

product of the units of Q_k and Q_s . For most cases of interest involving the fundamental constants, the variables x_i may be taken to be the fractional change in the physical quantity from some fiducial value, and the quantities Q can be expressed as powers of physical constants Z_j according to

$$Q_k = q_k \prod_{j=1}^N Z_j^{Y_{kj}}, \quad (2)$$

where q_k is a auxiliary constant or a numerical factor. If the variances and covariances are then expressed in relative units, eq. (1) becomes

$$v_{ks} = \sum_{i,j=1}^N Y_{ki} Y_{sj} v_{ij}. \quad (3)$$

Equation (3) is the basis for the expansion of the variance matrix to include e , h , m_e , N_A , and F .

In terms of correlation coefficients defined by $r_{ij} = v_{ij}(v_{ii}v_{jj})^{-\frac{1}{2}} = v_{ij}/\epsilon_i\epsilon_j$, where ϵ_i is the standard deviation ($\epsilon_i^2 = v_{ii}$) we may write, from eq. (3),

$$\epsilon_k^2 = \sum_{i=1}^N Y_{ki}^2 \epsilon_i^2 + 2 \sum_{j < i}^N Y_{ki} Y_{kj} r_{ij} \epsilon_i \epsilon_j. \quad (4)$$

6 RECOMMENDED VALUES OF THE FUNDAMENTAL PHYSICAL CONSTANTS

This report is primarily concerned with establishing recognized standards of usage for symbols, units and nomenclature in physics, thus improving comprehension and understanding. However, communication is simplified not only if there are standards for symbols, but also if there is a uniformity of usage of the numerical values of the basic physical quantities that enter into data analysis in all branches of science and technology. To this end, the Committee on Data for Science and Technology (CODATA), through its Task Group on Fundamental Constants, has recommended a set of values of the physical constants for general use. These numerical values have the advantage that they are consistent in the sense that they properly reflect all known physical interrelationships among the constants and take into account the constraints imposed by the results of all evaluated experimental measurements and theoretical calculations.

The tables in this section are drawn from the Task Group report*, and are based on a least-squares adjustment with 17 degrees of freedom. The digits in parentheses following the numerical values are the one-standard-deviation uncertainty in the last digits of the given value.

Table 9 gives a listing of CODATA recommended values of important physical and chemical constants; table 10 gives the values of some conversion constants and standards which, although they cannot be considered to be 'fundamental' constants, are nonetheless important in pure and applied physics.

Since the uncertainties of many of these entries are correlated, the full variance matrix must be used in evaluating the uncertainties of quantities computed from them. An expanded variance matrix for the variables of tables 9 and 10 is given in table 11. To use this table note that the covariance between two quantities Q_k and Q_s which are functions of a common set of variables x_i ($i = 1, \dots, N$) is given by

$$v_{ks} = \sum_{i,j=1}^N \frac{\partial Q_k}{\partial x_i} \frac{\partial Q_s}{\partial x_j} v_{ij}, \quad (1)$$

where v_{ij} is the covariance of x_i and x_j . In this general form, the units of v_{ij} are the product of the units of x_i and x_j and the units of v_{ks} are the

* *The 1986 Adjustment of the Fundamental Physical Constants*, E. Richard Cohen and Barry N. Taylor, CODATA Bulletin Number 63 (Pergamon Press, Elmsford, NY 10523, USA, and Headinghill Hall, Oxford OX3 0BW, UK, November, 1986). CODATA is a Committee of the International Council of Scientific Unions, 51 Blvd de Montmorency, 75016 Paris, France.

Table 9. 1986 recommended values of the fundamental physical constants. The digits in parentheses are the one-standard-deviation uncertainty in the last digits of the given value. Since the uncertainties of many of these entries are correlated, the full variance matrix must be used in evaluating the uncertainties of quantities computed from them.

Quantity	Symbol	Value	Relative uncertainty, parts in 10^6
GENERAL CONSTANTS			
Universal constants			
speed of light in vacuum; <i>vitesse de la lumière dans le vide</i>	c	$299\,792\,458\text{ m s}^{-1}$	(exact)
permeability of vacuum; <i>perméabilité du vide</i>	μ_0	$4\pi \times 10^{-7}\text{ N A}^{-2}$ $= 12.566\,370\,614 \dots \times 10^{-7}\text{ N A}^{-2}$	(exact)
permittivity of vacuum; <i>permittivité du vide</i> : $1/\mu_0 c^2$	ϵ_0	$8.854\,187\,817 \dots \times 10^{-12}\text{ F m}^{-1}$	(exact)
gravitational constant; <i>constante de gravitation</i>	G	$6.672\,59(85) \times 10^{-11}\text{ m}^3\text{ kg}^{-1}\text{ s}^{-2}$	128
Planck constant; <i>constante de Planck</i>	h	$6.626\,0755(40) \times 10^{-34}\text{ J s}$	0.60
$h/2\pi$	\hbar	$4.135\,6692(12) \times 10^{-15}\text{ eV s}$ $1.054\,572\,66(63) \times 10^{-34}\text{ J s}$ $6.582\,1220(20) \times 10^{-16}\text{ eV s}$	0.30 0.60 0.30
Planck mass; <i>masse de Planck</i> : $(\hbar c/G)^{1/2}$	m_P	$2.176\,71(14) \times 10^{-8}\text{ kg}$	64
Planck length; <i>longueur de Planck</i> : $\hbar/m_P c = (\hbar G/c^3)^{1/2}$	l_P	$1.616\,05(10) \times 10^{-35}\text{ m}$	64
Planck time; <i>temps de Planck</i> : $l_P/c = (\hbar G/c^5)^{1/2}$	t_P	$5.390\,56(34) \times 10^{-44}\text{ s}$	64
Electromagnetic constants			
elementary charge; <i>charge élémentaire</i>	e	$1.602\,177\,33(49) \times 10^{-19}\text{ C}$	0.30
magnetic flux quantum; <i>quantum de flux magnétique</i> : $h/2e$	e/h	$2.417\,988\,36(72) \times 10^{14}\text{ A J}^{-1}$	0.30
Josephson frequency-voltage quotient; <i>quotient fréquence-tension dans l'effet Josephson</i>	Φ_0	$2.067\,834\,61(61) \times 10^{-15}\text{ Wb}$	0.30
quantized Hall conductance; <i>conductance quantifiée de Hall</i>	$2e/h$	$4.835\,9767(14) \times 10^{14}\text{ Hz V}^{-1}$	0.30
quantized Hall resistance; <i>résistance quantifiée de Hall</i> : $h/e^2 = \mu_0 c/2\alpha$	e^2/h	$3.874\,046\,14(17) \times 10^{-5}\text{ S}$	0.045
Bohr magneton; <i>magnéton de Bohr</i> : $e\hbar/2m_e$	R_H	$25\,812.8056(12)\text{ }\Omega$	0.045
	μ_B	$9.274\,0154(31) \times 10^{-24}\text{ J T}^{-1}$	0.34
	μ_B/h	$5.788\,382\,63(52) \times 10^{-5}\text{ eV T}^{-1}$	0.089
	μ_B/hc	$1.399\,624\,18(42) \times 10^{10}\text{ Hz T}^{-1}$	0.30
	μ_B/k	$46.686\,437(14)\text{ m}^{-1}\text{ T}^{-1}$ $0.671\,7099(57)\text{ K T}^{-1}$	0.30 8.5

nuclear magneton; <i>magnéton nucléaire</i> : $e\hbar/2m_p$	μ_N	$5.050\,7866(17) \times 10^{-27}\text{ J T}^{-1}$ $3.152\,451\,66(28) \times 10^{-8}\text{ eV T}^{-1}$	0.34 0.089
	μ_N/h	$7.622\,5914(23)\text{ MHz T}^{-1}$	0.30
	μ_N/hc	$2.542\,622\,81(77) \times 10^{-2}\text{ m}^{-1}\text{ T}^{-1}$	0.30
	μ_N/k	$3.658\,246(31) \times 10^{-4}\text{ K T}^{-1}$	8.5

ATOMIC CONSTANTS

fine-structure constant; <i>constante de structure fine</i> : $\mu_0 c e^2/2h$	α	$0.007\,297\,353\,08(33)$	0.045
	α^{-1}	$137.035\,9895(61)$	0.045
	α^2	$5.325\,136\,20(48) \times 10^{-5}$	0.090
Rydberg constant; <i>constante de Rydberg</i> : $m_e c \alpha^2/2h$	R_∞	$10\,973\,731.534(13)\text{ m}^{-1}$	0.0012
	$R_\infty c$	$3.289\,841\,9499(39) \times 10^{15}\text{ Hz}$	0.0012
	$R_\infty hc$	$2.179\,8741(13) \times 10^{-18}\text{ J}$ $13.605\,6981(40)\text{ eV}$	0.60 0.30
Bohr radius; <i>rayon de Bohr</i> : $a_0/4\pi R_\infty$	a_0	$0.529\,177\,249(24) \times 10^{-10}\text{ m}$	0.045
quantum of circulation; <i>quantum de circulation</i>	$h/2m_e$	$3.636\,948\,07(33) \times 10^{-4}\text{ m}^2\text{ s}^{-1}$	0.089
	h/m_e	$7.273\,896\,14(65) \times 10^{-4}\text{ m}^2\text{ s}^{-1}$	0.089
Electron			
electron mass; <i>masse de l'électron</i>	m_e	$9.109\,3897(54) \times 10^{-31}\text{ kg}$ $5.485\,799\,03(13) \times 10^{-4}\text{ u}$ $0.510\,999\,06(15)\text{ MeV}$	0.59 0.023 0.30
electron-muon mass ratio; <i>rapport de la masse du muon à celle de l'électron</i>	m_μ/m_μ	$0.004\,836\,332\,18(71)$	0.15
electron-proton mass ratio; <i>rapport de la masse de l'électron à celle du proton</i>	m_e/m_p	$5.446\,170\,13(11) \times 10^{-4}$	0.020
electron-deuteron mass ratio; <i>rapport de la masse du deuteron à celle de l'électron</i>	m_e/m_d	$2.724\,437\,07(6) \times 10^{-4}$	0.020
electron- α -particle mass ratio; <i>rapport de la masse de la particule α à celle de l'électron</i>	m_e/m_α	$1.370\,933\,54(3) \times 10^{-4}$	0.021
electron specific charge; <i>charge massique de l'électron</i>	$-e/m_e$	$-1.758\,819\,62(53) \times 10^{11}\text{ C kg}^{-1}$	0.30
electron molar mass; <i>masse molaire de l'électron</i>	$M(e), M_e$	$5.485\,799\,03(13) \times 10^{-7}\text{ kg/mol}$	0.023
Compton wavelength; <i>longueur d'onde de Compton</i> : $h/m_e c$	λ_C	$2.426\,310\,58(22) \times 10^{-12}\text{ m}$	0.089
$\lambda_C/2\pi = \alpha a_0 = \alpha^2/4\pi R_\infty$	λ_C	$3.861\,593\,23(35) \times 10^{-13}\text{ m}$	0.089
classical electron radius; <i>rayon classique de l'électron</i> : $\alpha^2 a_0$	r_e	$2.817\,940\,92(38) \times 10^{-15}\text{ m}$	0.13
Thomson cross section; <i>section efficace de Thomson</i> : $(8\pi/3)r_e^2$	σ_e	$0.665\,246\,16(18) \times 10^{-28}\text{ m}^2$	0.27

electron magnetic moment; <i>moment magnétique de l'électron</i>	μ_e	9.2847701(31) $\times 10^{-24}$ J T ⁻¹	0.34	
	μ_e/μ_B	1.001159652193(10)	1×10^{-5}	
	μ_e/μ_N	1838.282000(37)	0.020	
electron-muon magnetic moment ratio;	μ_e/μ_μ	206.766967(30)	0.15	
<i>rapport du moment magnétique de l'électron à celui du muon</i>	μ_e/μ_p	658.2106881(66)	0.010	
electron-proton magnetic moment ratio;	Muon			
<i>rapport du moment magnétique de l'électron à celui du proton</i>	m_μ	1.8835327(11) $\times 10^{-28}$ kg	0.61	
muon mass; <i>masse du muon</i>		0.113428913(17) u	0.15	
muon-electron mass ratio; <i>rapport de la masse du muon à celle de l'électron</i>	m_μ/m_e	105.658389(34) MeV	0.32	
muon molar mass;	$M(\mu), M_\mu$	206.768262(30)	0.15	
<i>masse molaire du muon</i>		1.13428913(17) $\times 10^{-4}$ kg/mol	0.15	
muon magnetic moment; <i>moment magnétique du muon</i>	μ_μ	4.4904514(15) $\times 10^{-26}$ J T ⁻¹	0.33	
muon magnetic moment anomaly; <i>anomalie du moment magnétique du muon</i> : $[\mu_\mu/(eh/2m_\mu)] - 1$	μ_μ/μ_B	0.00484197097(71)	0.15	
muon-proton magnetic moment ratio;	μ_μ/μ_N	8.8905981(13)	0.15	
<i>rapport du moment magnétique du muon à celui du proton</i>	a_μ	0.0011659230(84)	7.2	
proton mass; <i>masse du proton</i>	μ_μ/μ_p	3.18334547(47)	0.15	
proton-electron mass ratio; <i>rapport de la masse du proton à celle de l'électron</i>	Proton			
proton-muon mass ratio;	m_p	1.6726231(10) $\times 10^{-27}$ kg	0.59	
<i>rapport de la masse du proton à celle de l'électron</i>		1.007276470(12) u	0.012	
proton-muon magnetic moment ratio;		938.27231(28) MeV	0.30	
<i>rapport de la masse du proton à celle du muon</i>	m_p/m_e	1836.152701(37)	0.020	
charge massive du proton	m_p/m_μ	8.8802444(13)	0.15	
proton molar mass;	e/m_p	9.5788309(29) $\times 10^7$ C kg ⁻¹	0.30	
<i>masse molaire du proton</i>	$M(p), M_p$	1.007276470(12) $\times 10^{-3}$ kg/mol	0.012	
proton Compton wavelength; <i>longueur d'onde de Compton du proton</i> : $h/m_p c$	$\lambda_{C,p}$	1.32141002(12) $\times 10^{-15}$ m	0.089	
	$\lambda_{C,p}/2\pi$	2.10308937(19) $\times 10^{-16}$ m	0.089	
proton magnetic moment; <i>moment magnétique du proton</i>	μ_p	1.41060761(47) $\times 10^{-26}$ J T ⁻¹	0.34	
	μ_p/μ_B	0.001521032202(15)	0.010	
	μ_p/μ_N	2.792847386(63)	0.023	
diamagnetic shielding correction; <i>facteur d'écran diamagnétique (H₂O, sph., 25 °C) : $1 - \mu_p/\mu_p$</i>	σ_{H_2O}	25.689(15) $\times 10^{-6}$	-	
shielded proton moment; <i>moment magnétique du proton non corrigé (H₂O, sph., 25 °C)</i>	μ'_p	1.41057138(47) $\times 10^{-26}$ J T ⁻¹	0.34	
proton gyromagnetic ratio; <i>coefficient gyromagnétique du proton</i>	μ'_p/μ_B	0.001520993129(17)	0.011	
	μ'_p/μ_N	2.792775642(64)	0.023	
neutron-electron mass ratio; <i>rapport de la masse du neutron à celle de l'électron</i>	γ_p	26752.2128(81) $\times 10^4$ s ⁻¹ T ⁻¹	0.30	
neutron-proton mass ratio; <i>rapport de la masse du neutron à celle du proton</i>	$\gamma_p/2\pi$	42.577469(13) MHz T ⁻¹	0.30	
neutron molar mass;	γ'_p	26751.5255(81) $\times 10^4$ s ⁻¹ T ⁻¹	0.30	
<i>masse molaire du neutron</i>	$\gamma'_p/2\pi$	42.576375(13) MHz T ⁻¹	0.30	
neutron magnetic moment; <i>moment magnétique du neutron</i>	Neutron			
	m_n	1.6749286(10) $\times 10^{-27}$ kg	0.59	
		1.008664904(14) u	0.014	
		939.56563(28) MeV	0.30	
neutron-electron mass ratio; <i>rapport de la masse du neutron à celle de l'électron</i>	m_n/m_e	1838.683662(40)	0.022	
neutron-proton mass ratio; <i>rapport de la masse du neutron à celle du proton</i>	m_n/m_p	1.001378404(9)	0.009	
neutron molar mass;	$M(n), M_n$	1.008664904(14) $\times 10^{-3}$ kg/mol	0.014	
<i>masse molaire du neutron</i>				
neutron Compton wavelength; <i>longueur d'onde de Compton du neutron</i> : $h/m_n c$	$\lambda_{C,n}$	1.31959110(12) $\times 10^{-15}$ m	0.089	
	$\lambda_{C,n}/2\pi$	2.10019445(19) $\times 10^{-16}$ m	0.089	
neutron magnetic moment;	μ_n	0.96623707(40) $\times 10^{-26}$ J T ⁻¹	0.41	
<i>moment magnétique du neutron</i>	μ_n/μ_B	0.00104187563(25)	0.24	
	μ_n/μ_N	1.91304275(45)	0.24	
neutron-electron magnetic moment ratio;	μ_n/μ_e	0.00104066882(25)	0.24	
<i>rapport du moment magnétique du neutron à celui de l'électron</i>				
neutron-proton magnetic moment ratio;	μ_n/μ_p	0.68497934(16)	0.24	
<i>rapport du moment magnétique du neutron à celui du proton</i>	Deuteron			
deuteron mass; <i>masse du deuteron</i>	m_d	3.3435860(20) $\times 10^{-27}$ kg	0.59	
		2.013553214(24) u	0.012	
		1875.61339(57) MeV	0.30	

deuteron-electron mass ratio;
*rappart de la masse du deuteron
à celle de l'électron*
deuteron-proton mass ratio;
*rappart de la masse du deuteron
à celle du proton*
deuteron molar mass;
masse molaire du deuteron
deuteron magnetic moment;
moment magnétique du deuteron

deuteron-electron magnetic
moment ratio;

*rappart du moment magnétique
du deuteron à celui de l'électron*
deuteron-proton magnetic
moment ratio;

*rappart du moment magnétique
du deuteron à celui du proton*

PHYSICO-CHEMICAL CONSTANTS

Avogadro constant;
constante d'Avogadro
atomic mass constant;
constante de masse atomique :
 $\frac{1}{12}m(^{12}\text{C})$

Faraday constant;

constante de Faraday
molar Planck constant;

constante molaire de Planck

molar gas constant;

*constante molaire de gaz
Boltzmann constant;*

constante de Boltzmann : R/N_A

molar volume (ideal gas);

volume molaire (gaz parfait) : RT/p

$T = 273.15 \text{ K}$, $p = 101325 \text{ Pa}$

Loschmidt constant;

constante de Loschmidt : N_A/V_m

Sackur-Tetrode (absolute entropy)

constant; *constante de Sackur-*

Tetrode (entropie absolue) : *

$\frac{5}{2} + \ln\{(2\pi m_u kT_1/h^2)^{3/2} kT_1/p_0\}$

$T_1 = 1 \text{ K}$, $p_0 = 100 \text{ kPa}$

$P_0 = 101325 \text{ Pa}$

m_d/m_e 3670.483014(75) 0.020

m_d/m_p 1.999007496(6) 0.003

$M(\text{d})$, M_d 2.013553214(24) $\times 10^{-3}$ kg/mol 0.012

μ_d 0.43307375(15) $\times 10^{-26}$ J T⁻¹ 0.34

μ_d/μ_B 0.4669754479(91) $\times 10^{-3}$ 0.019

μ_d/μ_N 0.857438230(24) 0.028

μ_d/μ_e 4.664345460(91) $\times 10^{-4}$ 0.019

μ_d/μ_p 0.3070122035(51) 0.017

N_A , L 6.0221367(36) $\times 10^{23}$ mol⁻¹ 0.59

m_u 1.6605402(10) $\times 10^{-27}$ kg 0.59

931.49432(28) MeV 0.30

F 96485.309(29) C mol⁻¹ 0.30

$N_A h$ 3.99031323(36) $\times 10^{-10}$ J s mol⁻¹ 0.089

$N_A hc$ 0.11962658(11) J m mol⁻¹ 0.089

R 8.314510(70) J mol⁻¹ K⁻¹ 8.4

k 1.380658(12) $\times 10^{-23}$ J K⁻¹ 8.5

8.617385(73) $\times 10^{-5}$ eV K⁻¹ 8.4

k/h 2.083674(18) $\times 10^{10}$ Hz K⁻¹ 8.4

k/hc 69.50387(59) m⁻¹ K⁻¹ 8.4

V_m 22414.10(19) cm mol⁻¹ 8.4

n_0 2.686763(23) $\times 10^{25}$ m⁻³ 8.5

S_0/R -1.151693(21) 18

-1.164856(21) 18

RADIATION CONSTANTS

Stefan-Boltzmann constant;

constante de Stefan-Boltzmann :
 $(\pi^2/60)k^4/h^3c^2$

first radiation constant;

première constante

de rayonnement : $2\pi hc^2$

second radiation constant;

deuxième constante

de rayonnement : hc/k

Wien displacement law constant;

constante de la loi du déplacement

de Wien :

$\lambda_{\text{max}}T = c_2/4.96511423\dots$

b 0.002897756(24) m K 8.4

c_2 0.01438769(12) m K 8.4

σ 5.67051(19) $\times 10^{-8}$ W m⁻² K⁻⁴ 34

c_1 3.7417749(22) $\times 10^{-16}$ W m² 0.60

* The molar entropy of an ideal monatomic gas of relative atomic weight A_r is given by
 $S = S_0 + \frac{3}{2}R \ln A_r - R \ln(p/p_0) + \frac{5}{2}R \ln(T/K)$.

Table 10. Maintained units and standard values.

Quantity	Symbol	Value	Relative uncertainty, parts in 10^6
electron volt: $(e/C)J = \{e\}J$	eV	$1.60217733(49) \times 10^{-19} J$	0.30
(unified) atomic mass unit: $1 u = m_u = \frac{1}{12}m(^{12}C)$	u	$1.67354385(33) \times 10^{-27} kg$	8.5
standard atmosphere	atm	$101325 Pa$	0.30
standard acceleration of gravity	g_n	$9.80665 m s^{-2}$	(exact)
‘As-maintained’ electrical units			
BIPM maintained ohm, Ω_{89-BI} : $\Omega_{BIS5} \equiv \Omega_{89-BI}(1985 \text{ Jan 1})$	Ω_{BIS5}	$0.999998437(50) \Omega$	0.050
Drift rate: $d\Omega_{89-BI}/dt$		$-0.0566(15) \mu\Omega/a$	—
BIPM maintained volt: $2e/h \equiv 483594.0 GHz/V_{76-BI}$		$0.99999241(30) V$	0.30
BIPM maintained ampere: $A_{BIPM} = V_{76-BI}/\Omega_{89-BI}$	A_{BIS5}	$0.99999397(30) A$	0.30
X-ray standards			
x-unit: $\lambda(Cu K\alpha_1)/1537.400$	xu(Cu)	$1.00207789(70) \times 10^{-13} m$	0.70
x-unit: $\lambda(Mo K\alpha_1)/707.831$	xu(Mo)	$1.00209938(45) \times 10^{-13} m$	0.45
\dot{A}^* : $\lambda(W K\alpha_1)/0.209100$	\dot{A}^*	$1.00001481(92) \times 10^{-10} m$	0.92

Table 11. Expanded matrix of variances, covariances and correlation coefficients for the 1986 recommended set of fundamental physical constants.

The elements of the variance matrix appear on and above the major diagonal in (parts in 10^8)²; correlation coefficients appear in *italics* below the diagonal. The variances and covariances given here have been rounded from those given in CODATA Bulletin No. 63.

The correlation coefficient between m_e and N_A appears as -1.000 in this table because the auxiliary constants were considered to be exact in carrying out the least-squares adjustment. When the uncertainties of m_p/m_e and M_p are properly taken into account, the correlation coefficient is -0.999 and the variances of m_e and N_A are slightly increased.

	α^{-1}	e	h	m_e	N_A	F	μ_μ/μ_p
α^{-1}	20	-31	-41	-1	1	-29	33
e	-0.226	921	1812	1750	-1750	-829	-50
h	-0.154	0.997	3582	3500	-3500	-1688	-67
m_e	-0.005	0.975	0.989	3497	-3497	-1747	-2
N_A	0.005	-0.975	-0.989	-1.000	3497	1747	2
F	-0.217	-0.902	-0.931	-0.975	0.975	917	-48
μ_μ/μ_p	0.498	-0.112	-0.077	-0.002	0.002	-0.108	215