

# Conception, Definition and Realization of Time Scale in GNSS

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# Time Conceptions

## ➤ What is Time?

- a significant, challenging question for all philosophers and scientists

Plato, Aristotle, Kant, Newton, Einstein...

## ➤ Newtonian Time

**absolute**, independent to any observer /space

same for everyone and everywhere

## ➤ Relativistic Time

**relative**, dependent to the observer/space

( space and time are merged into spacetime)

different observers have different times for an event, also for a time interval between two events.

so called "**proper time**" of observer

# Time Conceptions

## ➤ Coordinate Time

a **timelike variable**, or a special observer's proper time. defined for a spacetime coordinate system.

**different reference systems have different time coordinates.** such as: TCG, TT for geocentric coordinate systems, and TCB, TDB for solar barycentric coordinate systems

A public time standard must be a coordinate time.

# Time Definitions

## ➤ The Geocentric coordinate Time(TCG)

**coordinate time** of non-rotating geocentric reference systems

~ proper time of the geocenter assumed with no earth gravitational field

## ➤ The Terrestrial Time(TT)

**coordinate time** of non-rotating geocentric reference system, different to TCG by a scale factor

$$dT_T/dT_{CG} \equiv 1 - L_G \quad L_G \equiv 6.969290134 \times 10^{-10}$$

~ proper time of the Geocenter assumed with a gravity potential just like on the geoid (or mean sea level )

# Time Definitions

## ➤ SI second

- ✓ **UT second** (before 1960)

the fraction  $1/86\,400$  of the mean solar day

- ✓ **ET second**(1960,CGPM 11, Resolution 9)

the fraction  $1/31,556,925.9747$  of the tropical year for 1900 January 0 at 12 hours ephemeris time.

# Time Definitions

## ➤ SI second

### ✓ Atomic Second

(1967/1968, CGPM 13, Resolution 1)

The second is the duration of 9 192 631 770 periods of the radiation corresponding to the transition between the two hyperfine levels of the ground state of the caesium 133 atom.

*It was designed for continuity with ET*

in 1997 the CIPM affirmed that:

The definition refers to a caesium atom at rest at a temperature of 0 K.

# Time Definitions

## ➤ SI second

### ✓ TAI second

Atomic Second on the geoid(mean sea level)

The second is the duration of 9 192 631 770 periods of the radiation corresponding to the transition between the two hyperfine levels of the ground state of the caesium 133 atom at rest on the geoid at a temperature of 0 K .



# Time Realizations

## ➤ Apparent Solar Time

-apparent solar position on the sky.

basic time unit: **solar day**, **tropical year**

*easy to observe, but not uniform*

*dependent to the position observer*



Sundial, Palace Museum



built in 1279



# Time Realizations

➤ **Mean Solar Time (*Universal Time*)**

basic unit: **mean solar day** , referred to a **fictitious "mean sun"**

*local time and Universal Time , Time Zone  
more uniform than the aparent solar time , but still has  
irregularity caused by the earth rotation*

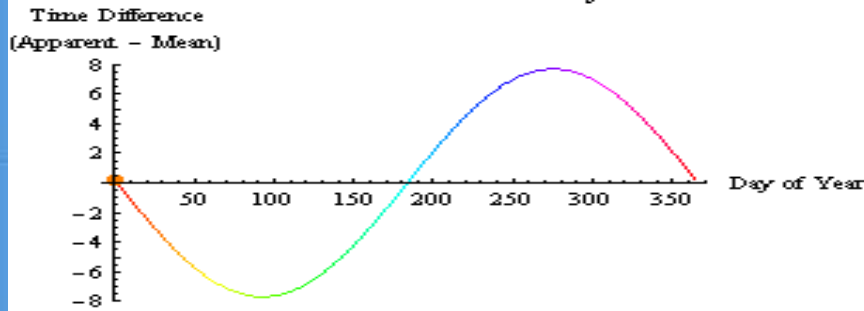
***uncertainty: 1E-8***

➤ **Equation of Time**

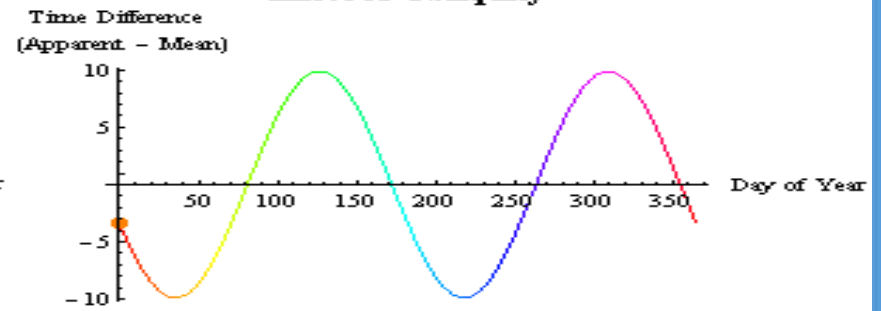
diference of solar time to mean solar time

$$(T_{\ominus} - T_{\ominus}) \in (-14^{\text{m}}15^{\text{s}}, +16^{\text{m}}25^{\text{s}})$$

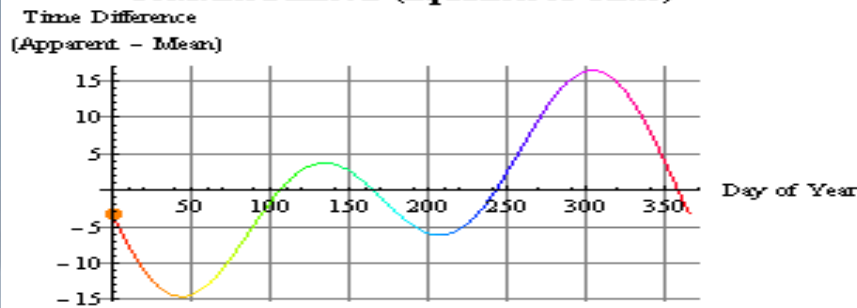
### Effect of Orbit Eccentricity



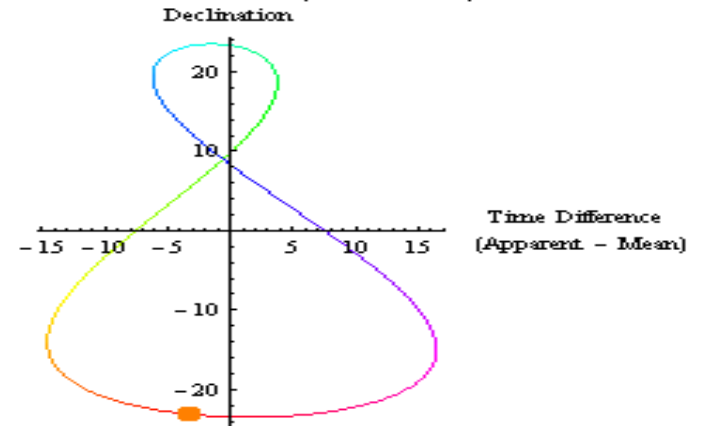
### Effect of Obliquity



### Combined Effects (Equation of Time)



### Sun Position Trace (Analemma)



Wikipedia,

# Time Realizations

## ➤ Ephemeris Time (ET)

adopted in 1952 by the IAU and superseded in the 1970s.

basic unit: **ET second**

***in order to define a uniform time based on Newtonian theory, but affected by observation errors.***

*Although ET is no longer directly in use, it leaves a **continuing legacy**. Its successor time scales, such as TT, TAI, were designed with a relationship that "provides continuity with ephemeris time". it was used for the calibration of atomic clocks in the 1950s.*

# Time Realizations

## ➤ International Atomic Time(TAI)

running since 1958

basic unit: **SI second**, *with a relationship to ET  
using an ensemble of atomic clocks spread over the  
world*

*to match the rate of proper time on the geoid*

*more precisely uniform than ET,  
the best realization of TT*

$$TT = TAI + 32.184s$$

***uncertainty***:  $< 1E-14$

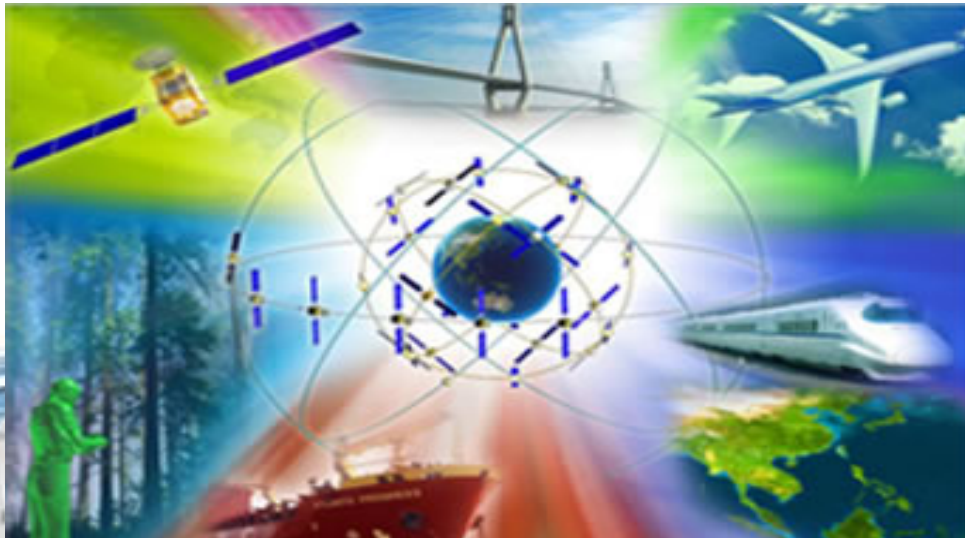
# GNSS Times

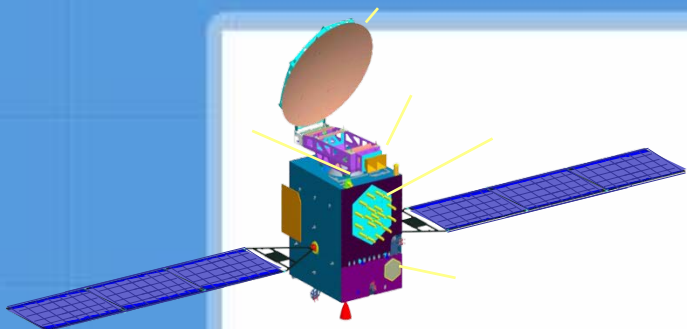
## ➤ Work principle

*three segments:* space segment (satellite constellation), ground control segment (a master station, uplink stations and monitor stations) and user segment (user receivers).

*basic observables:* pseudo-ranges.

*navigation information:* satellite orbits, clock offsets and ionospheric time delay





# GNSS Times

## ➤ System Time

The coordinate time of geocentric reference systems: **TT**

basic unit: **SI second**

*Time synchronization based on TT*

*GNSS Times, such as **GPST**, **BDT** are realizations of TT.*

$$GPST \cong TAI - 19s = TT - 51.184s$$

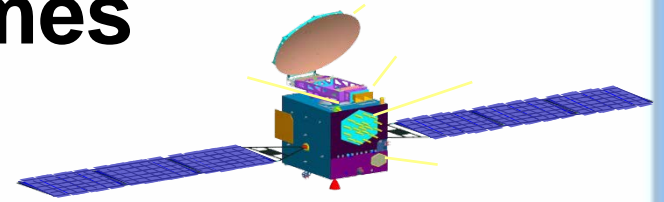
(uncertainty: <30ns)

$$BDT \cong TAI - 33s = TT - 65.184s$$

(uncertainty: <100ns)



# GNSS Times



## ➤ Time Service

**Standard Time :UTC**

**Nav. Data: UTC parameters**

number of leap seconds:  $\Delta t_{LS}$

time offset parameters ( modulo 1s)

$$\Delta t_{ST} = T_{GNSS} - UTC = A_0 + A_1 (T - T_0)$$

$$UTC = T_{GNSS} - \Delta t_{LS} - \Delta t_{ST}$$

*for example:*

$$UTC (USNO) = GPST - \Delta t_{LS}^{GPS} - \Delta t_{ST}^{GPS}$$

$$UTC (BSNC) = BDT - \Delta t_{LS}^{BDS} - \Delta t_{ST}^{BDS}$$

$$(UTC(BSNC) - UTC < 100ns)$$

*BSNC: Beijing Satellite Navigation Center*

# Time Standards

## ➤ Coordinated Universal Time (UTC)

an atomic time scale designed to approximate UT1.

basic unit: **SI second**

*differs from TAI by an integral number of seconds.  
kept within 0.9 s of UT1 by the introduction of leap  
second*

*up to day*

$$UTC=TAI-35s$$

## ➤ Standard time

**civil time in a region**, deviates a fixed, usually a whole number of hours from UT1, now usually UTC.

The offset is chosen such that a new day starts approximately while the sun is at the nadir (midnight)

# The Variability of UT1

- The variety of UT1 referred to TT

$$\Delta T = UT1 - TT = a + b t + c t^2$$

**note:**

$b, c$  not invariable constant !

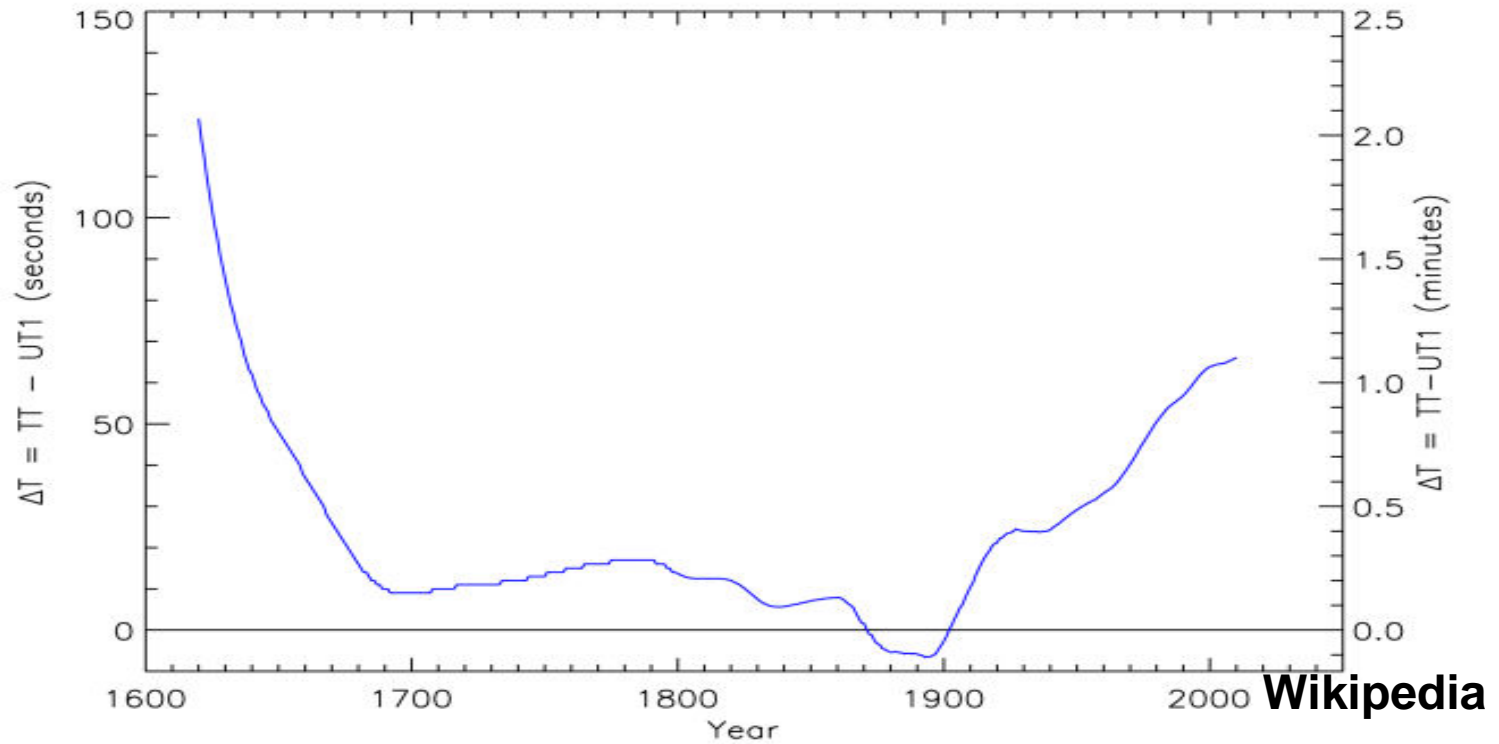
$\Delta T$  not predictable in fine detail

***There **no ways** to give a rigorous relationship between UT1 and TT.***

# The Variability of UT1

## ➤ The observed results

$\Delta T = \text{Terrestrial Time (TT)} - \text{Universal Time (UT1)}$



Wikipedia

Observed values of  $\Delta T = TT - UT1$  (seconds)  
 (values before 1955.5 based on  $n' = 26.0$  "/cy/cy)

**Wikipedia,**

year	+0	+1	+2	+3	+4	+5	+6	+7	+8	+9
1890	-5.87	-6.01	-6.19	-6.64	-6.44	-6.47	-6.09	-5.76	-4.66	-3.74
1900	-2.72	-1.54	-0.02	1.24	2.64	3.86	5.37	6.14	7.75	9.13
1910	10.46	11.53	13.36	14.65	16.01	17.20	18.24	19.06	20.25	20.95
1920	21.16	22.25	22.41	23.03	23.49	23.62	23.86	24.49	24.34	24.08
1930	24.02	24.00	23.87	23.95	23.86	23.93	23.73	23.92	23.96	24.02
1940	24.33	24.83	25.30	25.70	26.24	26.77	27.28	27.78	28.25	28.71
1950	29.15	29.57	29.97	30.36	30.72	31.07	31.35	31.68	32.18	32.68
1960	33.15	33.59	34.00	34.47	35.03	35.73	36.54	37.43	38.29	39.20
1970	40.18	41.17	42.23	43.37	44.49	45.48	46.46	47.52	48.53	49.59
1980	50.54	51.38	52.17	52.96	53.79	54.34	54.87	55.32	55.82	56.30
1990	56.86	57.57	58.31	59.12	59.99	60.78	61.63	62.30	62.97	63.47
2000	63.83	64.09	64.30	64.47	64.57	64.69	64.85	65.15	65.46	65.78
2010	66.07	67.1(8)	68(1)	68(2)	69(2)	69(3)	70(4)	70(4)	-	-
year	+0	+1	+2	+3	+4	+5	+6	+7	+8	+9

➤ **The predictor formula (F Espenak & J Meeus,2006 )**

1900 to 1920	$-2.79 + 149.4119 u - 598.939 u^2 + 6196.6 u^3$	$(\text{year} - 1900)/100$
1920 to 1941	$+21.20 + 84.493 u - 761.00 u^2 + 2093.6 u^3$	$(\text{year} - 1920)/100$
1941 to 1961	$+29.07 + 40.7 u - u^2/0.0233 + u^3/0.002547$	$(\text{year} - 1950)/100$
1961 to 1986	$+45.45 + 106.7 u - u^2/0.026 - u^3/0.000718$	$(\text{year} - 1975)/100$
1986 to 2005	$+63.86 + 33.45 u - 603.74 u^2 + 1727.5 u^3 + 65181.4 u^4 + 237359.9 u^5$	$(\text{year} - 2000)/100$
2005 to 2050	$+62.92 + 32.217 u + 55.89 u^2$	$(\text{year} - 2000)/100$
2050 to 2150	$-205.72 + 56.28 u + 32 u^2$	$(\text{year} - 1820)/100$



# On The Future of UTC

## ➤ Questions and discussions

- ✓ Do we really need a uniform time scale as the standard time which is close enough with the solar time(UT1) ?

**yes, certainly**

- ✓ How much difference between UTC and UT1 can be tolerated?

**□ time difference:**

**1 minute or 10 minutes?**

**□ frequency deviation?**

**1E-6, 1E-7 or 1E-8?**

# On The Future of UTC

➤ **What method is better to make them consistent?**

□ **time adjustment:**

leap second, leap minute, leap hour?

□ **frequency adjustment:**

adjustment the frequency offset within a **certain range** at a fixed time?

# On The Future of UTC

## ➤ Personal suggestions:

- ✓ Stop the leap second
- ✓ Maintain the continuity of UTC
- ✓ Adjust the frequency of UTC once a century, and keep the unit of UTC to be consistent with that of UT1 within 1E-7.

Define UTC in the form:

$$\text{UTC} = (1 - L_{\text{cyi}})(\text{TT} - \text{TT}_{\text{cyi}}) + a_{\text{cyi}}$$

# On The Future of UTC

➤ **Personal suggestions:**

and  $L_{cyi}$  **Satisfies:**

$$\left| \frac{dUT1}{dT} + L_{cyi} - 1 \right| \leq 1E-7?$$

**In this century,** we can simply let

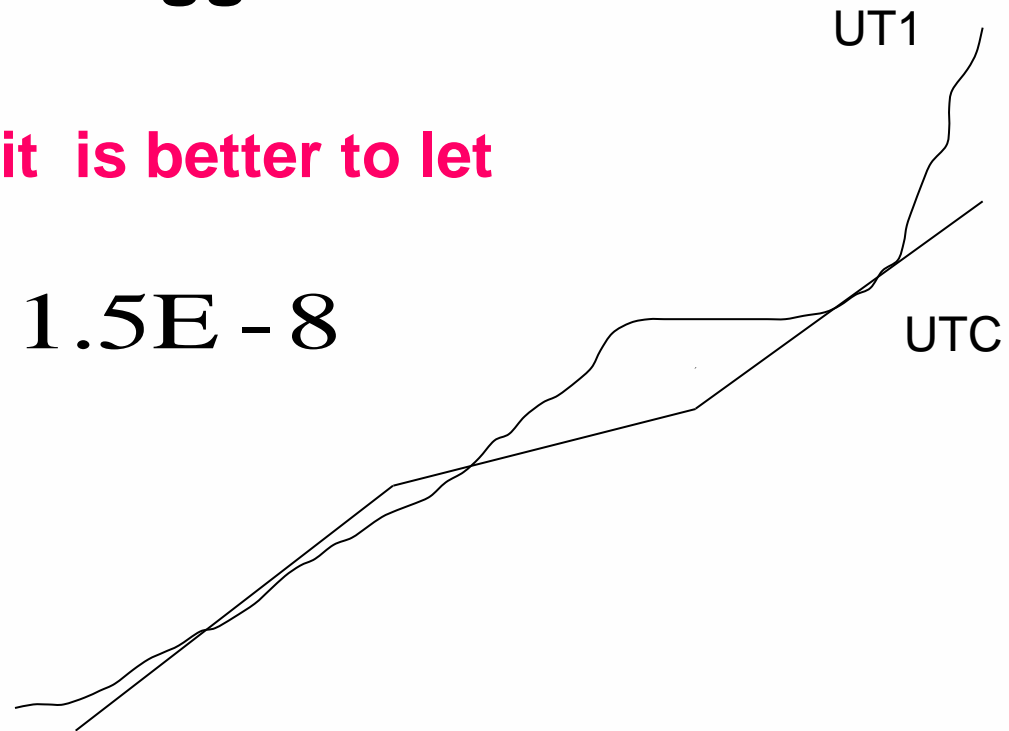
$$UTC = TT - 67.184s = TAI - 35s$$

# On The Future of UTC

➤ **Personal suggestions:**

**Maybe it is better to let**

$$L_{21} = 1.5E - 8$$



# Primary viewpoints

- (1) A continuous and uniform time scale is the essential goal of science and technology. The evolution of standard time from the apparent solar time to the mean solar time, and to UTC fully revealed the desire of human being.**
- (2) The negative impacts of the irregular insertion of leap seconds are increasing with the development of computer and automation technology. So the requirement for eliminating leap seconds is not only urgent but also reasonable.**



# Primary viewpoints

- (3) Though the evolution of standard time is an inevitable trend with the development of time scale, but the redefinition of UTC should be treated with caution, seeking benefits and avoiding disadvantages.**
- (4) As a base of world-wide time standard, UTC must have the coordinate function for UT1 and TAI, so the name and continuity of UTC should not be changed.**

# Primary viewpoints

- (5) Uniform and close to the solar time are important requirements for civil time. Then the definition and realization of standard time must keep some relations to the mean solar time.**
- (6) The elimination of leap seconds will break UTC the close relation to UT1. But as an approximation of UT1, UTC is used in many fields, such as astronomy, geodesy, space activities, then some online software should be updated.**

# Primary viewpoints

- (7) Global navigation satellite systems should disseminate the earth orientation parameters, include the UT1 parameter.**
- (8) The elimination of leap seconds maybe have no negative impacts on the operation of Beidou system, it is convenient not only to the operator, but also to the users.**



**Thank you  
for your attention**