterrestrial visitors), with a device or "oracle" that "computes" an uncomputable function?"



# Wolfgang Bibel (2006)



Applications of first-order proving

Connection method

"Those who transformed from Logic to Informatics... became sort of banned, in any case kept in low regard."



# Alan Bundy (2007)

Induction heuristics

"[A review] is  
something that will  
ruin your day."





# Ed Clarke (2008)

Incremental model  
checking

"We found several errors that had been previously undetected. Apparently, this is the first time that formal methods have been used to find nontrivial errors in an IEEE standard."





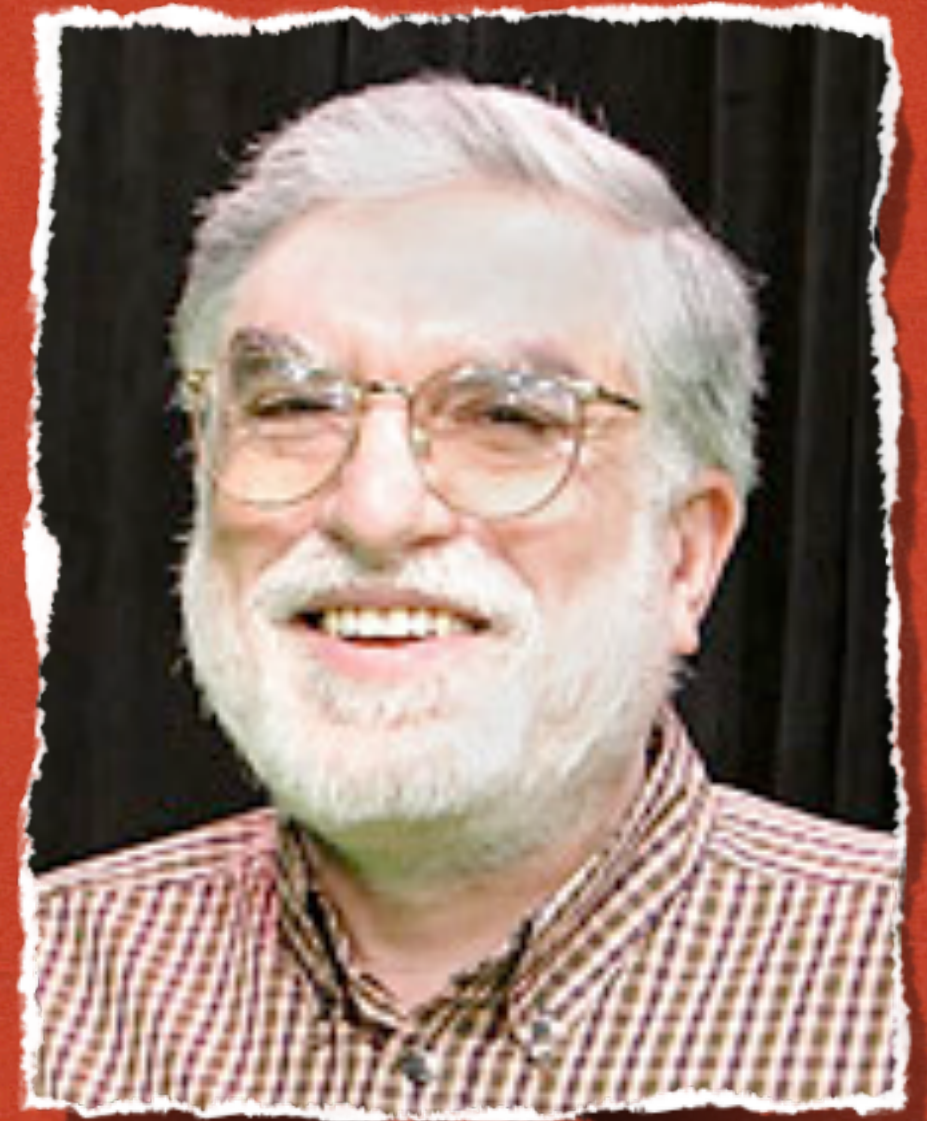
# Deepak Kapur (2009)

Algebra & Geometry

Equational

Invariants

"We analyze the perceptions of male and female CS/CE undergraduate students with regard to gender-related issues and show how they are articulated."





# Dave Plaisted (2010)

Strategies

Abstraction

Instance-based

"We are interested in the sizes of the search spaces produced by clause form refutational theorem proving strategies for first-order logic. This interest is different from that of most logicians who are interested in provability or the length of proofs."

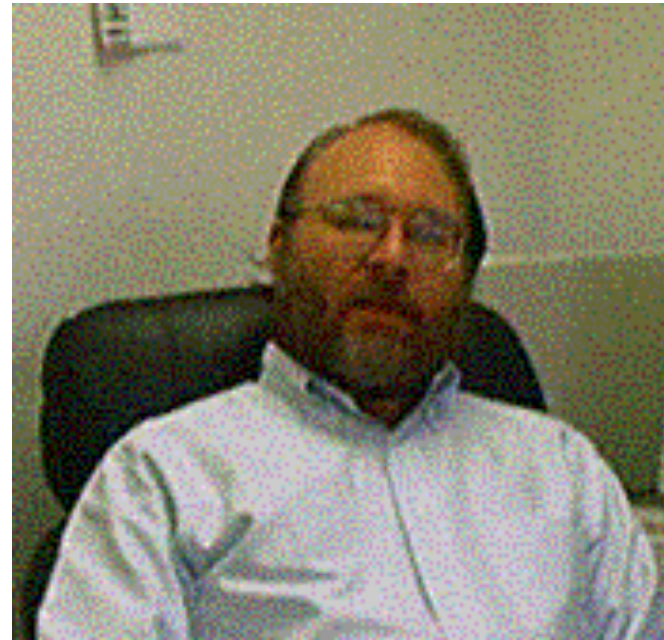




My Students  
(of deduction)



G Sivakumar



Charles Hoot



Naomi Lindenstrauss



Jieh Hsiang



Leo Bachmair





Subrata Mitra



Alan Josephson



Yuh-jeng  
Lee

Fei-Pei  
Lai



Ely  
Pinchover



Iddo  
Tzameret



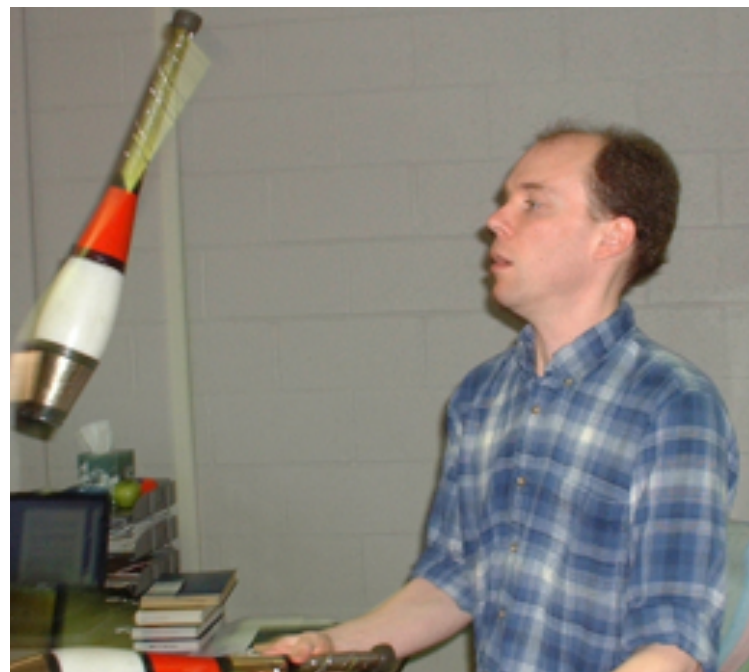




Alex Nadel



Daher Kaiss



Mitch Harris



Jacob Katz

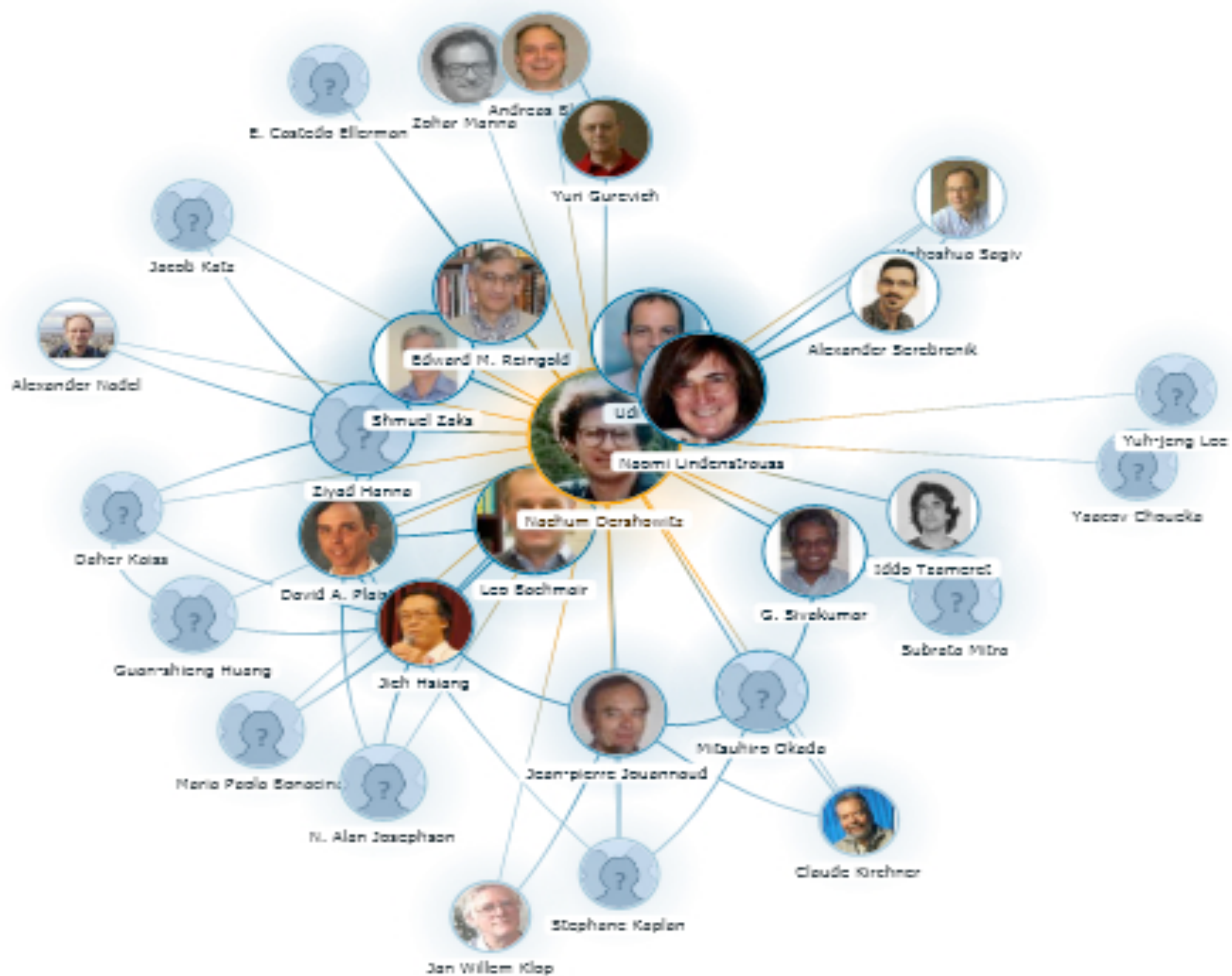


Yulik Feldman



My Circles







# CADE cfp

- Logics of interest include, but are not limited to
  - propositional, first-order, equational, higher-order, classical, description, modal, temporal, many-valued, intuitionistic, other non-classical, meta-logics, logical frameworks, type theory and set theory.
- Methods of interest include, but are not limited to
  - saturation, resolution, tableaux, sequent calculi, natural deduction, term rewriting, decision procedures, model generation, model checking, constraint solving, induction, unification, proof planning, proof checking, proof presentation and explanation.
- Applications of interest include, but are not limited to
  - program analysis and verification, hardware verification, mathematics, natural language processing, computational linguistics, knowledge representation, ontology reasoning, deductive databases, functional and logic programming, robotics, planning, and other areas of AI.



# CADE cfp

- Propositional
- Equational
- Term rewriting
- Unification
- Saturation
- Program verification
- Functional & logic programming
- Synthesis



# Propositional

• Alex Nadel

• Ziyad Hanna

• Yulik Feldman

• Guan-Shieng Huang

• Daher Kaiss

• Jieh Hsiang

• Mitch Harris



# Rewriting

• Leo Bachmair

• Jieh Hsiang

• G Sivakumar

• J-P Jouannaud

• David Plaisted

• Alan Josephson

• Stephane Kaplan

• Naomi Lindenstrauss

• Mitsu Okada

• Jan Willem Klop

• Leo Marcus

• Andrzej Tarlecki

• Ralf Treinen



# Saturation

© Leo Bachmair

© Claude Kirchner

© Jieh Hsiang

© Maria-Paola Bonacina

© David Plaisted

© Mitsu Okada



# Unification

• Subrata Mitra

• G Sivakumar

• Claude Kirchner

• Alan Josephson



# Verification

• Zohar Manna

• Jay Jayasimha

• Jacob Katz

• Seungjoon Park

• Ziyad Hanna



# Termination

• Zohar Manna

• Charles Hoot

• G Sivakumar

• Subrata Mitra

• Mitsu Okada

• Georg Moser

• Leo Bachmair

• Jieh Hsiang

• Naomi Lindenstrauss

• Shuki Sagiv

• Alex Serebrenik

• Iddo Tzameret

• Ed Reingold

• Castedo Ellerman





# Programming & Synthesis

• Zohar Manna

• Uday Reddy

• David Plaisted

• Alan Josephson

• Yuh-jeng Lee

• Ely Pinchover

• Naomi Lindenstrauss





Jouannaud



Klop



Plaisted



Treinen

Surveys

& Problems



Circles & Stars







# Shmuel Zaks

## Technion

coauthored

"Patterns in trees"





# Paul Erdős



"Minimum-diameter cyclic arrangements in mapping data-flow graphs onto VLSI arrays"



# Peter Salamon

## San Diego



"The solution to a  
problem of  
Grunbaum"



# Lars Kai Hansen

## TU Denmark

"Neural network  
ensembles"





# Nicholas T. Lange

## McLean Hospital (Harvard)

"Plurality and  
resemblance in  
fMRI data  
analysis"





# Bruce M. Cohen

## McLean Hospital (Harvard)



"Structural brain  
magnetic  
resonance imaging  
of limbic and  
thalamic volumes  
in pediatric  
bipolar disorder"



# Abigail A. Baird

## Dartmouth

"Functional  
magnetic  
resonance imaging  
of facial affect  
recognition in  
children and  
adolescents"





# Natalie Hersklag

## Harvard



"Frontal lobe  
activation during  
object  
permanence:  
Data from near-  
infrared  
spectroscopy"



# Natalie Portman Harvard



"Frontal lobe  
activation during  
object  
permanence:  
Data from near-  
infrared  
spectroscopy"



Freedom

Intellectual

Academic

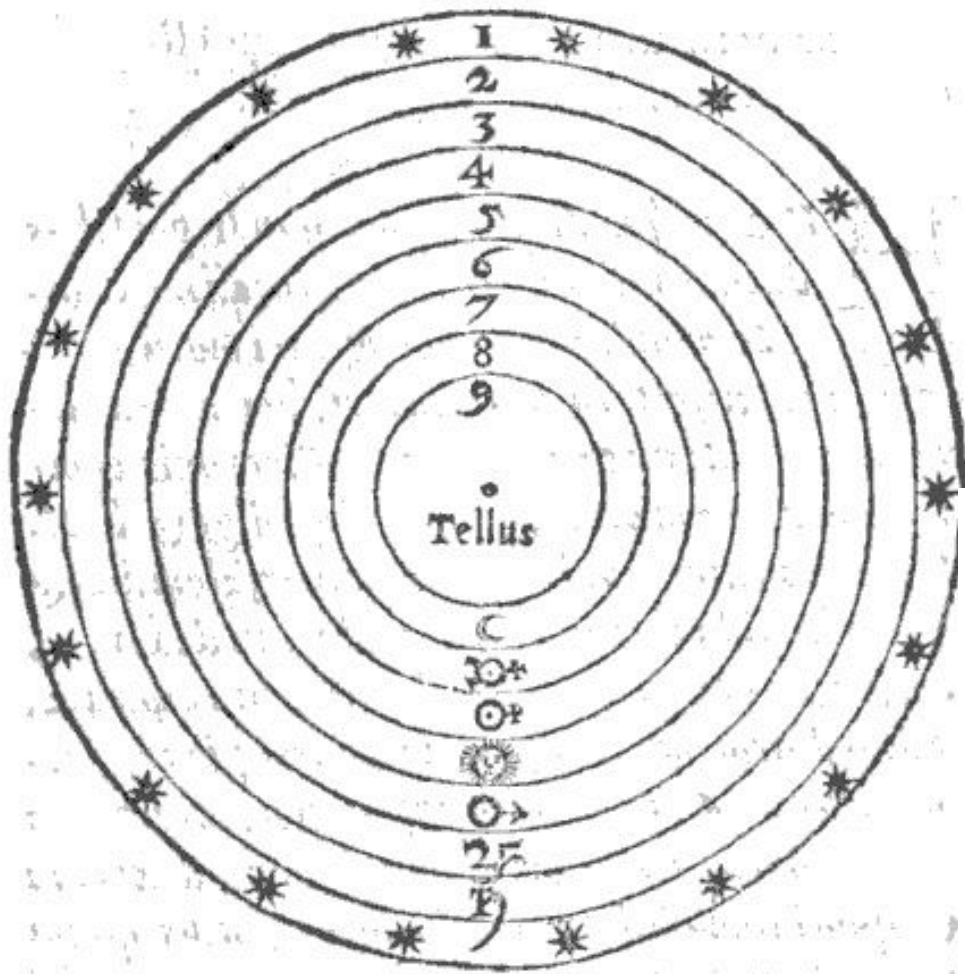




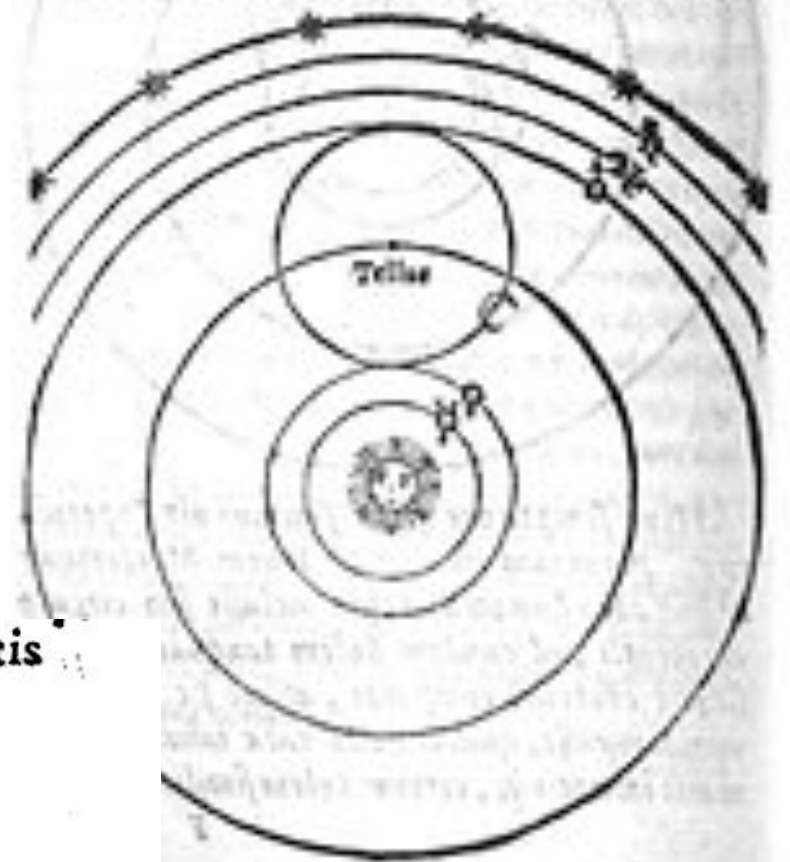
Mikolaj Kopernik



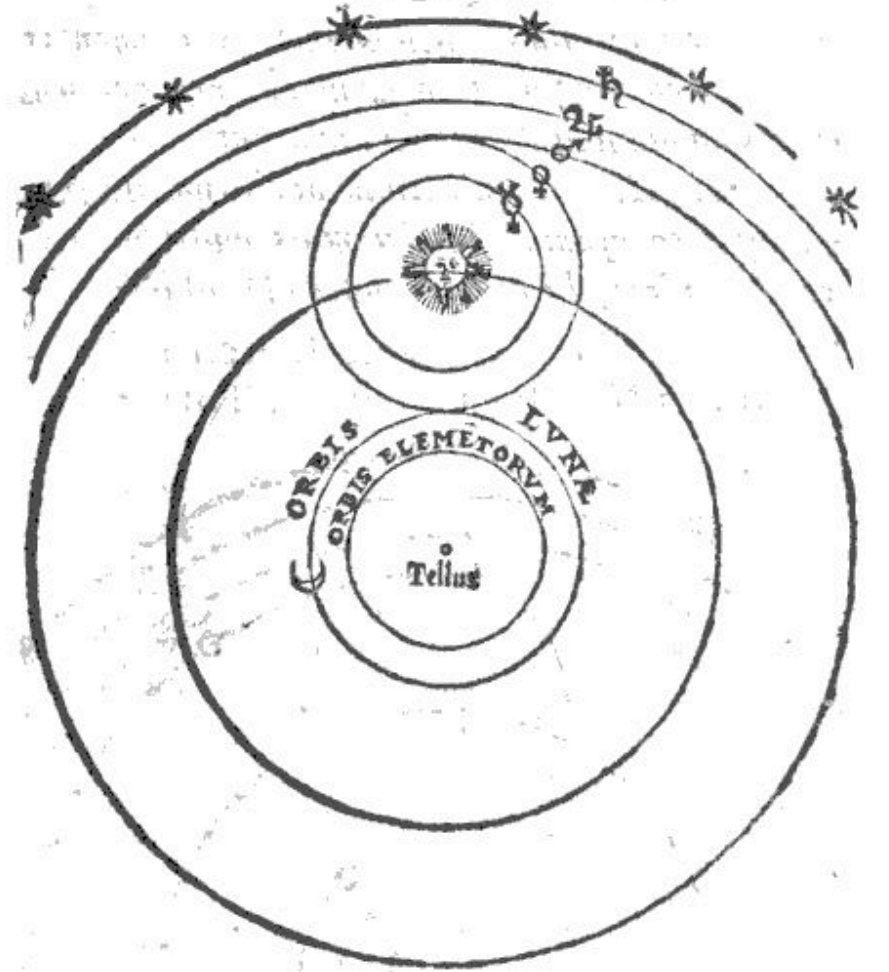
Systema maximarum mundi partium,  
 quibus totam rerum vniuersitatem  
 connexam esse tradiderunt communi-  
 ter authores.



Systema vniuersitatis de sententia sum-  
 mi viri Nicolai Copernici Torinensis.



Systema maximarum vniuersitatis  
 partium ex sententia Martiani  
 Capellæ.



Naibod





Boaz Trakhtenbrot

"Idealist of the Carnap Species"



# Bad Reviews

Theory  
conference:

Applications  
conference:

But where's the  
implementation?

But there are no  
theorems!

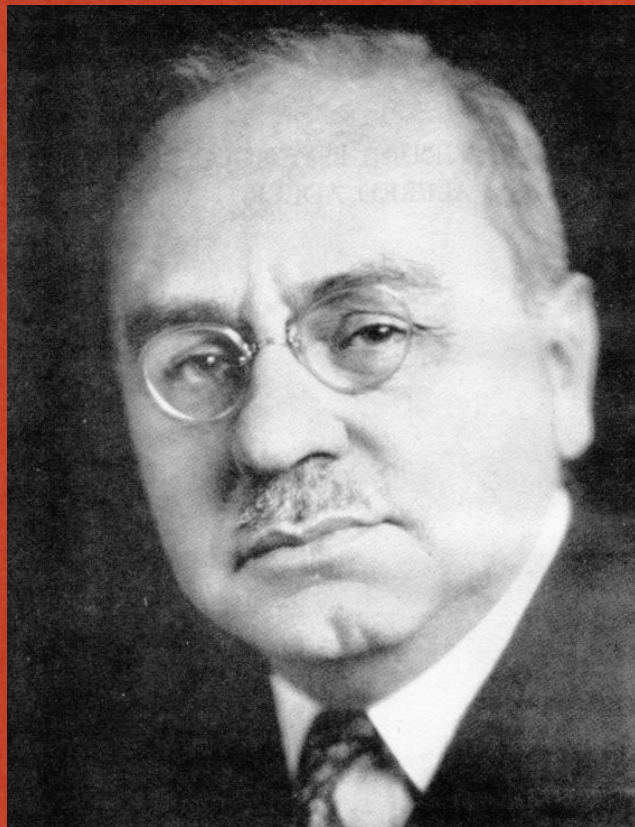


# Review of Toby Walsh

I don't find the phase transition experiments of much value at this stage. So, there may be a phase transition, so what?



# Motto



One good definition  
is worth three theorems.

- Alfred Adler  
"Mathematics and creativity"  
The New Yorker (1972)





# *In Memoriam*

*Millions in WWII*

*Stéphane Kaplan*

*Ron Book*

*Harald Ganzinger*

*Bob Floyd*

*Amir Pnueli*

*Bill McCune*